INSTITUTE OF AERONAUTICAL ENGINEERING
(Autonomous)
Dundigal, Hyderabad - 500043
CIVIL ENGINEERING
COURSE DESCRIPTION

| Course Title | MATHEMATICS-II |  |  |  |
| :--- | :---: | :---: | :---: | :---: |
| Course Code | A30006 |  |  |  |
| Course Structure | Lectures | Tutorials | Practicals | Credits |
|  | 4 | 1 | - | 4 |
| Course Coordinator | Mr. Ch. Kumara Swamy, Asst Professor |  |  |  |
| Team of Instructors | Dr. M. Anita, Professor <br> Mr. Ch. Kumara Swamy, Asst Professor <br> Ms. K.. Rama Jyothi, Asst Professor |  |  |  |

## I. COURSE OVERVIEW

The course focuses on more advanced Engineering Mathematics topics which provide with the relevant mathematical tools required in the analysis of problems in engineering and scientific professions. The course includes vector calculus, Fourier series and transform, Interpolation, curve fitting, numerical techniques and boundary value problems. The mathematical skills derived from this course form a necessary base to analytical and design concepts encountered in the program.

## II. PREREQUISITE(S)

| Level | Credits | Periods | Prerequisite |
| :---: | :---: | :---: | :---: |
| UG | 4 | 5 | Basic mathematics, calculus. |

## III. MARKS DISTRIBUTION

| Sessional Marks | University End <br> Exam Marks | Total <br> Marks |
| :--- | :---: | :---: |
| There shall be 2 midterm examinations. Each midterm examination consists of <br> subjective test. The subjective test is for 20 marks, with duration of 2 hours. <br> Subjective test of each semester shall contain 5 one mark compulsory questions <br> in part-A and part-B contains 5 questions, the student has to answer 3 <br> questions, each carrying 5 marks. |  |  |
| First midterm examination shall be conducted for the first two and half units of <br> syllabus and second midterm examination shall be conducted for the remaining <br> portion. <br> Five marks are earmarked for assignments. There shall be two assignments in <br> every theory course. Marks shall be awarded considering the average of two <br> assignments in each course. | 75 | 100 |

## IV. EVALUATION SCHEME

| S.No | Component | Duration | Marks |
| :---: | :---: | :---: | :---: |
| 1 | I Mid examination | 90 minutes | 20 |
| 2 | I Assignment | -- | 05 |
| 3 | II Mid examination | 90 minutes | 20 |
| 4 | II Assignment | -- | 05 |
| 5 | External examination | 3 hours | 75 |

## V. COURSE OBJECTIVES

The goal of this course is to provide students with better understanding of and preparation for mathematics which are applicable in most of engineering branches.

## At the end of the course, the students will be able to:

I. Analyze scalar and vector fields and compute the gradient, divergence and curl. They should be able to evaluate line, surface and volume integrals.
II. Develop functions in a Fourier series and Fourier transforms
III. Apply numerical methods to interpolate, extrapolate, differentiate and integrate functions IV. Solve differential equation using numerical methods and solve systems of equations.

## VI. COURSE OUTCOMES

After completing this course the student must demonstrate the knowledge and ability to:

1. Analyze scalar and vector fields and compute the gradient, divergence and curl.
2. Evaluate line, surface and volume integrals.
3. Apply Green's Theorem, Divergence Theorem and Stoke's theorem to evaluate integrals.
4. Demonstrate Dirichlet's conditions by using them to evaluate infinite series
5. Explain fundamental understanding of Fourier series and be able to give Fourier expansions of a given function
6. Determine the Fourier transform of elementary functions from the definition
7. Compute the intermediate point for the data and find the most appropriate formula for a guessed relation of the data variables
8. Solve the model by selecting and applying a suitable mathematical method
9. Explain errors involved in computations and to estimate the errors
10. Solve algebraic and transcendental equations using Bisection method, Regula-falsi method and Newton-Raphson method
11. Solve systems of equations by Crout's, Jacobi and gauss-seidel methods.
12. Apply numerical methods to interpolate, extrapolate integrate functions.
13. Solve differential equation using numerical methods.(Taylor's series, Euler's, Picard's and RungeKutta method up to 4th order)
14. Apply power method to find the Eigen values of the given matrix

