

## DISCRETE MATHEMATICAL STRUCTURES

<b>III Semester: CSE / IT</b>								
Course Code	Category	Hours / Week			Credits	Maximum Marks		
ACSB04	<b>Core</b>	L	T	P	C	CIA	SEE	Total
		3	1	0	4	30	70	100
<b>Contact Classes: 45</b>		<b>Tutorial Classes: 15</b>		<b>Practical Classes: Nil</b>			<b>Total Classes: 60</b>	

  

**COURSE OBJECTIVES:**

**The course should enable the students to:**

- Describe the logical and mathematical foundations, and study abstract models of computation.
- Illustrate the limitations of predicate logic.
- Define modern algebra for constructing and writing mathematical proofs.
- Solve the practical examples of sets, functions, relations and recurrence relations.
- Recognize the patterns that arise in graph problems and use this knowledge for constructing the trees and spanning trees.

**COURSE OUTCOMES (COs):**

CO 1 : To understand the concepts associated with Mathematical Logic and Predicate calculus  
 CO 2 : Ability to learn the basic concepts about relations, functions and to draw different diagrams like Lattice, Hasse diagrams.  
 CO 3 : To understand the concepts of Algebraic Structures and combinatorics.  
 CO 4 : To describe various types of recurrence relations and the methods to find out their solutions.  
 CO 5 : To understand the basic concepts associated with Graphs and Trees.

**COURSE LEARNING OUTCOMES (CLOs):**

- Understand logical connectives and compound prepositions for building compound statements.
- Learn the formal symbols and use the preposition logic and predicate logic to solve problems on logical equivalences and implications.
- Memorize different scientific notations to simplify the logical statements.
- Prepare valid arguments from the given propositional statements by using rules of inference.
- Identify ordered pairs to form a binary relation from the given sets.
- Construct directed graph and a matrix representation using a binary relation on finite order pairs.
- Identify the properties of relations to check for equivalence relation and partial order relation and compute relations using operations on relations.
- Construct a hasse diagram to recognize the relevant partial ordered sets from the given binary relation.
- Describe the types of functions (one to one, on-to, bijective, Identity and constant function).
- Implement the concept of the inverse and recursive functions to get solution for an appropriate problem.
- Use the concept of lattices (Greatest Lower Bound (GLB) and Least Upper Bound (LUB) to represent a defined finite set in multi-dimension applications.
- Explain about the properties and types of lattices (bounded and distributive lattice)
- Construct different algebraic structures by using concepts of groups, sub groups, monoids and rings.
- Understand binomial and multinomial theorem to compute the coefficients for the given expansions.
- Understand the concept of homomorphism and isomorphism of semi-groups.
- Analyze the given sets by using inclusion and exclusion principle.
- Identify the different counting techniques (permutations) related to mathematics and computer science.
- Solve discrete probability and set problems by using permutations and combinatorics.
- Identify the series of expansion to represent the sequence by using generating functions.
- Identify the general solution for first-order and second-order linear homogeneous recurrence relations.
- Identify the roots of second and higher order linear non-homogeneous recurrence relations.
- Understand the use of graphs and trees as representation tools in a variety of context
- Identify Euler's and Hamilton rule for a simple connected graph in NP-complete problems.
- Construct a spanning tree by using search techniques (Depth First Search and Breadth First Search).
- Construct a minimal spanning tree by using Kruskal's and Prim's algorithm to obtain a solution for a real time problem.
- Possess the knowledge and skills for employability and to succeed in national and international level competitive exams.

