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**INSTITUTE OF AERONAUTICAL ENGINEERING
(Autonomous)**

MODEL QUESTION PAPER

B.Tech III Semester End Examinations (Regular), November – 2017

Regulation: IARE-R16

**DISCRETE MATHEMATICAL STRUCTURES
(Common to CSE/IT)**

Time: 3 Hours

Max Marks: 70

Answer ONE Question from each Unit

All Questions Carry Equal Marks

All parts of the question must be answered in one place only

UNIT – I

1. (a) Explain about logical equivalence and tautological implications. Specify the laws of logic. [7M]
- (b) Determine a valid conclusion from the given premises: [7M]
 - i. $P \rightarrow (Q \rightarrow S), \sim R \vee P, Q \Leftrightarrow R \rightarrow S$
 - ii. $P \vee Q, Q \rightarrow R, P \rightarrow M \text{ and } \sim M \Leftrightarrow R \wedge (P \vee Q)$
2. (a) Explain about principle conjunctive normal form and principle disjunctive normal form with its procedural steps. Obtain the principal disjunctive normal form of $P \rightarrow ((P \rightarrow Q) \wedge \sim (\sim Q \vee \sim P))$. [7M]
- (b) Prove the following logical equivalences: [7M]
 - i. $[(p \leftrightarrow q) \wedge (q \leftrightarrow r) \wedge (r \leftrightarrow p)] \Leftrightarrow [(p \wedge q) \wedge (q \rightarrow r) \wedge (r \rightarrow p)]$
 - ii. $p \rightarrow (q \rightarrow r) \Leftrightarrow p \rightarrow (\sim q \wedge r) \Leftrightarrow (p \wedge q) \rightarrow r \Leftrightarrow (p \rightarrow r) \vee (q \rightarrow r)$.

UNIT – II

3. (a) Let R and S be relations from a set A to a set B and T be a relation from the set B to a set C. [7M]
Prove that if $R \subseteq S$ then $R \circ T \subseteq S \circ T$.
- (b) Consider sets $A = \{a, b, c\}$ and $B = \{1, 2, 3\}$, and relations from A to B are $R = \{(a, 1), (b, 1), (c, 2), (c, 3)\}$ and $S = \{(a, 1), (a, 2), (b, 1), (b, 2)\}$. Compute the following: [7M]
 - i. $R \cup S$
 - ii. $R \cap S$
 - iii. R^c
 - iv. S^c
4. (a) Let $X \rightarrow Y$ be a function and A and B be arbitrary non-empty subsets of X. Then: [7M]
 - i. If $A \subseteq B$, then $f(A) \subseteq f(B)$.
 - ii. $f(A \cup B) = f(A) \cup f(B)$.
 - iii. $f(A \cup B) = f(A) \cup f(B)$. and the equality holds if f is one-to-one.
- (b) Construct the hasse diagram for the divisibility relation on following sets. [7M]
 - i. $A = \{3, 6, 12, 36, 72\}$
 - ii. $A = \{1, 2, 3, 5, 6, 10, 15, 30\}$

UNIT – III

5. (a) Describe Binomial theorem. Find the coefficient of x^5y^7 in the expansion of $(x + 3y)^{12}$. [7M]
- (b) A chain letter is sent to 10 people in the first week of the year. The next week each person who received a letter sends letters to 10 new people and so on. How many people have received the letters at the end of the year? [7M]

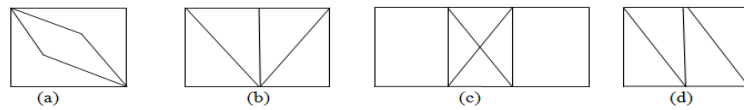
6. (a) Solve that $(Z, *)$ is an abelian group where Z is a set of integers and the binary operations $*$ is defined as $a * b = a + b - 3$. [7M]
 (b) Construct the co-efficient of $a^2b^3c^3d^5$ in the expansion of $(a + 2b - 3c + 2d + 5)^{16}$. [7M]

