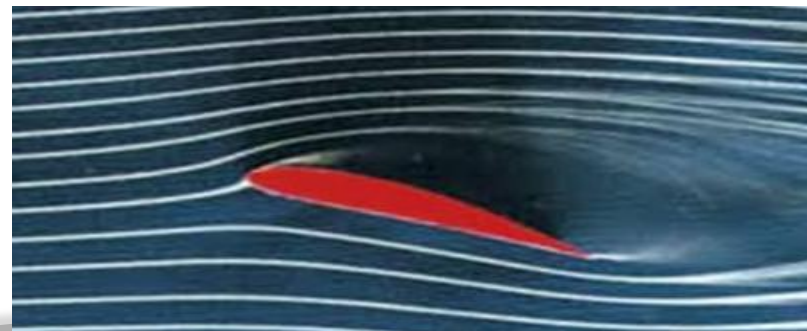
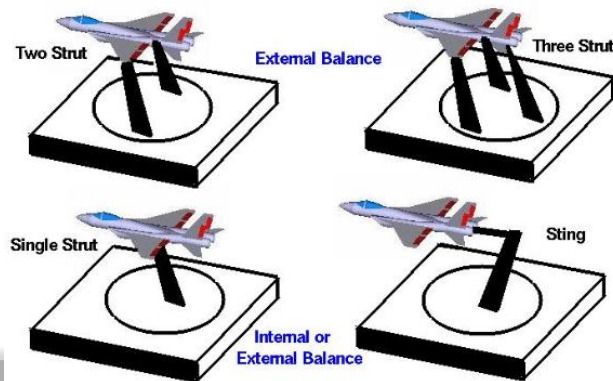
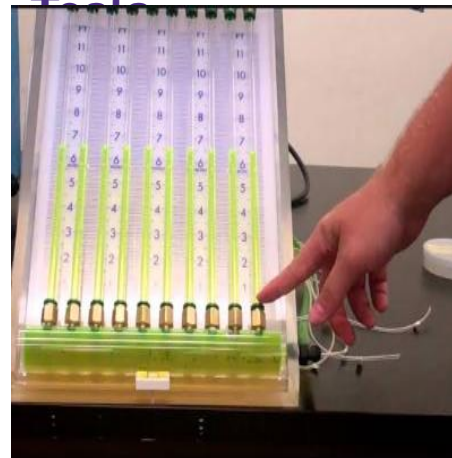
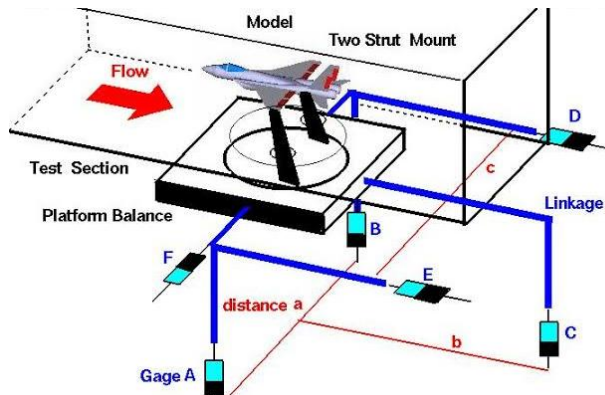


- ❖ Forms of Aerodynamic Experiments
- ❖ Observations
- ❖ Measurement Objectives
- ❖ History:
 - Wright Brother's Wind Tunnel
- ❖ Model Testing
- ❖ Wind Tunnel Principles
- ❖ Scaling Laws
- ❖ Scale Parameters
- ❖ Geometric Similarity
- ❖ Kinematic Similarity
- ❖ Dynamic Similarity
- ❖ Wind Tunnels:
 - ❖ Low Speed Tunnel
 - ❖ High Speed Tunnels
 - ❖ Transonic
 - ❖ Supersonic
 - ❖ Hypersonic Tunnels
 - ❖ Shock Tubes
- ❖ Special Tunnels:
 - Low Turbulence Tunnels
 - High Reynolds Number Tunnels
 - Environmental Tunnels
 - Automobile Tunnels
- ❖ Distinctive Features
- ❖ Application

Forms of Aerodynamic Experiments

- ❖ Six component force tests
- ❖ Pressure tests
- ❖ Internal balance tests
- ❖ Flow Visualization Tests



Observations

Aerodynamic behaviour of Various Geometry

Pressure Behaviour

Control Behaviour

Flow Visualisation Behaviour

Measurement Objectives

- Various Types Wind Tunnel
- Various Testing Methods
- Model mounting Methods
- Testing Tools and Application

Wright Brother's Wind Tunnel

The Wrights large wind tunnel

After building and testing a small wind tunnel, the Wright brothers completed a larger, more sophisticated one in October 1901. They used it extensively to carry out aerodynamic research that proved essential in designing their 1903 airplane.

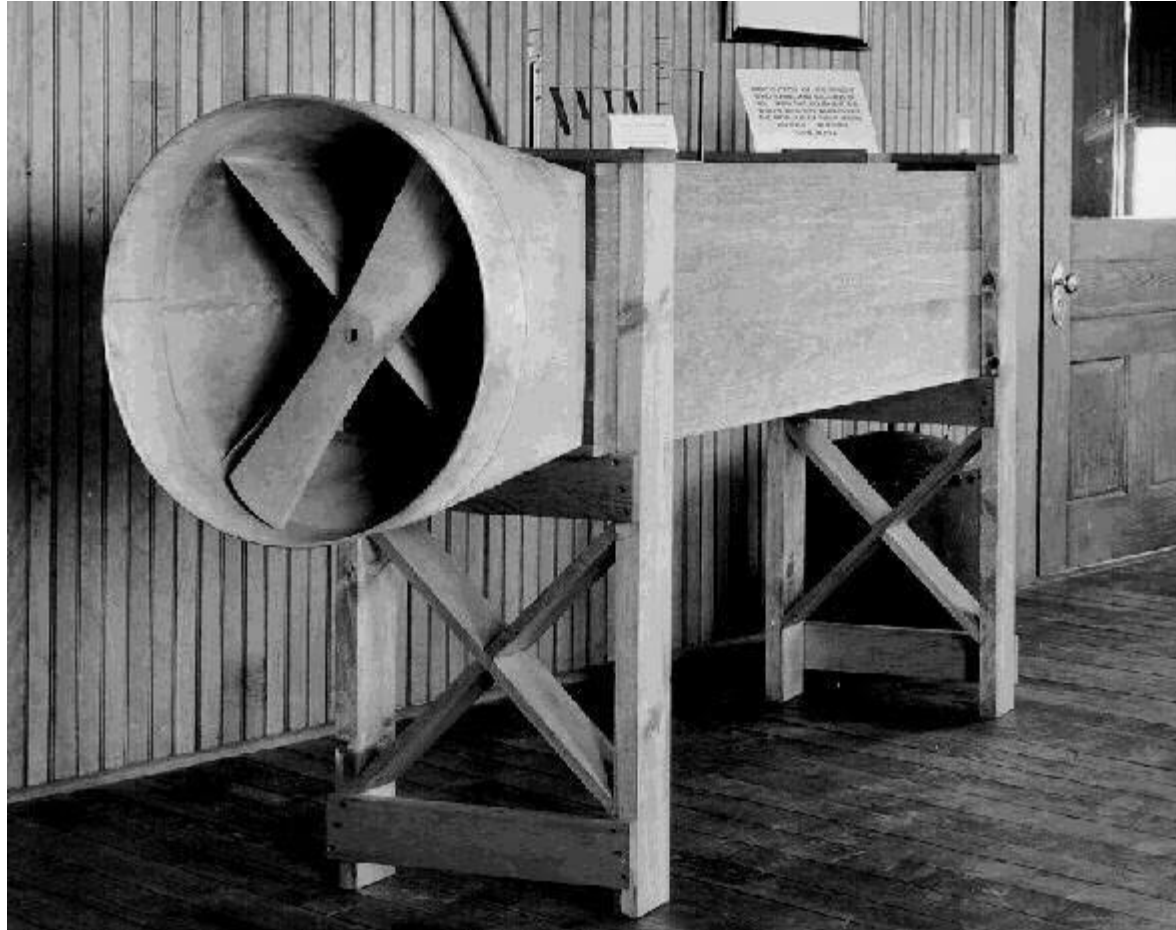
The wind tunnel consisted of a simple wooden box with a square glass window on top for viewing the interior during testing. A fan belted to a one-horsepower engine, which ran the machinery in their bicycle shop, provided an airflow of about 30 miles per hour.

Wright wind tunnel balances

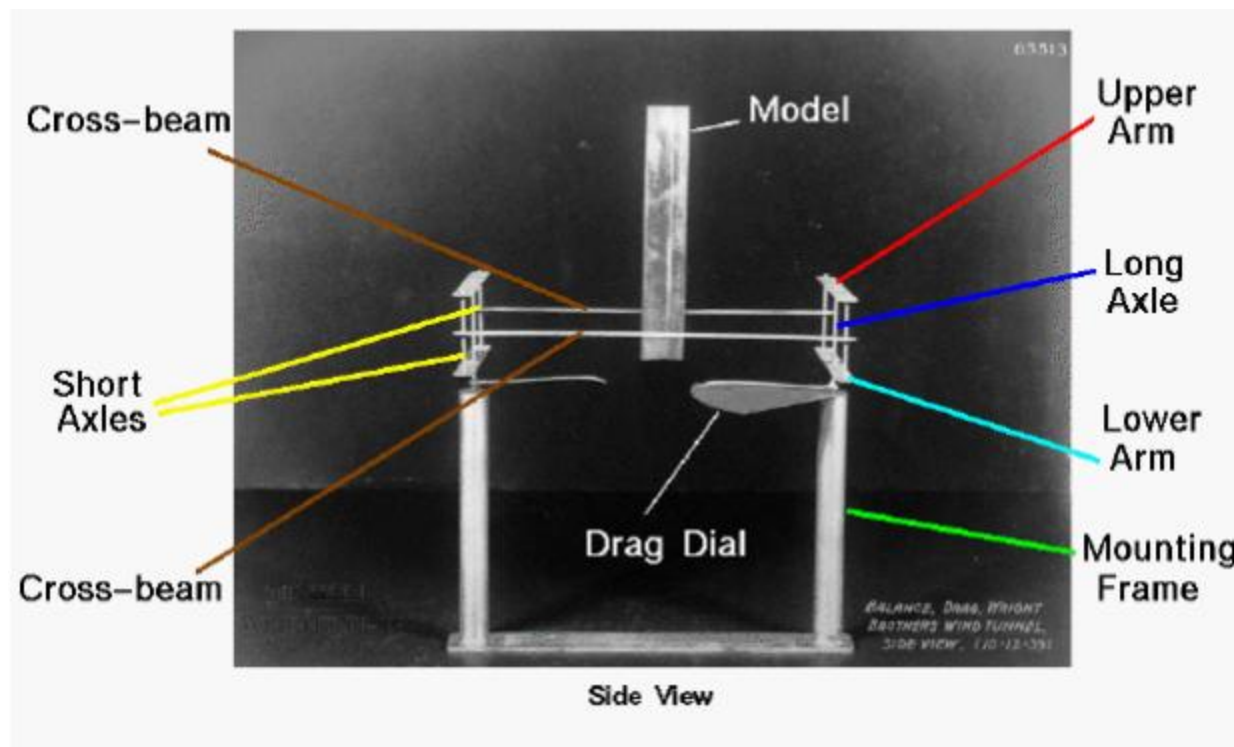
What made the Wrights' wind tunnel unique were the instruments they designed and built to measure lift and drag. Called balances, after the force-balancing concept, these instruments measured the forces of lift and drag acting on a wing in terms that could be used in the equations.