<b>MODULE-I</b>	<b>MATHEMATICAL LOGIC AND PREDICATES</b>	<b>Classes: 09</b>
Mathematical logic: Statements and notations, connectives, well-formed formulas, truth tables, tautology, equivalence implication; Normal forms: Disjunctive normal forms, conjunctive normal forms, principle disjunctive normal forms, principle conjunctive normal forms; Predicate calculus: Predicative logic, statement functions, variables and quantifiers, free and bound variables, rules of inference, consistency, proof of contradiction, automatic theorem proving.		
<b>MODULE-II</b>	<b>RELATIONS, FUNCTIONS AND LATTICES</b>	<b>Classes: 09</b>
Relations: Properties of binary relations, equivalence, compatibility and partial ordering relations, lattices, Hasse diagram; Functions: Inverse function, composition of functions, recursive functions; Lattices: Lattices as partially ordered sets; Definition and examples, properties of lattices, sub lattices, some special lattices.		
<b>MODULE-III</b>	<b>ALGEBRAIC STRUCTURES AND COMBINATORICS</b>	<b>Classes: 09</b>
Algebraic structures: Algebraic systems, examples and general properties, semi groups and monoids, groups, sub groups, homomorphism, isomorphism, rings. Combinatory: The fundamental counting principles, permutations, disarrangements, combinations, permutations and combinations with repetitions, the binomial theorem, multinomial theorem, generalized inclusion exclusion principle.		
<b>MODULE-IV</b>	<b>RECURRENCE RELATIONS</b>	<b>Classes: 09</b>
Recurrence relation: Generating functions, function of sequences calculating coefficient of generating function, recurrence relations, solving recurrence relation by substitution and generating functions, characteristics roots solution of homogeneous recurrence relation.		
<b>MODULE-V</b>	<b>GRAPHS AND TREES</b>	<b>Classes: 09</b>
Graphs: Basic concepts of graphs, isomorphic graphs, Euler graphs, Hamiltonian graphs, planar graphs, graph coloring, digraphs, directed acyclic graphs, weighted digraphs, region graph, chromatic numbers; Trees: Trees, spanning trees, minimal spanning trees.		
<b>Text Books:</b>		
<ol style="list-style-type: none"> <li>1. J. P. Tremblay, R. Manohar, -Discrete Mathematical Structures with Applications to Computer Science, Tata McGraw Hill, India, 1<sup>st</sup> Edition, 1997.</li> <li>2. Joe L. Mott, Abraham Kandel, Theodore P. Baker, -Discrete Mathematics for Computer Scientists and Mathematicians, Prentice Hall of India Learning Private Limited, New Delhi, India, 2<sup>nd</sup> Edition, 2010.</li> </ol>		
<b>Reference Books:</b>		
<ol style="list-style-type: none"> <li>1. Kenneth H. Rosen, -Discrete Mathematics and Its Applications, Tata McGraw-Hill, New Delhi, India, 6<sup>th</sup> Edition, 2012.</li> <li>2. C. L. Liu, D. P. Mohapatra, -Elements of Discrete Mathematics, Tata McGraw-Hill, India, 3<sup>rd</sup> Edition, 2008.</li> <li>3. Ralph P. Grimaldi, B. V. Ramana, -Discrete and Combinatorial Mathematics - An Applied Introduction, Pearson Education, India, 5<sup>th</sup> Edition, 2011.</li> <li>4. D. S. Malik, M.K. Sen, -Discrete Mathematical Structures: Theory and Applications, Thomson Course Technology, India, 1<sup>st</sup> Edition, 2004.</li> </ol>		
<b>Web References:</b>		
<ol style="list-style-type: none"> <li>1. <a href="http://www.web.stanford.edu/class/cs103x">http://www.web.stanford.edu/class/cs103x</a></li> <li>2. <a href="http://www.cs.odu.edu/~cs381/cs381content/web_course.html">http://www.cs.odu.edu/~cs381/cs381content/web_course.html</a></li> <li>3. <a href="http://www.cse.iitd.ernet.in/~bagchi/courses/discrete-book">http://www.cse.iitd.ernet.in/~bagchi/courses/discrete-book</a></li> <li>4. <a href="http://www.saylor.org/course/cs202/">http://www.saylor.org/course/cs202/</a></li> <li>5. <a href="http://www.nptel.ac.in/courses/106106094/">http://www.nptel.ac.in/courses/106106094/</a></li> <li>6. <a href="http://www.tutorialspoint.com/discrete_mathematics">http://www.tutorialspoint.com/discrete_mathematics</a></li> <li>7. <a href="http://www.dmtcs.org/dmtcs-ojs/index.php/dmtcs">http://www.dmtcs.org/dmtcs-ojs/index.php/dmtcs</a></li> </ol>		

**E-Text Books:**

1. <https://people.eecs.berkeley.edu/~daw/teaching/cs70-s05/>
2. <http://home.anadolu.edu.tr/~eakyar/dersler/ayrik/kitap/kitap.pdf>
3. <http://45.63.83.30/graph-theory-keijo-ruohonen-pdf-tut.pdf>
4. <http://www.zib.de/groetschel/teaching/WS1314/BondyMurtyGTWA.pdf>