UNIT – IV

7. (a) Identify the generating function for the following sequence : [7M]
 i. $1^2, 2^2, 3^2, \dots$
 ii. $0^2, 1^2, 2^2, 3^2, \dots$
 iii. $1^3, 2^3, 3^3, \dots$
 (b) Solve the recurrence relation given below : [7M]
 i. $a_n + a_{n-1} + n^3, n \geq 1$ where $a_0 = 5$ by using substitution method.
 ii. $a_n + 4a_{n-1} + 4a_{n-2} = 8$ for $n \geq 2$, and $a_0 = 1, a_1 = 2$ by using non-homogeneous recurrence relation.
8. (a) Solve the recurrence relation $a_n - 6a_{n-1} + 12a_{n-2} - 8a_{n-3} = 0$ for $n \geq 3$ using generating functions. [7M]
 (b) Solve the co-efficient of x^{27} of the following functions: [7M]
 i. $(x^4 + x^5 + x^6 + \dots)^5$
 ii. $(x^4 + 2x^5 + 3x^6 + \dots)^5$

UNIT – V

9. (a) Describe Euler and Hamilton graphs. Which of the following graphs are Euler graphs and Hamilton graphs? [7M]



- (b) Construct the spanning tree by using (i) Breadth First Search (ii) Depth First Search of graph G shown in Figure 1. [7M]

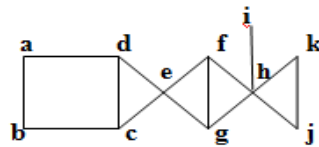


Figure 1

10. (a) Find the union, intersection and the ring sum of the graphs G1 and G2 given below: [7M]



- (b) Eight cities A, B, C, D, E, F, G, H are required to be connected by a new railway network. The possible tracks and the cost of involved to lay them (in crores of Rupees) are summarized in the below given table: [7M]

| Track Between | Cost | Track Between | Cost |
|---------------|------|---------------|------|
| A and B | 155 | D and F | 100 |
| A and D | 145 | E and F | 150 |
| A and G | 120 | F and G | 140 |
| B and C | 145 | F and H | 150 |
| C and D | 150 | G and H | 160 |
| C and E | 95 | | |

Determine a Railway network of minimal cost that connects all these cities.



INSTITUTE OF AERONAUTICAL ENGINEERING (Autonomous)

COURSE OBJECTIVES:

The course should enable the students to:

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|---|---|
| 1 | Describe the logical and mathematical foundations and study the predicate logic. |
| 2 | Be familiar with the basic terminology of functions, relations, and sets and demonstrate knowledge of their associated operations. |
| 3 | Be familiar with the practical applications the use of basic counting principles of permutations, combinations, inclusion/exclusion principle and the pigeonhole methodology. |
| 4 | Master to solve advanced mathematical problems on recurrence relations. |
| 5 | Recognize the patterns that arise in graph problems and use this knowledge for constructing the trees and spanning trees. |

COURSE LEARNING OUTCOMES:

Students, who complete the course, will have demonstrated the ability to do the following:

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| CAHS013.01 | Understand logical connectives and compound prepositions for building compound statements. |
| CAHS013.02 | Learn the formal symbols and use the preposition logic and predicate logic to solve problems on logical equivalences and implications. |
| CAHS013.03 | Memorize different scientific notations to simplify the logical statements. |
| CAHS013.04 | Prepare valid arguments from the given propositional statements by using rules of inference. |
| CAHS013.05 | Identify ordered pairs to form a binary relation from the given sets. |
| CAHS013.06 | Construct directed graph and a matrix representation using a binary relation on finite order pairs. |
| CAHS013.07 | Identify the properties of relations to check for equivalence relation and partial order relation and compute relations using operations on relations. |
| CAHS013.08 | Construct a hasse diagram to recognize the relevant partial ordered sets from the given binary relation. |
| CAHS013.09 | Describe the types of functions (one to one, on-to, bijective, Identity and constant function). |
| CAHS013.10 | Implement the concept of the inverse and recursive functions to get an optimized solution for an appropriate problem. |
| CAHS013.11 | Use the concept of lattices (Greatest Lower Bound (GLB) and Least Upper Bound (LUB) to represent a defined finite set in multi-dimension applications. |
| CAHS013.12 | Explain about the properties and types of lattices (bounded and distributive lattice). |
| CAHS013.13 | Construct different algebraic structures by using concepts of groups, sub groups, monoids and rings. |
| CAHS013.14 | .Understand binomial and multinomial theorems to compute the coefficients for the given expansions. |
| CAHS013.15 | Understand the concept of homomorphism and isomorphism of semi-groups. |
| CAHS013.16 | Analyze the given sets by using inclusion and exclusion principle. |
| CAHS013.17 | Identify the different counting techniques (permutations) related to mathematics and computer science. |