## VII. HOW PROGRAM OUTCOMES ARE ASSESSED

| Program Outcomes | Level | Proficiency <br> assessed by |  |
| :--- | :--- | :---: | :---: |
| PO1 | Capability to apply the knowledge of Mathematics, science and Engineering <br> in the field of Mechanical Engineering | H | Assignments, <br> Tutorials |


| PO2 | An Ability to analyze complex engineering problems to arrive at relevant conclusions using knowledge of Mathematics, Science and Engineering. | H | Assignments |
| :---: | :---: | :---: | :---: |
| PO3 | Competence to design a system, component or process to meet societal needs within realistic constraints. | H | Assignments |
| PO4 | To design and conduct research oriented experiments as well as to analyze and implement data using research methodologies | S | Assignments |
| PO5 | An ability to formulate solve complex engineering problem using modern engineering and Information technology tools. | S | -- |
| PO6 | To utilize the engineering practices, techniques, skills to meet needs of the health, safety, legal, cultural and societal issues. | S | -- |
| PO7 | To understand impact of engineering solutions in the societal context and demonstrate the knowledge for sustainable development | N | -- |
| PO8 | An understanding and implementation of professional and Ethical responsibilities | N | -- |
| PO9 | To function as an effective individual and as a member or leader in Multidisciplinary environment and adopt in diverse teams | N | -- |
| PO10 | An ability to assimilate, comprehends, communicate, give and receive instructions to present effectively with engineering community and society | N | -- |
| PO11 | An ability to provide leadership in managing complex engineering projects at multi-disciplinary environment and to become a professional engineer. | N | -- |
| PO12 | Recognition of the need and an ability to engage in lifelong learning to keep abreast with technological changes. | N | -- |

## VIII. HOW PROGRAM SPECIFIC OUTCOMES ARE ASSESSED

| Program Specific Outcomes |  | Level | Proficiency <br> Assessed by |
| :--- | :--- | :---: | :---: |
| PSO 1 | UNDERSTANDING: To produce engineering professional capable of <br> synthesizing and analyzing mechanical systems including allied engineering | S | Lectures and <br> Assignments |
| PSO 2 | ANALYTICAL SKILLS: An ability to adopt and integrate current technologies <br> in the design and manufacturing domain to enhance the employability | S | Guest <br> Lectures |
| PSO 3 | BROADNESS: To build the nation, by imparting technological inputs and <br> managerial skills to become Technocrats | S | Assignments |

N - None
S - Supportive
H - Highly Related

## IX. SYLLABUS

## UNIT - I

## Vector Calculus

Scalar point function and vector point function, Gradient- Divergence- Curl and their related properties. Solenoidal and irrotational vectors- Finding Potential function. Laplacian operator, Line integral - work done - Surface integrals - Volume integral. Green's Theorem, Stoke's theorem and Gauss's Divergence Theorems (Statement \& their Verification).

UNIT - II
Fourier series and Fourier Transforms
Fourier series: Definition of periodic function. Fourier expansion of periodic functions in a given interval of length $2 \pi$ Determination of Fourier coefficients - Fourier series of even and odd functions - Fourier series in an arbitrary interval - even and odd periodic continuation - Half-range Fourier sine and cosine expansions

Fourier Transforms: Fourier integral theorem - Fourier sine and cosine integrals. Fourier transforms - Fourier sine and cosine transforms- properties - inverse transforms - Finite Fourier transforms.

UNIT - III
Interpolation and Curve fitting
Interpolation: Introduction- Errors in Polynomial Interpolation - Finite differences- Forward DifferencesBackward differences - Central differences - Symbolic relations and separation of symbols- Difference Equations Differences of a polynomial-Newton's formulae for interpolation - Central difference interpolation Formulae Gauss Central Difference Formulae -Interpolation with unevenly spaced points-Lagrange's Interpolation formula.

Curve fitting: Fitting a straight line -Second degree curve-exponential curve-power curve by method of least squares.

## UNIT - IV: Numerical techniques <br> Solution of Algebraic and Transcendental Equations and Linear system of equations

Introduction - Graphical interpretation of solution of equations. The Bisection Method - The Method of False Position- the Iteration Method - Newton-Raphson Method.

Solving system of non-homogeneous equations by L-U Decomposition method (Crout's Method) Jacobi's and Gauss-Seidel Iteration method

## UNIT - V:

Numerical techniques
Numerical Integration and Numerical solutions of First order differential equations:
Numerical integration - Trapezoidal rule, Simpson's $1 / 3$ rd and $3 / 8$ Rule, Generalized Quadrature
Numerical solution of Ordinary Differential equations: Solution by Taylor's series method -Picard's Method of successive Approximation- single step methods-Euler's Method-Euler's modified method, Runge-Kutta(Second and Classical fourth order)Methods.

Boundary values \&Eigen value Problems
Shooting method, Finite difference method and solving Eigen values problems, power method

## Textbooks:

1. Electric Circuits - A.Chakrabarhty, DhanipatRai\& Sons.
2. Network analysis - N.C Jagan and C. Lakhminarayana, BSpublications.

