

INSTITUTE OF AERONAUTICAL ENGINEERING

(Autonomous)

B.Tech I/II Semester Supplementary Examinations - July, 2017 Regulation: IA-R16

COMPLEX ANALYSIS AND PROBABILITY DISTRIBUTION

[II Semester - (Electronics and Communication Engineering)]

Time: 3 Hours

Max Marks: 70

Answer ONE Question from each Unit All Questions Carry Equal Marks All parts of the question must be answered in one place only

$\mathbf{UNIT} - \mathbf{I}$

1.	(a) Show that the function $f(z) = \overline{z}$ is continuous at all z but not differentiable anywhere.	[7M]
	(b) Find all values of k, such that $f(z) = e^x (\cos ky + i \sin ky)$ is analytic.	[7M]
2.	(a) If $v(r,\theta) = r^2 \cos 2\theta - r \cos \theta + 2$ find the analytic function $f(z) = u(r,\theta) + iv(r,\theta)$.	[7M]
	(b) If $(z) = u + i u i z$ analytic prove that $\left(\frac{\partial^2}{\partial z} + \frac{\partial^2}{\partial z} \right) \text{Real } f(z) ^2 = 2 f'(z) ^2$	[7]]

(b) If
$$(z) = u + iv$$
 is analytic prove that $\left(\frac{\partial^2}{\partial x^2} + \frac{\partial^2}{\partial y^2}\right) |\text{Real } f(z)|^2 = 2|f'(z)|^2$. [7M]

$\mathbf{UNIT}-\mathbf{II}$

(b) Evaluate
$$\int_{C} \frac{e^z}{(z-1)(z-4)} dz$$
, where C: $|z| = 2$. [7M]

4. (a) Evaluate
$$\int_{1-i}^{2+i} (2x + iy + 1) dz$$
 along
i. $x = t + 1, y = 2t^2 - 1$ [7M]

ii. Straight line joining the points 1-i and 2+i

(b) Verify Cauchy theorem for the function $f(z) = Ze^{-Z}$ over the unit circle with Centre as origin.

[7M]

$\mathbf{UNIT}-\mathbf{III}$

5. (a) Write Laurent's series expansion of $f(z) = \frac{1}{(z^2-4z+3)}$ in powers of for [7M] i. |z| < 1ii. 1 < |z| < 3 2π

(b) Evaluate
$$\int_{0}^{2\pi} \frac{d\theta}{2-\sin\theta}$$
 by residue theorem. [7M]

- 6. (a) Find the bilinear transformation which maps the points z = 1, i, -1 onto the points w = i, 0, -i. [7M]
 - (b) Find the poles and residues at each pole of $f(z) = \frac{2z+1}{1-z^4}$. [7M]

$\mathbf{UNIT}-\mathbf{IV}$

- 7. (a) The distribution function of a random variable X is given by, $f(x) = 1 (1 + x)e^{-x}$, x>0. Find the density function, mean and Variance. [7M]
 - (b) Find the MGF of a random Variable with $p(x) = pq^{x-1}, x = 1, 2, 3, \ldots$ and hence find mean and Variance. [7M]
- 8. (a) A perfect coin is tossed twice. Find the MGF of the number of heads. Find Mean and Variance.
 [7M]
 - (b) Probability density function of a continuous random variable is $f(x) = e^{-x}$, x > 0, find the third moment about the mean. [7M]

$\mathbf{UNIT}-\mathbf{V}$

- 9. (a) It has been claimed that in 60% of all solar heat installations the utility bill is reduced by at least one-third. Accordingly, what are the probabilities that the utility bill will be reduced by at least one-third in [7M]
 - i. four of five installations
 - ii. at least four of five installations.
 - (b) Derive mean of the normal distribution.
- 10. (a) The number of telephone lines busy at any instant of time is a binomial Variate with Probability 0.1, that the line is busy. If 10 lines are chosen at random, what is the probability that: **[7M]**
 - i. No line is busy.
 - ii. All lines are busy.
 - iii. At least one line is busy.
 - (b) An air line knows that 5% of the people making reservations on a certain flight will not turn up. Consequently their policy is to sell 52 tickets for a flight that can only hold 50 passengers what is the probability that there will be a seat for every passenger who turns up? [7M]

 $-\circ\circ\bigcirc\circ\circ-$

[7M]