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| CAHS013.18 | Solve discrete probability and set problems by using permutations and combinatorics. |
| CAHS013.19 | Identify the series of expansion to represent the sequence by using generating functions |
| CAIT001.20 | Identify the general solution for first-order and second-order linear homogeneous recurrence relations. |
| CAHS013.21 | Identify the roots of second and higher order linear non-homogeneous recurrence relations. |
| CAHS013.22 | Understand the use of graphs and trees as representation tools in a variety of context. |
| CAHS013.23 | Identify Euler's and Hamilton rule for a simple connected graph in NP-complete problems. |
| CAHS013.24 | Construct a spanning tree by using search techniques (Depth First Search and Breadth First Search). |
| CAHS013.25 | Construct a minimal spanning tree by using Kruskal's and Prim's algorithm in order to obtain a solution for a real time problem. |
| CAHS013.26 | Possess the knowledge and skills for employability and to succeed in national and international level competitive exams. |

Mapping of Semester End Examinations to Course Learning Outcomes:

| SEE Question No | | Course Learning Outcomes | Blooms Taxonomy Level |
|-----------------|---|--|-----------------------|
| 1 | a | CAHS013.03 Memorize different scientific notations to simplify the logical statements. | Remember |
| | b | CAHS013.04 Prepare valid arguments from the given propositional statements by using rules of inference. | Remember |
| 2 | a | CAHS013.01 Understand logical connectives and compound prepositions for building compound statements. | Understand |
| | b | CAHS013.02 Use the formal symbols to represent the preposition logic and predicate logic to solve problems on logical equivalences and implications. | Remember |
| 3 | a | CAHS013.05 Identify ordered pairs to form a binary relation from the given sets. | Understand |
| | b | CAHS013.07 Identify the properties of relations to check for equivalence relation and partial order relation and compute relations using operations on relations. | Understand |
| 4 | a | CAHS013.09 Describe the types of functions (one to one, on-to, bijective, Identity and constant function). | Remember |
| | b | CAHS013.08 Construct a Hasse diagram to recognize the relevant partial ordered sets from the given binary relation. | Understand |
| 5 | a | CAHS013.14 Understand binomial and multinomial theorems to compute the coefficients for the given expansions. | Understand |
| | b | CAHS013.17 Identify the different counting techniques (permutations) related to mathematics and computer science. | Understand |
| 6 | a | CAHS013.13 Construct different algebraic structures by using concepts of groups, sub groups, monoids and rings. Remember. | Remember |
| | b | CAHS013.14 Understand binomial and multinomial theorems to compute the coefficients for the given expansions. Understand | Understand |
| 7 | a | CAHS013.19 Identify the series of expansion to represent the sequence by using generating functions | Understand |
| | b | CAHS013.21 Identify the roots of second and higher order linear non-homogeneous recurrence relations. | Understand |

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|----|---|------------|---|------------|
| 8 | a | CAHS013.19 | Identify the series of expansion to represent the sequence by using generating functions | Understand |
| | b | CAHS013.14 | Understand binomial and multinomial theorems to compute the coefficients for the given expansions. | Understand |
| 9 | a | CAHS013.23 | Identify Euler's and Hamilton rule for a simple connected graph in NP-complete problems. | Understand |
| | b | CAHS013.24 | Construct a spanning tree by using search techniques (Depth First Search and Breadth First Search). | Remember |
| 10 | a | CAHS013.22 | Understand the use of graphs and trees as representation tools in a variety of context. | Understand |
| | b | CAHS013.25 | Construct a minimal spanning tree by using Kruskal's and Prim's algorithm in order to obtain a solution for a real time problem.. | Remember |

Signature of Course Coordinator

HOD, CSE