## Referencebooks:

1. Mathematical Methods by T.K.V. Iyengar, B.Krishna Gandhi \& Others, S. Chand.
2. Introductory Methods by Numerical Analysis by S.S. Sastry, PHI Learning Pvt. Ltd.
3. Mathematical Methods by G.ShankarRao, I.K. International Publications, N.Delhi
4. Advanced Engineering Mathematics with MATLAB, Dean G. Duffy, 3rd Edi, 2013, CRC Press Taylor \&Francis Group.
5. Mathematics for Engineers and Scientists, Alan Jeffrey, 6ht Edi, 2013, Chapman \& Hall/ CRC
6. Advanced Engineering Mathematics, MichaelGreenbreg, SecondEdition,Person Education
7. Mathematics For Engineers By K.B.Datta and M.A.S Srinivas, Cengage Publications

## X. COURSE PLAN:

At the end of the course, the students are able to achieve the following course learning outcomes:

| Lecture No. | Course Learning Outcomes | Topics to be covered | Reference |
| :---: | :---: | :---: | :---: |
| 1 | Introduction to vector calculus | Define vector calculus and vector fields and their properties | T1,R1 |
| 2-4 | Gradient, divergent and curl | Determine Gradient, divergent and curl of vector fields | T1,R1 |
| 5-6 | Line integral | Calculate line integral along smooth path and find work done | T1,R1 |
| 7 | Surface integral | Calculate the surface area of field | T1,R1 |
| 8 | Volume integral | Calculate volume of field | T1,R1 |
| 9 | Green's theorem | Use Green's theorem to evaluate line integrals along simple closed contours on the plane | T1,R1 |
| 10-11 | Stoke's theorem | Use Stokes' theorem to give a physical interpretation of the curl of a vector field | T1,R1 |
| 12-13 | Gauss divergence theorem | Use the divergence theorem to give a physical interpretation of the divergence of a vector field | T1,R1 |
| 14-15 | Fourier series | Define periodic functions and Fourier series and Fourier coefficients | T2,R1 |
| 16-17 | Fourier expansion | Apply Fourier series for ( $0,2 \pi$. ), (- $\pi$, $\pi$ ) | T2,R1 |
| 18-19 | Fourier series of even, odd functions and half range. | Determine even and odd function and apply Fourier series in $(-\pi, \pi)$. and also half range series in $(0, \pi)$. | T2,R1 |
| 20-21 | Fourier series in an arbitrary interval | Determine Fourier series in $(0,2 l)$, $(-l, l)$.and also half range series in $(0, l)$. | T2,R1 |
| 22 | Fourier Transforms <br> Fourier integral theorem, Fourier sine and cosine integrals. | Define and apply Fourier transforms ,Fourier integral theorem , Fourier sine and cosine integrals | T2,R1 |
| 23 | Fourier sine and cosine transforms- properties | Use properties to solve the given functions | T2,R1 |
| 24 | Inverse transforms | Define and apply Inverse transforms | T2,R1 |
| 25 | Finite Fourier transforms | Define and apply Finite Fourier transforms | T2,R1 |


| 26 | Interpolation | Define what interpolation is | T1,R2 |
| :---: | :---: | :---: | :---: |
| 27 | Symbolic relations and separation of symbols | Explain the relation between symbols | T1,R2 |
| 28 | Newton's forward difference | Solve the problems by Newton's forward method | T1,R2 |
| 29-30 | Newton's backward difference | Solve the problems by Newton's backward method | T1,R2 |
| 31 | Gauss forward difference | Solve the problems by Gauss forward method | T1,R2 |
| 32 | Gauss backward difference | Solve the problems by Gauss backward method | T1,R2 |
| 33 | Lagrange's interpolation | Solve the problems by lagrange's method | T1,R2 |
| 34 | Difference equation | Formulate difference equation and solve | T1,R2 |
| 35 | Curve fitting: Fitting straight line | Solve a straight line | T1,R2 |
| 36-37 | Fitting a second degree curve | Solve a second degree parabola | T1,R2 |
| 38-39 | Fitting an exponential curve | Solve an exponential curve | T1,R2 |
| 40 | Fitting a power curve | Solve a power curve | T1,R2 |
| 41-42 | Solution of Algebraic and Transcendental Equations. Introduction | Define algebraic and transcendental equations and Explain graphical solution. | T1,R2 |
| 43 | Bisection Method | Apply bisection method to find the root | T1,R2 |
| 44 | Method of False Position | Apply False Position method to find the root | T1,R2 |
| 46 | Newton-Raphson Method | Apply Newton-Raphson method to find the root | T1,R2 |
| 47-48 | Linear system of equations.Solving system of non-homogeneous equations. L-U Decomposition method | Apply Crout's method to find the solution of square matrix | T1,R2 |
| 49-50 | Jacobi's Iteration method | Solve the linear system of equations by Jacobi's Iteration method | T1,R2 |
| 51-52 | Gauss-Seidel Iteration method | Solve the linear system of equations by Gauss-Seidel Iteration method | T1,R2 |
| 53-54 | Numerical Integration Numerical integration | Calculate integration by Trapezoidal and Simpson's $1 / 3$ and $3 / 8$ rule | T1,R2 |
| 55-56 | Gauss-Legendre one, two and three point | Calculate integration Gauss-Legendre | T1,R2 |