The balances are made from old hacksaw blades and bicycle spokes. Their crude appearance belies their sophisticated design. Largely the work of Orville, they represent a solid understanding of geometry, mathematics, and aerodynamic forces, and illustrate the Wrights' engineering talents at their finest.

Unit-I FUNDAMENTALS OF EXPERIMENTS IN AERODYNAMICS



At the end of the summer of 1901, the Wright brothers were frustrated by the flight tests of their 1901 glider. The aircraft was flown frequently up to 300 feet in a single glide. But the aircraft did not perform as well as the brothers had expected. The aircraft only developed $\frac{1}{3}$ of the lift which was predicted by the lift equation using Lilienthal's data. During the fall of 1901, the brothers began to question the aerodynamic data on which they were basing their designs. So, they decided to conduct a series of wind tunnel tests to verify the results they were experiencing in flight. They would measure the aerodynamic lift and drag on small models of their wing designs using a wind tunnel in their bicycle shop at Dayton, Ohio. They built two separate **balances** to perform these measurements, one for lift and the other for drag.



Model Testing

- ❖ **Aero Dynamic Force And Moments**
- ❖ **Model Size**
- ❖ **Model Geometry**

Wind Tunnel Principles

Energy per unit volume before = Energy per unit volume after

$$P_1 + \frac{1}{2} \rho v_1^2 + \rho g h_1 = P_2 + \frac{1}{2} \rho v_2^2 + \rho g h_2$$

Pressure Energy

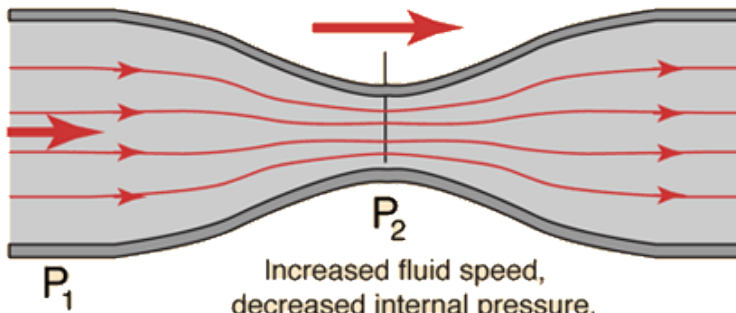
Kinetic Energy per unit volume

Potential Energy per unit volume

The often cited example of the Bernoulli Equation or "Bernoulli Effect" is the reduction in pressure which occurs when the fluid speed increases.

Flow velocity v_1

Flow velocity v_2

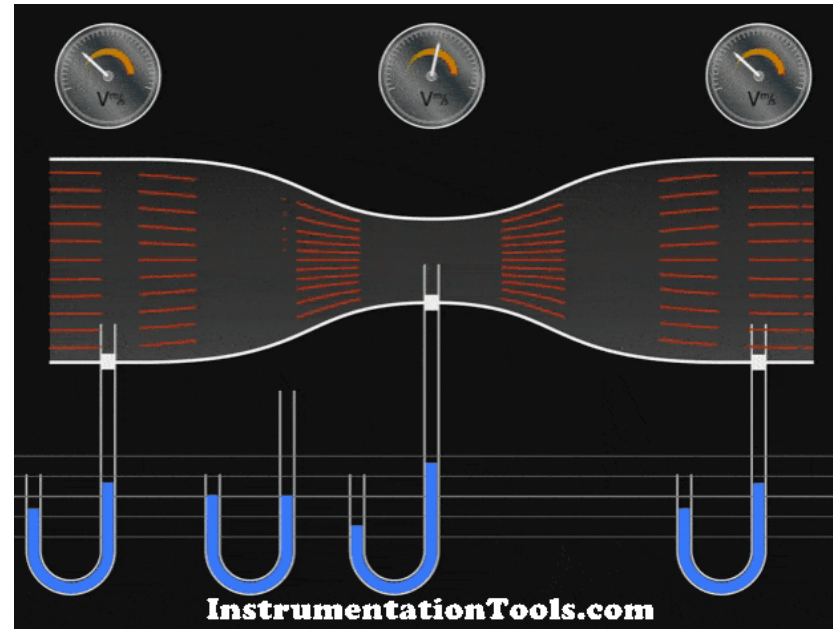


$$A_2 < A_1$$

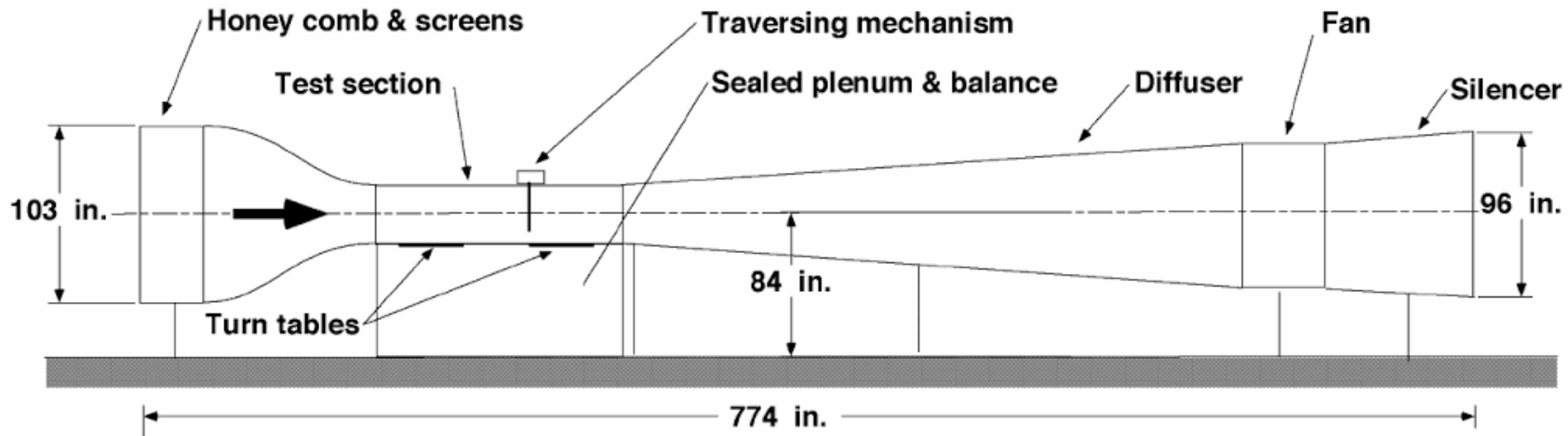
$$v_2 > v_1$$

$$P_2 < P_1!$$

Increased fluid speed, decreased internal pressure.



Low Speed Wind Tunnel and Major Parts



- ❖ Honey comb & Screen
- ❖ Contraction
- ❖ Test Section
- ❖ Diffuser
- ❖ Fan or Driving Unit
- ❖ Silencer

Scaling Laws

- Astronomical Scaling ->
Gravitational forces dominate on an astronomical scale (e.g., the earth 1 moves around the sun), but not on smaller scales
- Macro and Micro Scaling
- Geometry Scaling

Summary

Two types of scaling laws:

1. **The first type:** Depends on the size of physical objects.
2. **The second type:** Involves both the size and material properties of the system.

Scaling Laws

Scaling in Geometry

Surface and volume are two physical quantities that are frequently involved in micro-device design.

- **Volume:** related to the mass and weight of a device, which are related to both mechanical and thermal inertial. (thermal inertial: related to the heat capacity of a solid, which is a measure of how fast we can heat or cool a solid. → important in designing a thermal actuator)
- **Surface:** related to pressure and the buoyant forces in fluid mechanics, as well as heat absorption or dissipation by a solid in convective heat transfer.

Scaling Laws

Surface to volume ration (S/V ratio)

❖ $S \propto l^2$; $S \propto l^3$

❖ $S/V \propto l^{-1}$

❖ - As the size l decreases, its S/V ratio increases

6.7 Scaling in Fluid Mechanics

- In Fig. 6.7, moving the top plate to the right induces the motion of the fluid.

- Newtonian flow: $\tau \propto \frac{d\theta}{dt}$, or $\tau = \mu \frac{d\theta}{dt} = \mu \frac{dV}{dy}$

where τ : shear stress; μ : coefficient of viscosity (黏滯性); $d\theta/dt$: strain rate; V : fluid velocity.

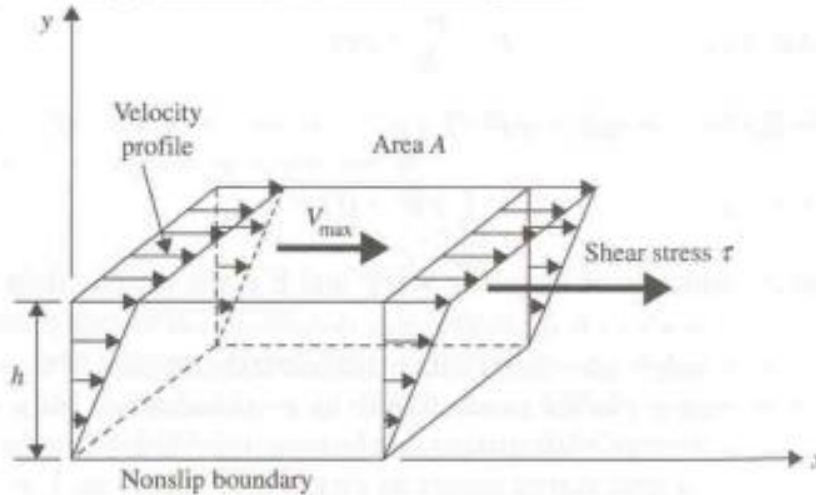
- Thus, $\mu = \frac{\tau}{R_s}$ (6.22)

where $R_s = V_{max}/h$

- Rate of volumetric fluid flow: $Q = A_s V_{ave}$ (6.23)

where A_s : cross-sectional area for the flow; V_{ave} : average velocity of the fluid.

Figure 6.7 | Velocity profile of a volume of moving fluid.



- Reynolds number: $Re = \frac{\rho VL}{\mu}$

where ρ : fluid density; V & L : characteristic velocity and length scales of the flow.

- $Re \propto (\text{inertial forces})/(\text{viscous force})$
- Macro flows: high inertial forces \rightarrow high $Re \rightarrow$ turbulence flow
- Micro flows: high viscosity \rightarrow low $Re \rightarrow$ laminar flow

p.s.: (1) turbulence flow: fluctuating and agitated;

(2) laminar flow: smooth and steady;

(3) transition from laminar to turbulent: $10^3 \sim 10^5$

Scale Parameters

Wind Tunnel Design

Increase in Area :

For subsonic flow ($M < 1$)

velocity decreases & pressure increases

For supersonic flow ($M > 1$)

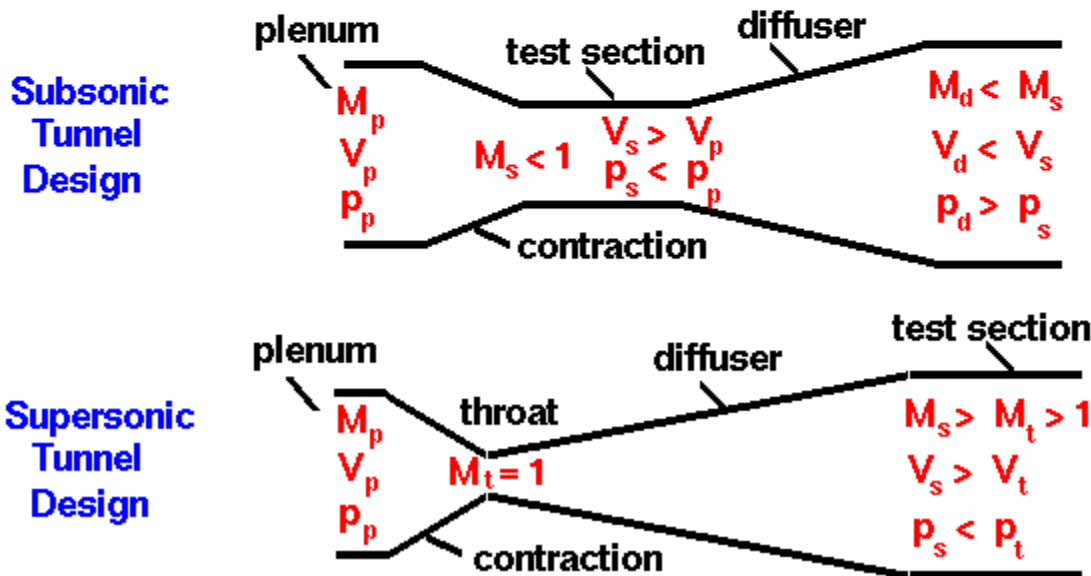
velocity increases & pressure decreases

M = Mach

V = velocity

p = pressure

A = area



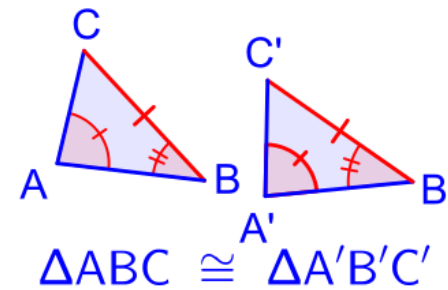
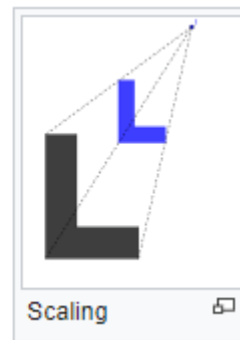
- ⊙ **Let $f(x)$ be any pdf. The family of pdfs $f(x-\mu)$ indexed by parameter μ is called the location family with standard pdf $f(x)$ and μ is the location parameter for the family.**
- ⊙ **Equivalently, μ is a location parameter for $f(x)$ iff the distribution of $X-\mu$ does not depend on μ .**

Example

- ⊙ If $X \sim N(\theta, 1)$, then $X - \theta \sim N(0, 1) \rightarrow$ distribution is independent of θ . $\rightarrow \theta$ is a location parameter.
- ⊙ If $X \sim N(0, \theta)$, then $X - \theta \sim N(-\theta, \theta) \rightarrow$ distribution is NOT independent of θ . $\rightarrow \theta$ is NOT a location parameter.

Geometric Similarity

Two objects are **similar** if they both have the same shape, or one has the same shape as the mirror image of the other. More precisely, one can be obtained from the other by uniformly scaling (enlarging or reducing), possibly with additional translation, rotation and reflection. This means that either object can be rescaled, repositioned, and reflected, so as to coincide precisely with the other object. If two objects are similar, each is congruent to the result of a particular uniform scaling of the other.



Geometric Similarity

Geometric similarity: *Model scale* $S = L_{WT}/L_{FL}$

Compressibility: *Mach number* $M_{WT} = M_{FL}; \left(\frac{V}{a}\right)_{WT} = \left(\frac{V}{a}\right)_{FL}$

Viscous effects: *Reynolds number* $Re_{WT} = Re_{FL}; \left(\frac{\rho VL}{\mu}\right)_{WT} = \left(\frac{\rho VL}{\mu}\right)_{FL}$

Wall stagnation temperature ratio: $\left(\frac{T_w}{T_0}\right)_{WT} = \left(\frac{T_w}{T_0}\right)_{FL}$

Kinematic Similarity & Dynamic Similarity

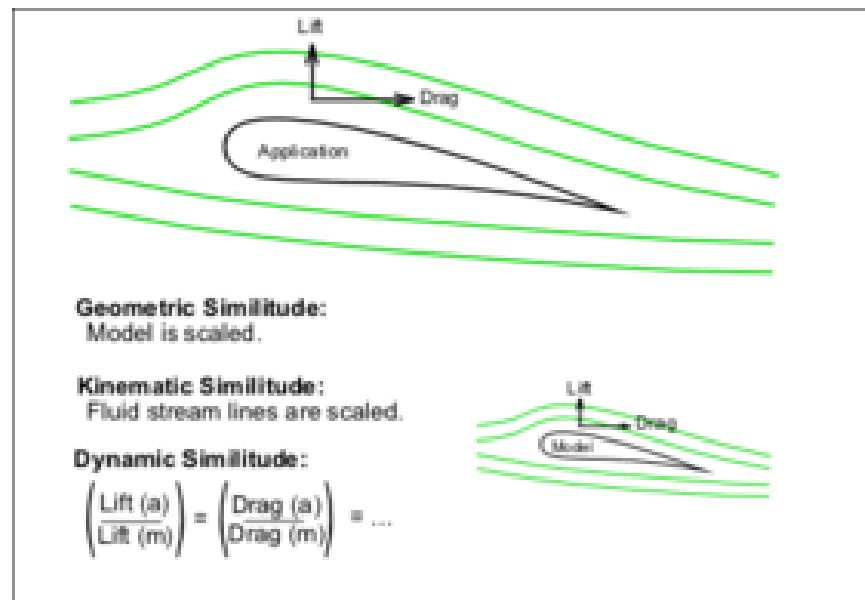
Kinematic similarity – fluid flow of both the model and real application must undergo similar time rates of change motions. (fluid streamlines are similar)

Dynamic similarity – ratios of all forces acting on corresponding fluid particles and boundary surfaces **in the** two systems are constant.

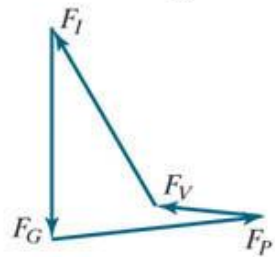
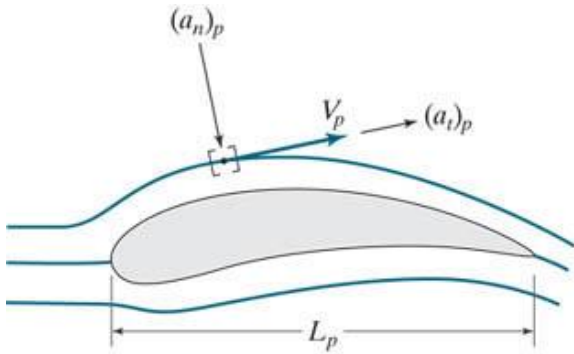
2. Kinematics similarity

- The kinematic similarity exist between model and prototype, if both of them have identical motions.
- The ratio of the corresponding velocity at corresponding points are equal.

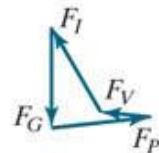
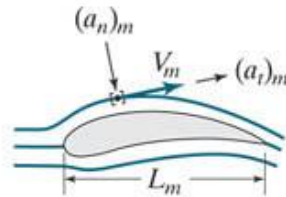
$$V_r = \frac{(V_1)_m}{(V_1)_p} = \frac{(V_2)_m}{(V_2)_p} = \frac{(V_3)_m}{(V_3)_p}$$



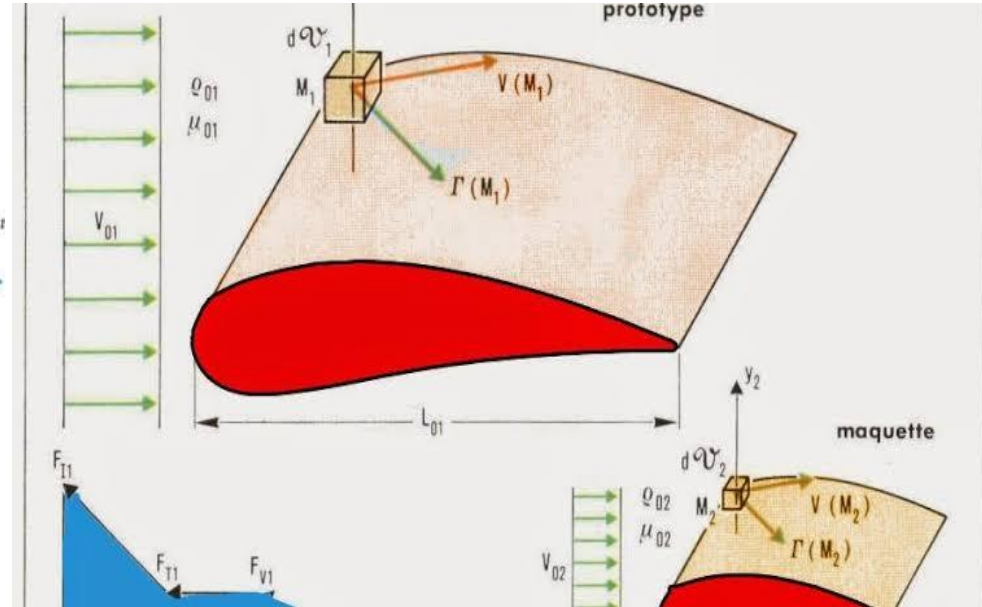
Unit-I FUNDAMENTALS OF EXPERIMENTS IN AERODYNAMICS



(a) Prototype



(b) Model



Dynamic Similarity

The dynamic similarity is said exist between model and prototype if the ratios of corresponding **forces** acting at the corresponding points are equal

$$\frac{F_p}{F_m} = F_r$$

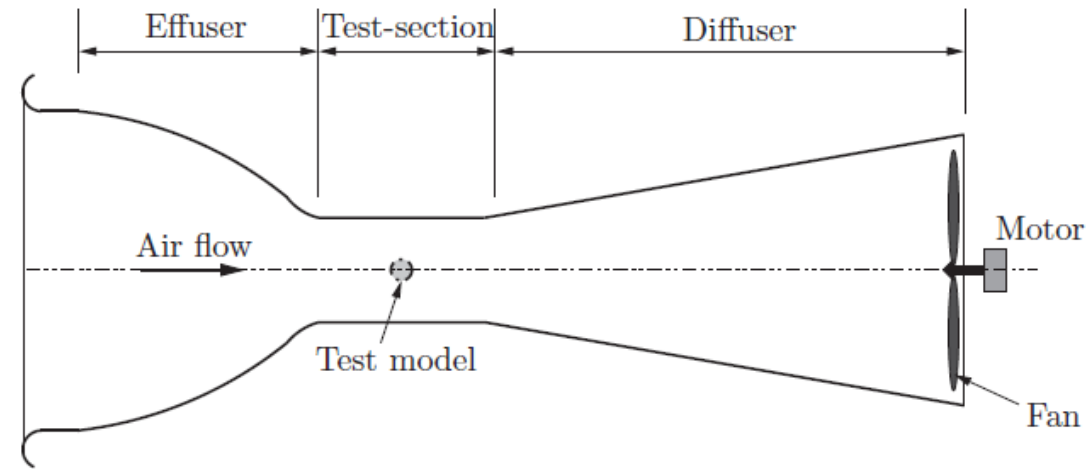
where F_r is Force Ratio

It means for dynamic similarity between the model and prototype, the dimensionless numbers should be same for model and prototype.