| 57 | Numerical solution of <br> Ordinary Differential <br> equations: <br> Taylor's series method | Solve the ODE by Taylor's series <br> method | T2,R3 |
| :---: | :--- | :--- | :---: |
| 58 | Picard's Method | Solve the ODE by Picard's method | T2,R3 |
| 59 | Euler's Method | Solve the ODE by Euler's Method- Euler's modified <br> method | T2,R3 |
| 60 | Euler's modified method, | Solve the ODE Euler's modified method | T2,R3 |
| 61 | Runge-Kutta Methods | Solve the ODE by Runge-Kutta Methods | $\mathrm{T} 2, \mathrm{R} 3$ |
| 62 | Boundary Value <br> Problems: Shooting <br> method | Solve the BVP by Shooting method | T 3 |
| 63 | Finite difference method | Solve the BVP by Finite difference method | $\mathrm{T}, \mathrm{R} 3$ |
| 64 | Eigen Value Problems: | Solve the Eigen Values Eigen value problems | $\mathrm{T} 2, \mathrm{R} 3$ |
| 65 | Power Method | Solve the Eigen Values by Power method |  |

XI. MAPPING COURSE OBJECTIVES LEADING TO THE ACHIEVEMENT OF THE PROGRAM OUTCOMES

| Course | Program Outcomes |  |  |  |  |  |  |  |  |  |  |  | Program Specific Outcomes |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | PO1 | PO2 | PO3 | PO4 | PO5 | PO6 | PO7 | PO8 | PO9 | PO10 | PO11 | PO12 | PSO1 | PSO2 | PSO3 |
| I | H | H | S | S |  |  |  |  |  |  |  |  | S |  | S |
| II | H | S |  | S |  |  |  |  |  |  |  |  | S |  |  |
| III | H | H | S | S |  |  |  | S |  |  |  |  | S | S |  |
| IV | H | S |  |  |  |  |  |  | S |  |  |  | S | S |  |

XII. MAPPING COURSE OUTCOMES LEADING TO THE ACHIEVEMENT OF TSHE PROGRAM OUTCOMES

| Course | Program Outcomes |  |  |  |  |  |  |  |  |  |  |  | Program Specific Outcomes |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Objectives | PO1 | PO2 | PO3 | PO4 | PO5 | PO6 | PO7 | P08 | PO9 | PO10 | PO11 | PO12 | PSO1 | PSO2 | PSO3 |
| 1 | H |  |  |  |  |  |  |  |  |  |  |  | S |  |  |
| 2 | H |  | S |  |  |  |  |  |  |  |  |  | S | S |  |


| $\mathbf{3}$ | H |  |  |  |  |  |  |  |  |  |  |  | S |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathbf{4}$ |  | S | S |  |  |  |  |  |  |  |  |  | S | S | S |
| $\mathbf{5}$ | S |  |  | S |  |  |  |  |  |  |  |  | S |  |  |
| $\mathbf{6}$ | H | H | S |  |  |  |  |  |  |  |  |  | S |  |  |
| $\mathbf{7}$ |  |  |  |  |  |  |  |  |  |  |  |  | S |  |  |
| $\mathbf{8}$ |  | H |  |  |  |  |  |  |  |  |  |  |  |  | S |
| $\mathbf{9}$ |  |  | S |  |  |  |  |  |  |  |  |  |  |  |  |
| $\mathbf{1 0}$ |  | S |  | S |  |  |  |  |  |  |  |  | S |  |  |
| $\mathbf{1 1}$ | S |  |  |  |  |  |  |  |  |  |  |  | S | S | S |
| $\mathbf{1 2}$ | H |  | S |  |  |  |  |  |  |  |  |  | S | S |  |
| $\mathbf{1 3}$ | H |  |  |  |  |  |  |  |  |  |  |  | S | S |  |
| $\mathbf{1 4}$ | S |  |  | S |  |  |  |  |  |  |  |  |  |  |  |

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