Wind Tunnels:

- ❖ Low Speed Tunnel
- ❖ High Speed Tunnels
- ❖ Transonic
- ❖ Supersonic
- ❖ Hypersonic Tunnels
- ❖ Shock Tubes

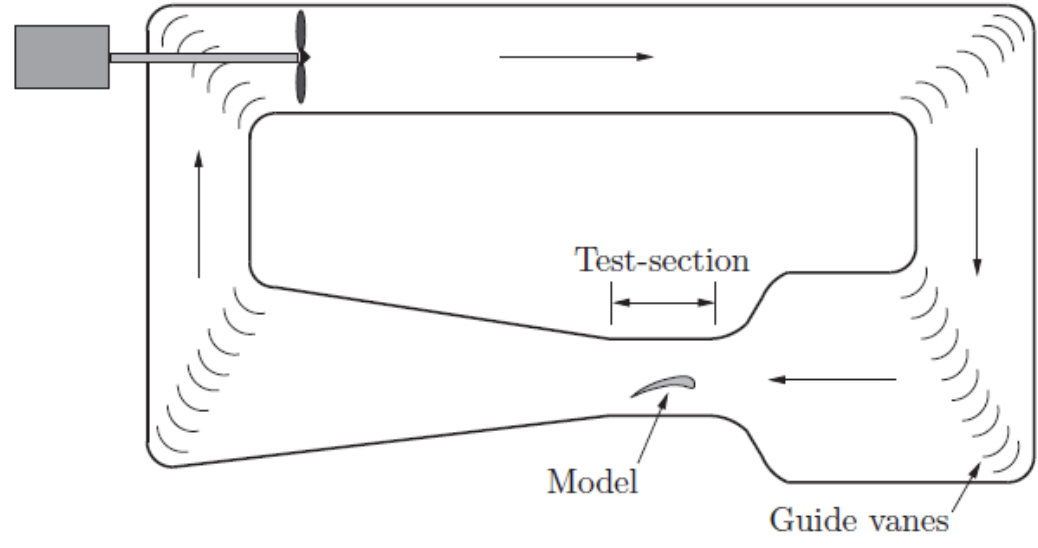
Low Speed Tunnel



Open-circuit
Tunnels

Closed-circuit Wind
Tunnel

Fan and motor



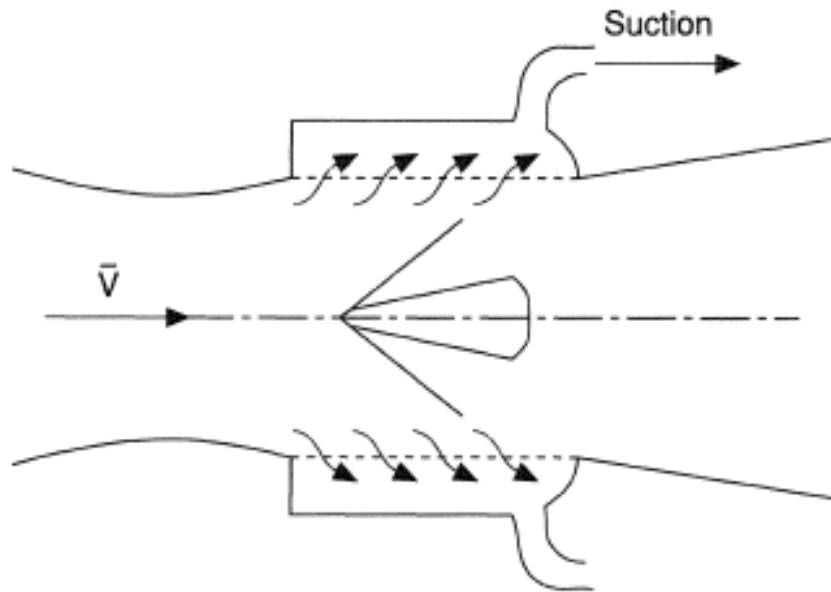
High Speed Tunnels

1. $0.8 < M < 1.2$ Transonic tunnel
2. $1.2 < M < 5$ Supersonic tunnel
3. $M > 5$ Hypersonic tunnel

$$M = \frac{\text{Pressure Force}}{\text{Inertia Force}} = \frac{\text{Speed of Object}}{\text{Speed of Sound}} = \frac{V}{a}$$

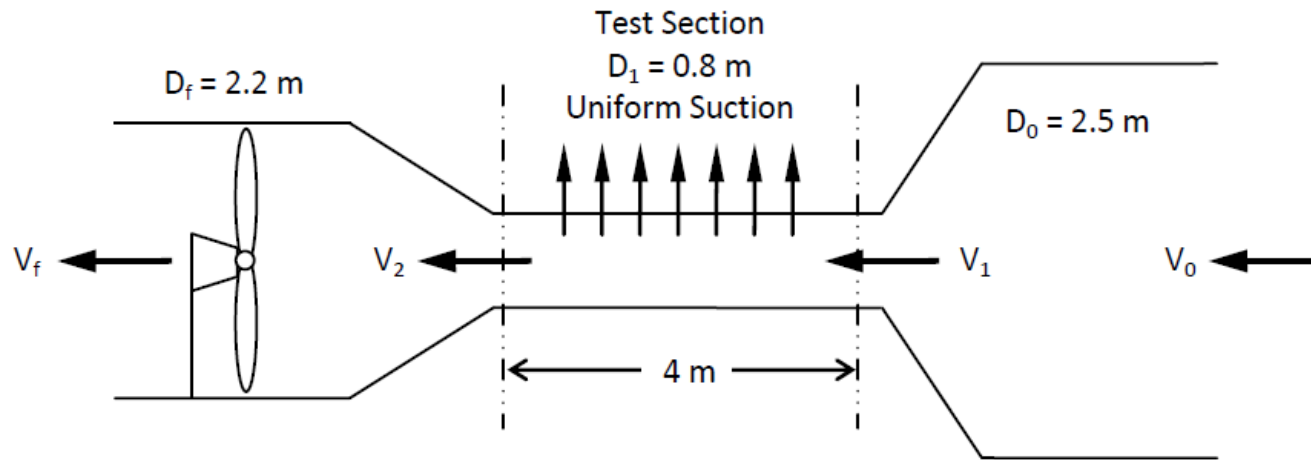
Where $a = \sqrt{\gamma RT}$

Transonic Windtunnel



Transonic Windtunnel

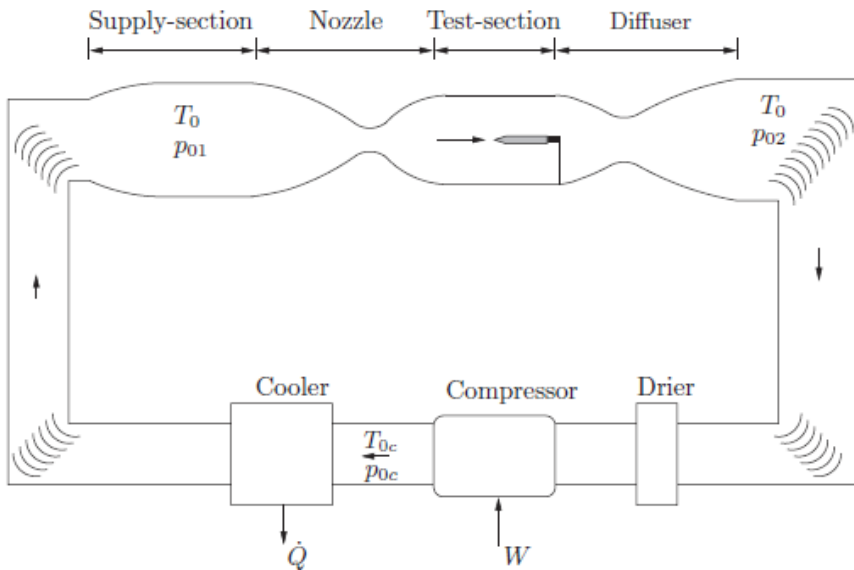
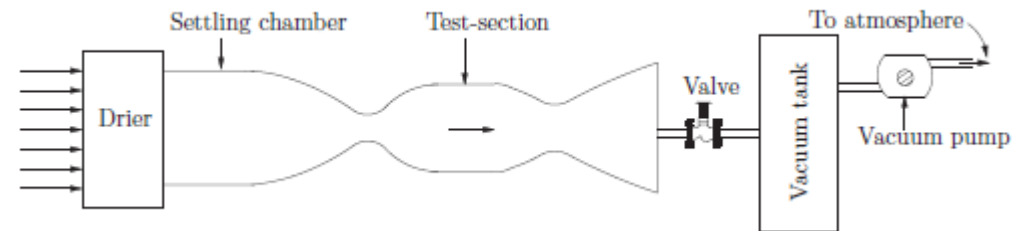
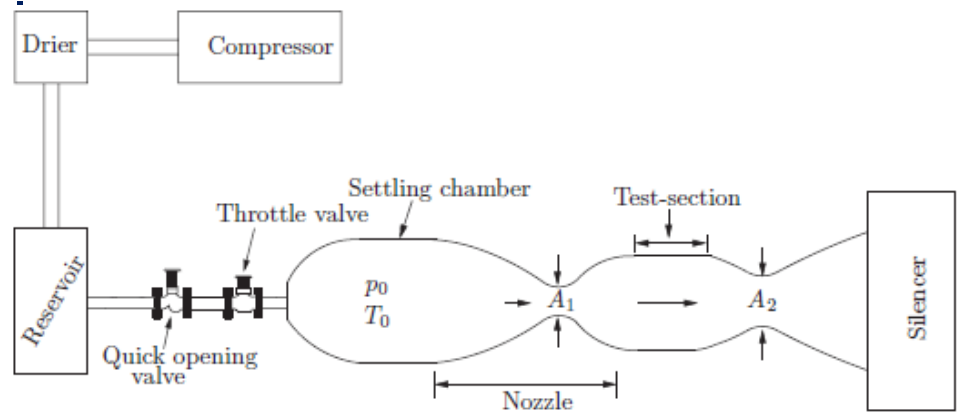
Problem 2. In some wind tunnels, the test section wall is porous or perforated; fluid is sucked out to provide a thin, viscous boundary layer. The wall is 4 m long and contains 800 holes of 6 mm diameter per square meter of area. The suction velocity out of each hold is $V_s = 10$ m/s, and the test section entrance velocity is $V_1 = 45$ m/s. Assuming incompressible flow of air at 20°C and 1 atm, compute (a) V_0 , (b) the total wall suction volume flow, (c) V_2 , and (d) V_f .



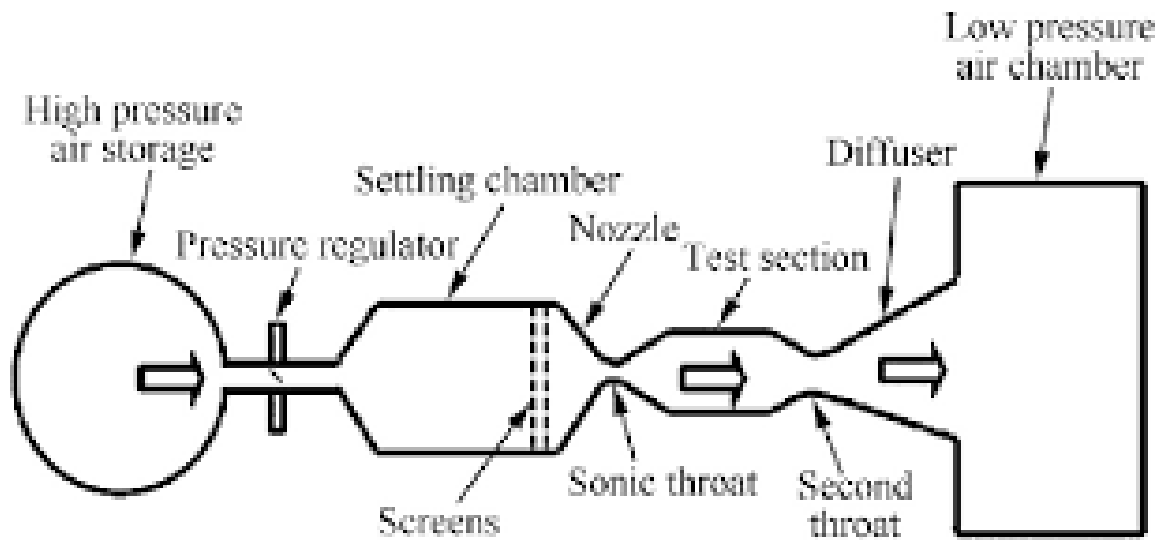
Unit-I FUNDAMENTALS OF EXPERIMENTS IN AERODYNAMICS

Supersonic

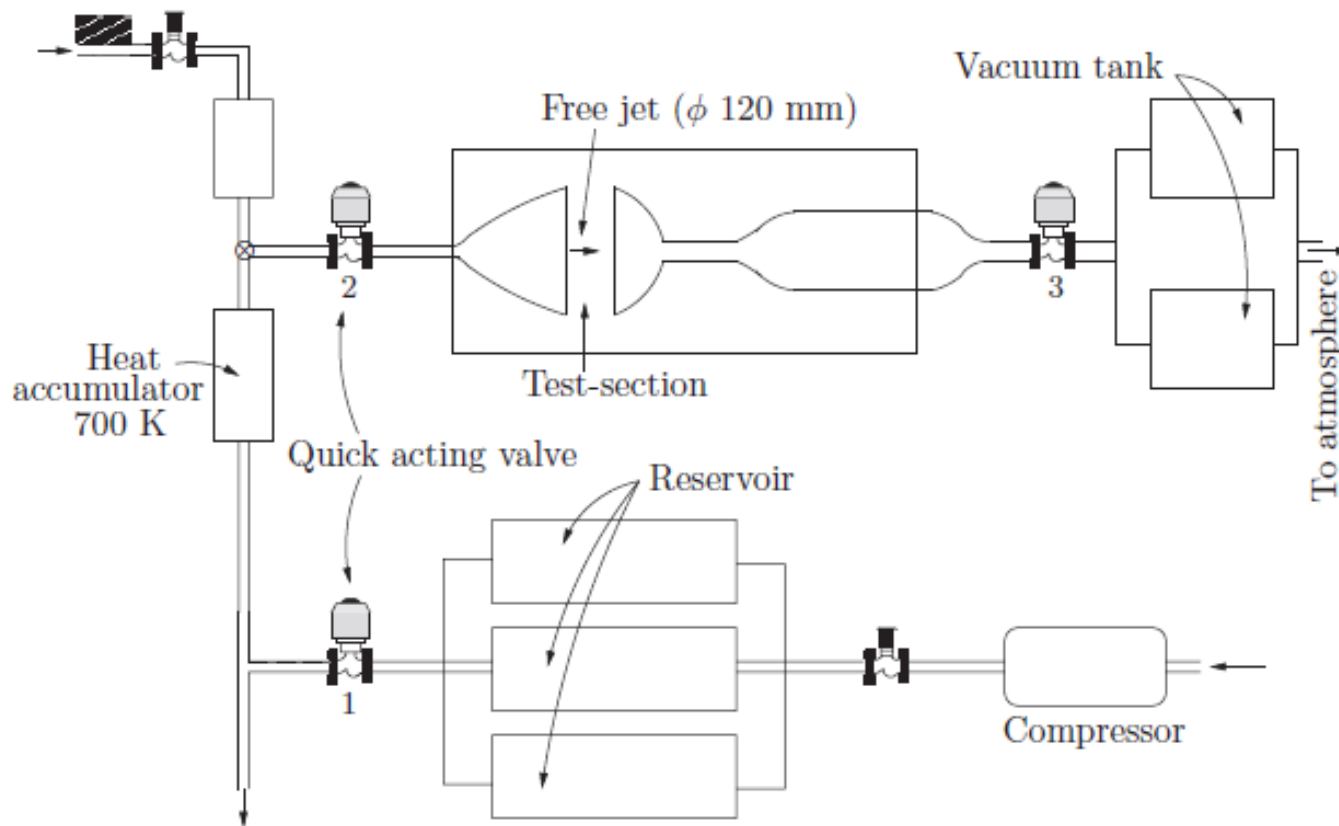
- ❖ Blowdown-Type Wind Tunnel
- ❖ Induction-Type Tunnels
- ❖ Closed-circuit Wind Tunnels



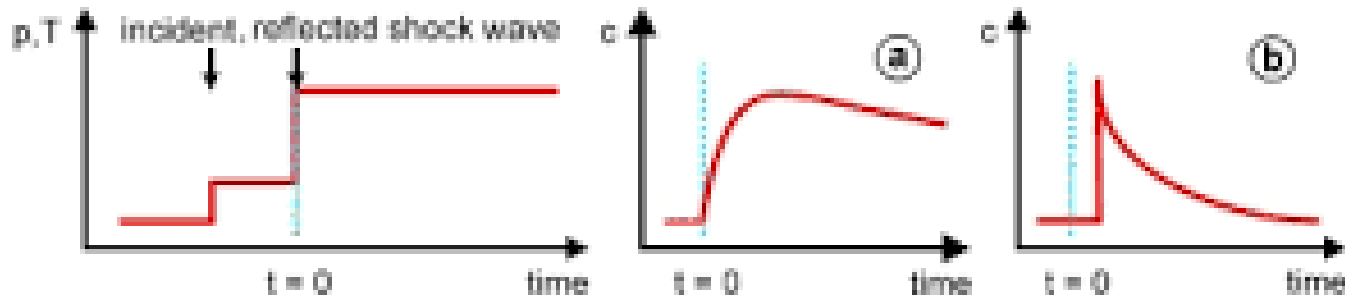
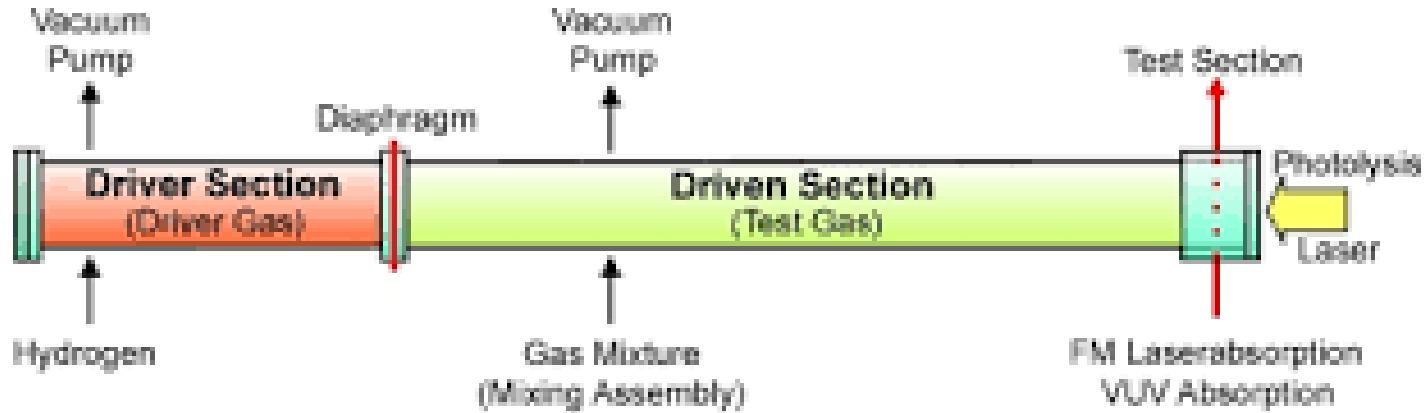
Blowdown-Type Wind Tunnels



Hypersonic Tunnels



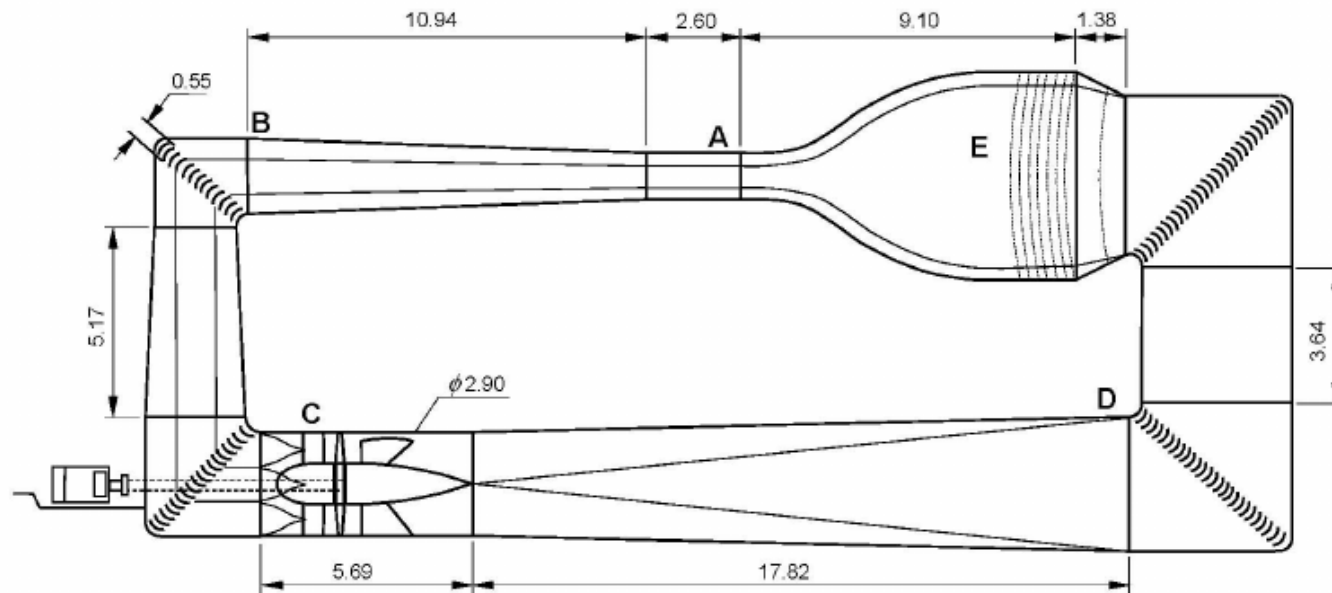
Shock Tubes



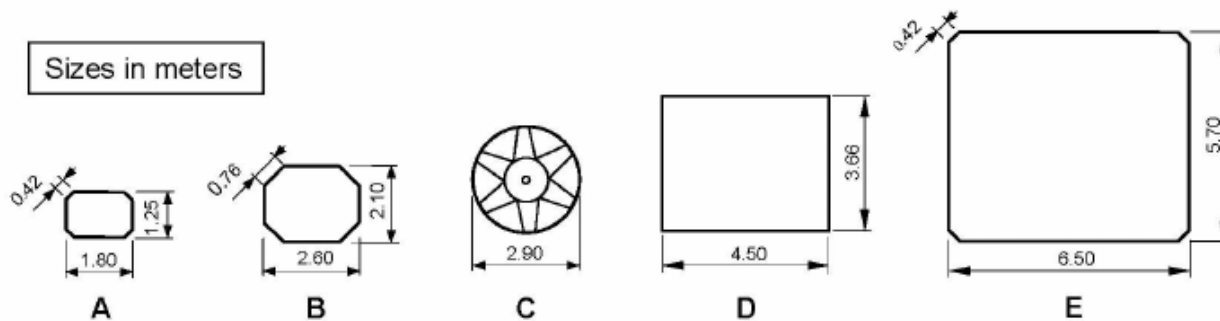
Special Tunnels:

- **Special Tunnels:**
 - **Low Turbulence Tunnels**
 - **High Reynolds Number Tunnels**
 - **Environmental Tunnels**
 - **Automobile Tunnels**

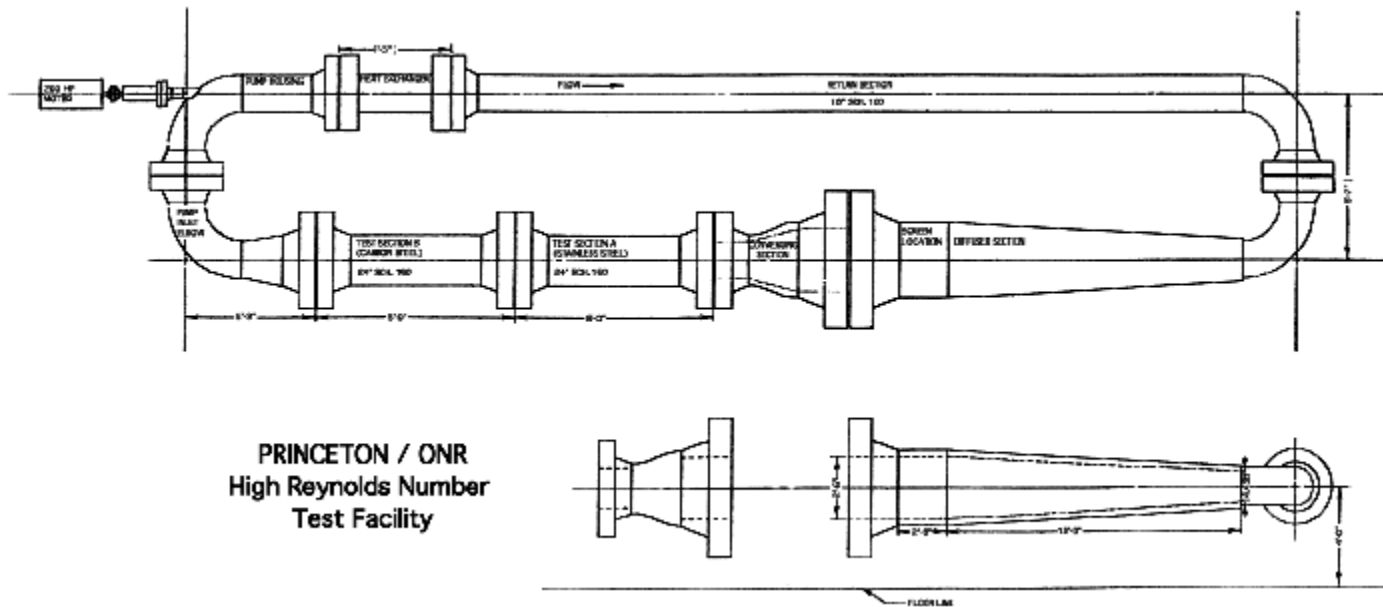
Low Turbulence Tunnels



Sizes in meters



High Reynolds Number Tunnels



Environmental Tunnels

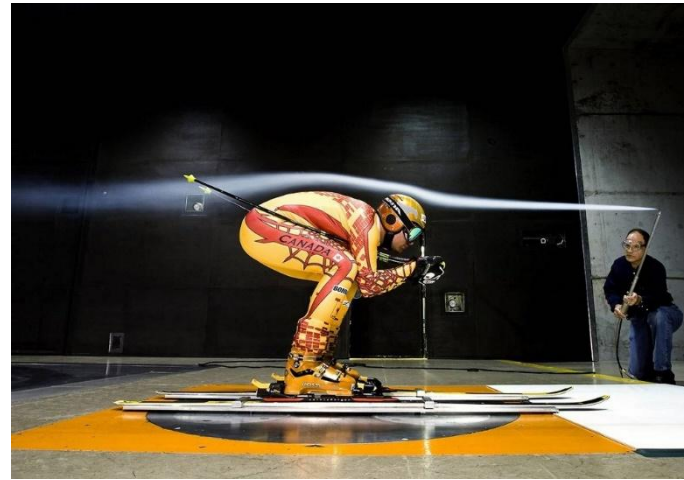


Automobile Tunnels



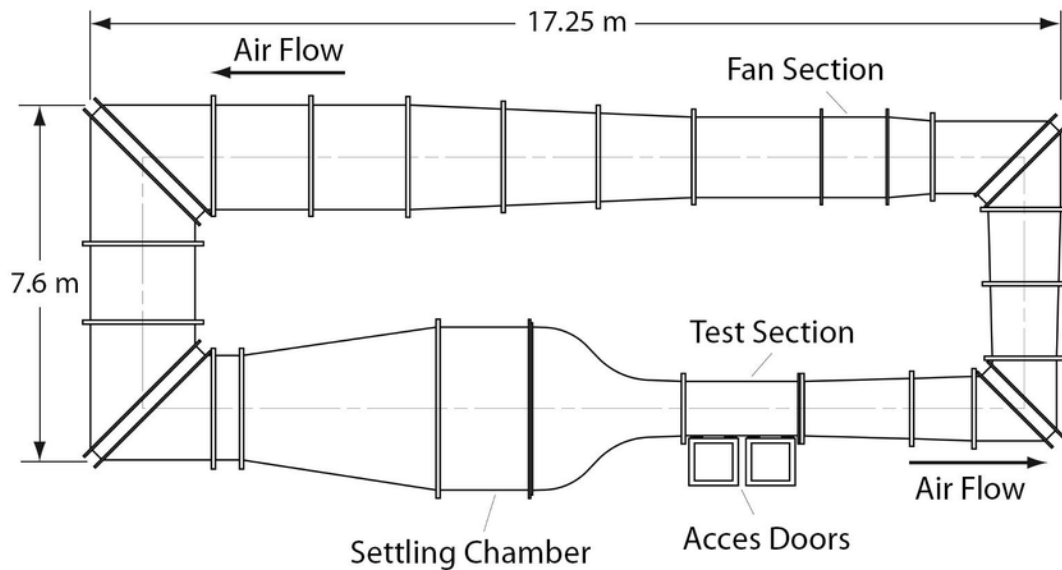
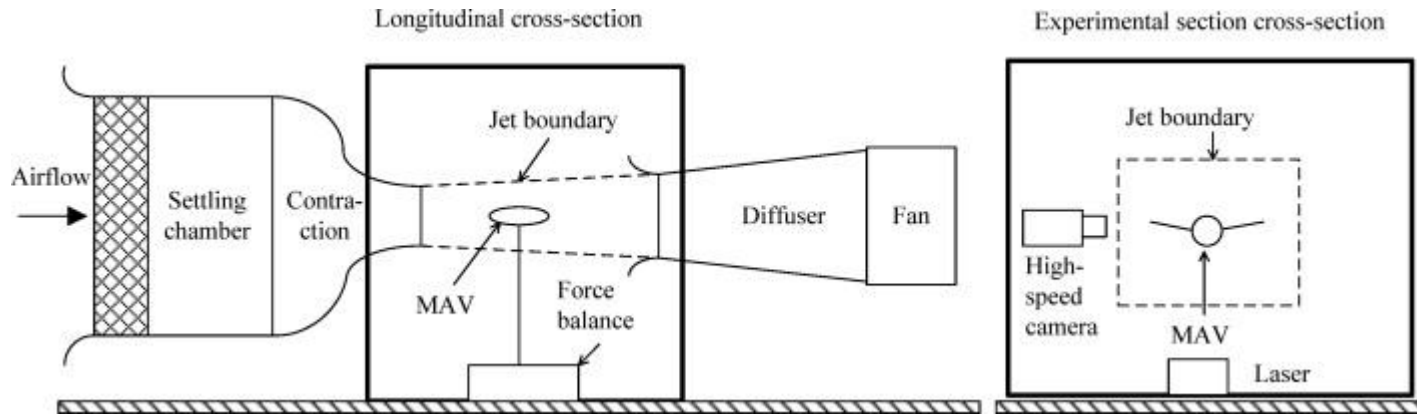


Application



Unit-II WIND TUNNEL EXPERIMENTATION CONSIDERATIONS

Low Speed Wind Tunnels

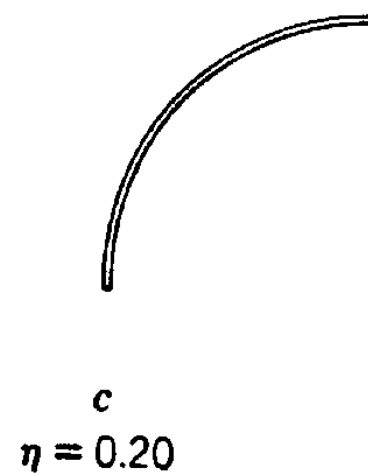
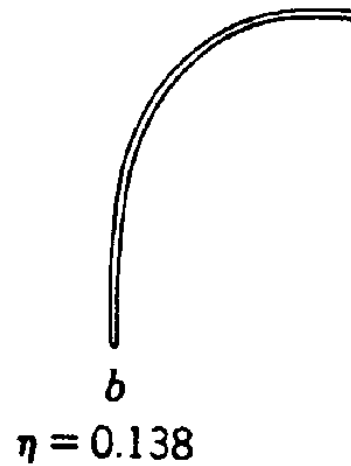
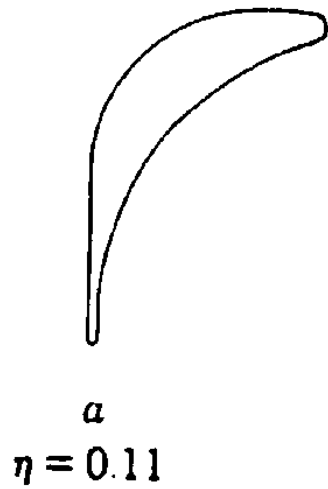


Principal Components

- ❖ Settling Chamber
- ❖ Contraction Cone
- ❖ Test Section
- ❖ Diffuser
- ❖ Drive Section.

Corners

$\eta = 1.0$



Function

Stilling Section - Low speed and uniform flow

Honeycomb - Reduces Large Swirl Component of Incoming Flow

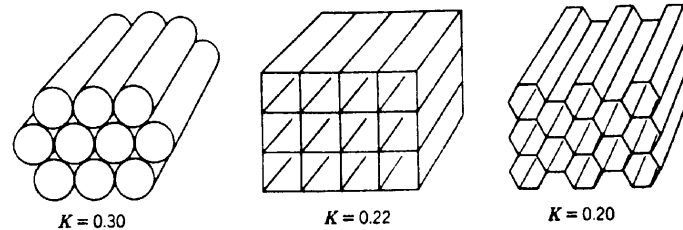


Fig. 2:16 Some honeycombs and their losses.

Screens - Reduce Turbulence [Reduces Eddy size for Faster Decay]

- Used to obtain a uniform test section profile
- Provide a flow resistance for more stable fan operation

Test Section

Test Section - Design criteria of Test Section Size and Speed Determine Rest of Tunnel Design

Test Section Reynolds Number

Larger JET - Lower Speed - Less Power - More Expensive

Section Shape - Round-Elliptical, Square, Rectangular-Octagonal with flats for windows-mounting platforms

Rectangular with filled corners

Not usable but requires power

For Aerodynamics Testing 7x10 Height/Width Ratio

Test Section Length - $L = (1 \text{ to } 2)w$

Energy Ratio

$$(E.R.)_t = \frac{\text{Jet Energy}}{\sum \text{Circuit Losses}} = \frac{1/2 \rho_0 U_0^3 A_0}{\sum \text{Losses}} = \frac{q_0 U_0 A_0}{\eta P}$$

Subscript 0 refers to the test section
P is the motor power

η is the fan efficiency

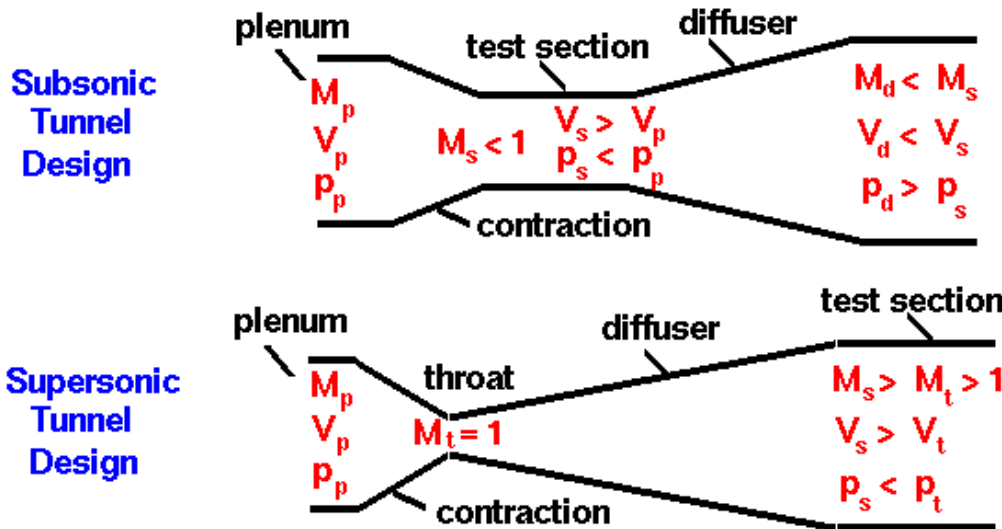
Design Requirements

Wind Tunnel Design

Increase in Area :

- For subsonic flow ($M < 1$)
velocity decreases & pressure increases
- For supersonic flow ($M > 1$)
velocity increases & pressure decreases

M = Mach
V = velocity
p = pressure
A = area



Losses

$$K = \frac{P_{t1} - P_{t2}}{q}$$

Local Pressure Loss Coefficient

$$K_0 = \frac{P_{t1} - P_{t2}}{q_0} = K \frac{q}{q_0}$$

Pressure Loss Referred to Test Section

$$\Delta E = K_0 \frac{1}{2} \rho_0 U_0^3 A_0$$

Section Energy Loss

$$(E.R.)_t = \frac{\text{Jet Energy}}{\sum \text{Circuit Losses}} = \frac{\frac{1}{2} \rho_0 U_0^3 A_0}{\sum K_0 \frac{1}{2} \rho_0 U_0^3 A_0} = \frac{1}{\sum K_0}$$

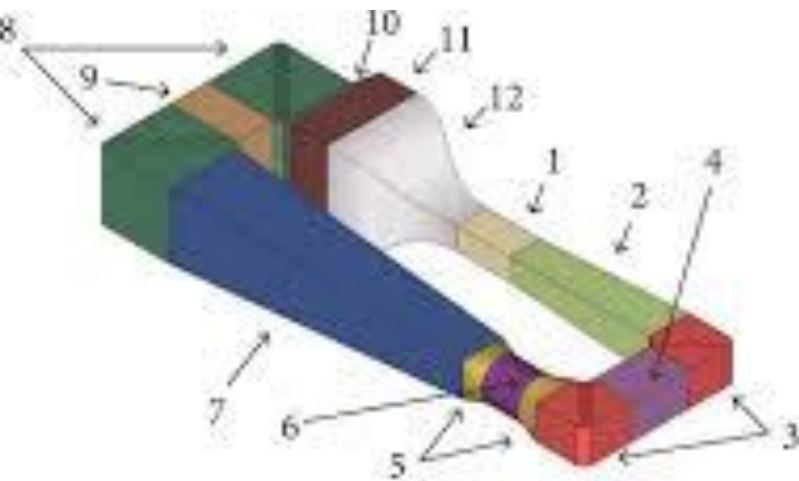
Constraints And Loss Coefficients.

Example Open Return Tunnel

	Section	Ko	% Total Loss
1	Inlet Including Screens	.021	14.0
2	Contraction and Test Section	.013	8.6
3	Diffuser	.080	53.4
4	Discharge at Outlet	.036	24.0
	Total	.150	100.0

$$(E.R.)_t = \frac{1}{\sum K_0} = \frac{1}{.150} = 6.67$$

Wind Tunnel Performance Flow Quality



- | | | | |
|---|--------------------|----|-----------------|
| 1 | Test section | 7 | Big diffuser |
| 2 | Small diffuser | 8 | Corners 3 and 4 |
| 3 | Corners 1 and 2 | 9 | Big connector |
| 4 | Small connector | 10 | Expansor |
| 5 | Variable junctions | 11 | Setting chamber |
| 6 | Drive system | 12 | Contraction |

Power Losses

$$\text{Reynolds number} = \frac{\text{inertia force}}{\text{viscous force}} = \frac{\rho V l}{\mu}$$

$$\text{Mach number} = \frac{\text{inertia force}}{\text{elasticity force}} = \frac{V}{a}$$

$$\text{Froude number} = \sqrt{\frac{\text{inertia force}}{\text{gravity force}}} = \sqrt{\frac{V^2}{lg}}$$

Wind Tunnel Corrections

Wall Interference

- It is a major concern for wind tunnel design, model shape and experimental techniques
- Wind Tunnel Walls effect the free flow conditions and needs to be corrected in measurements
- It becomes most serious when the airflow began to choke in the transonic range.

$$\text{Blockage Ratio (BR)} = \frac{\text{Projected Area of the Model}}{\text{Projected Area of Wind Tunnel Test Section}}$$

- Models with higher blockage ratios create more wall interference

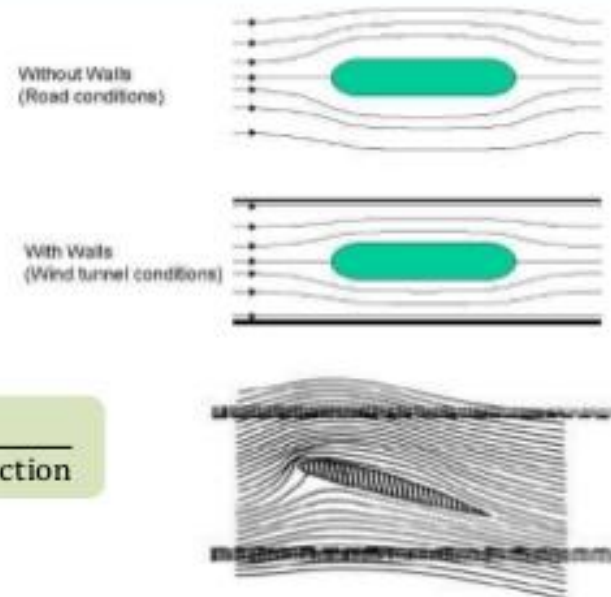
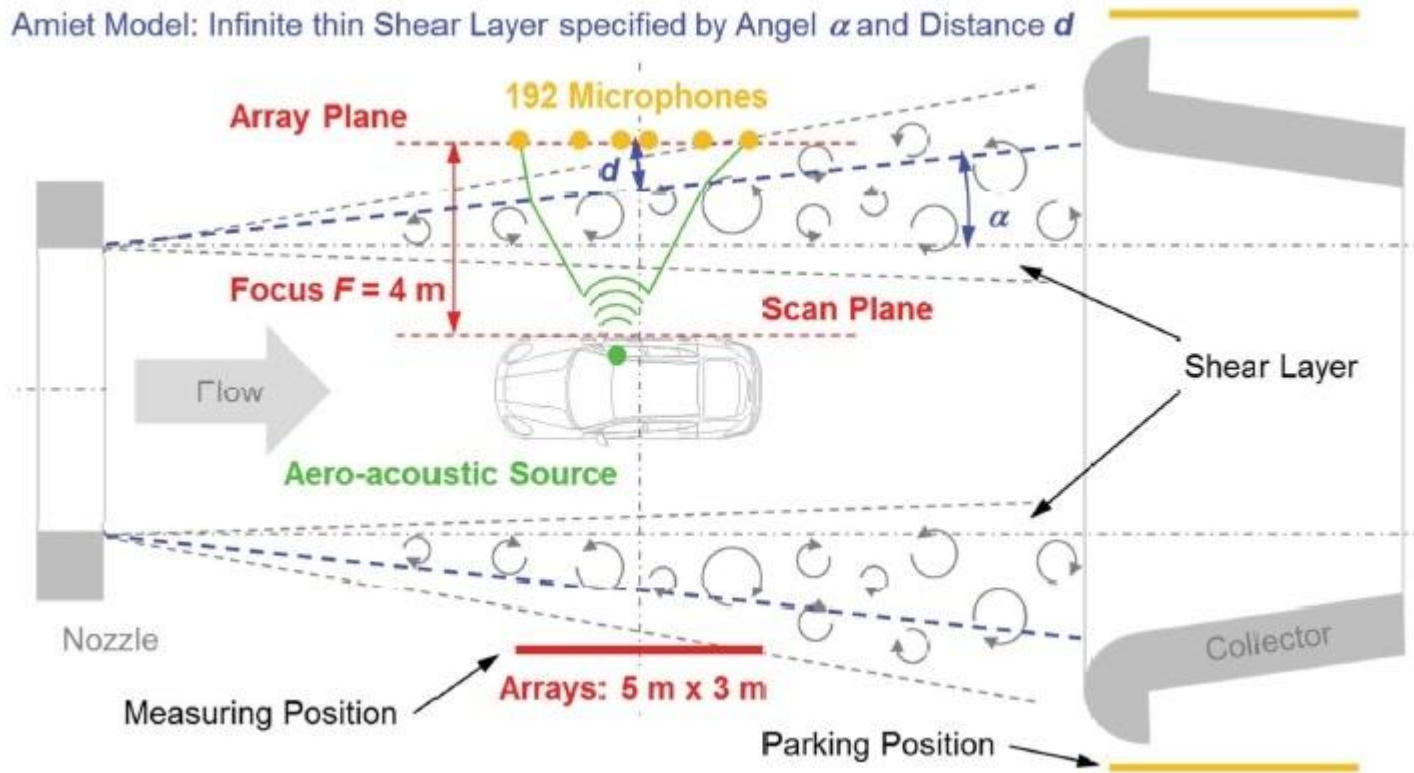


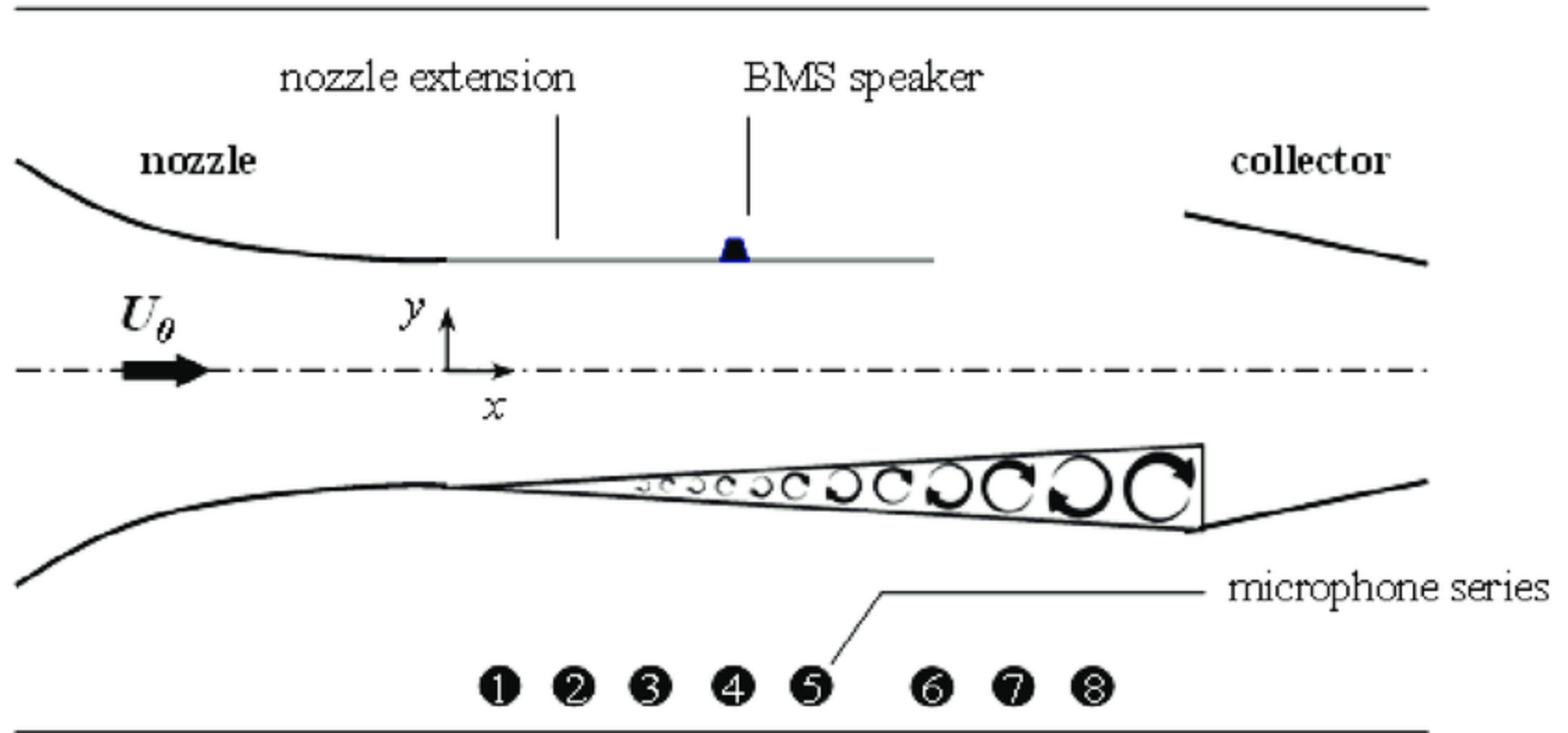
Figure: Constraining effect of streamlines due to wall interference (Courtesy: NASA)

Sources of Inaccuracies

Amiet Model: Infinite thin Shear Layer specified by Angle α and Distance d

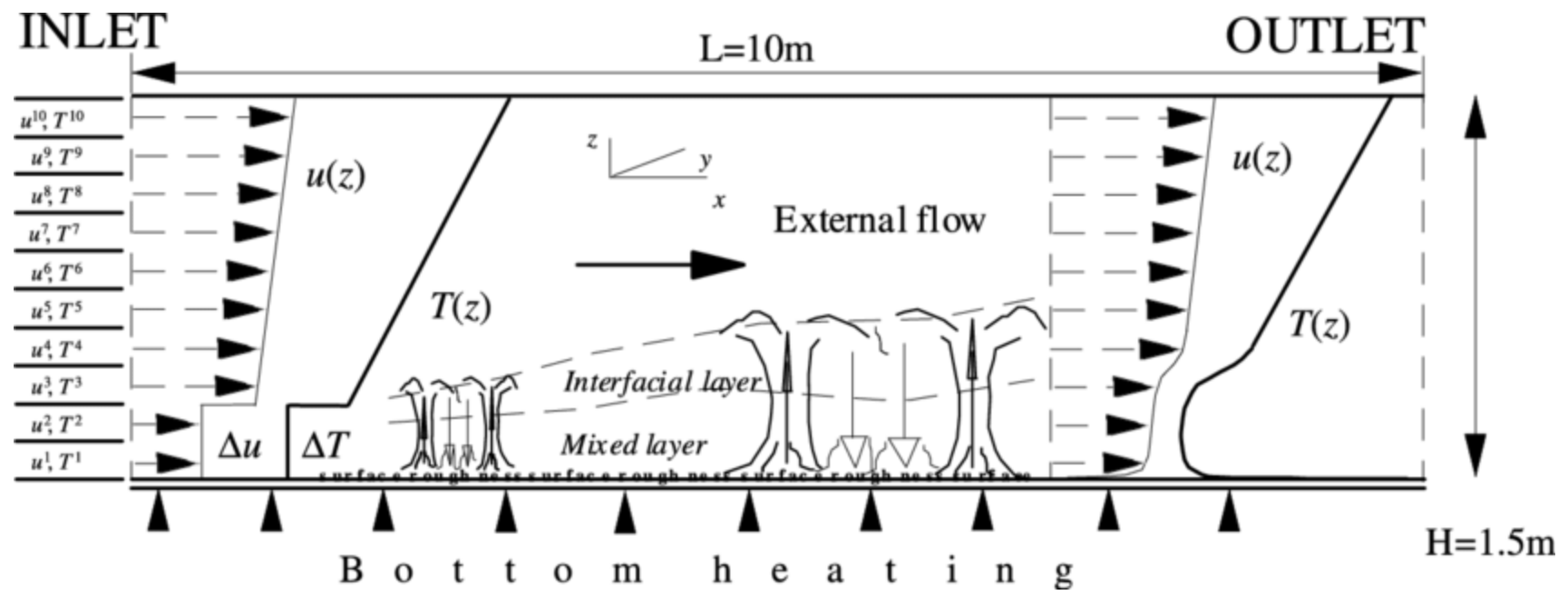


Unit-II

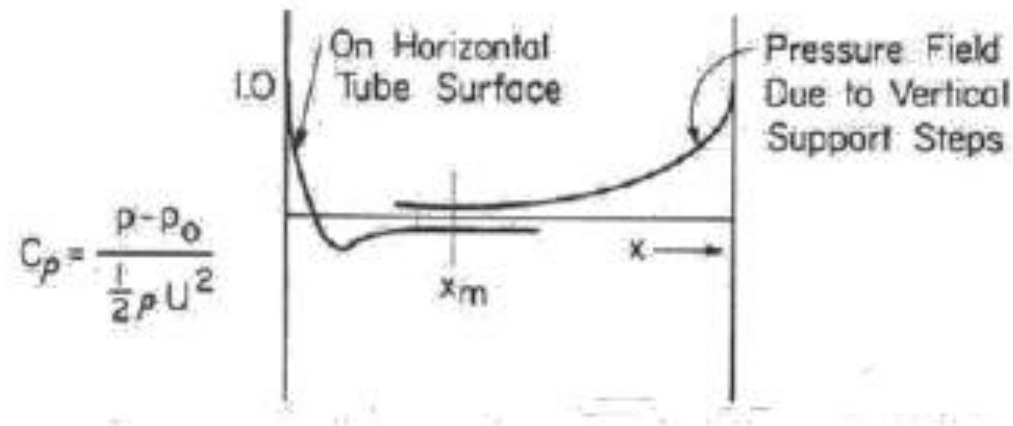


Unit-II

Buoyancy

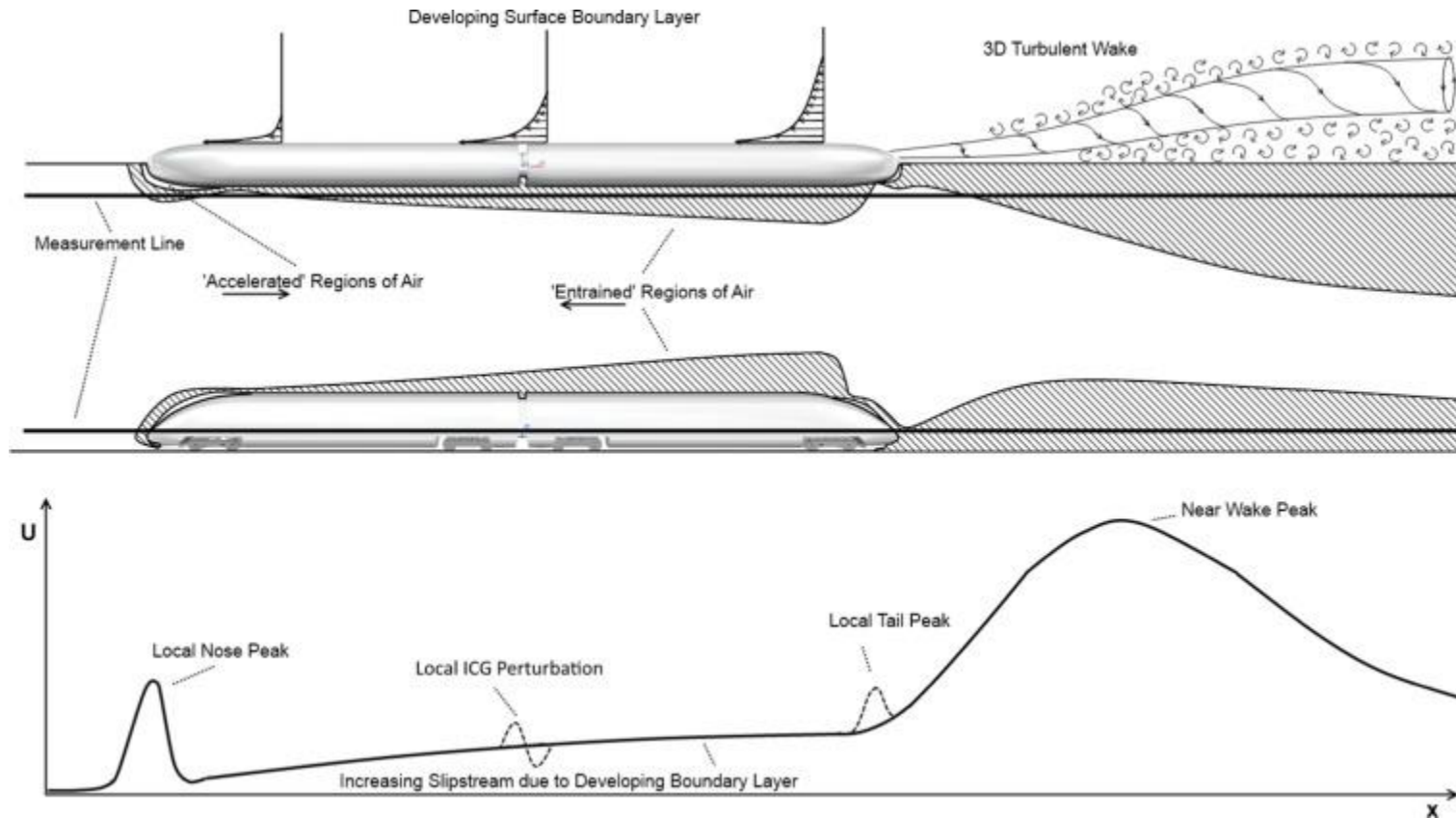


Solid Blockage

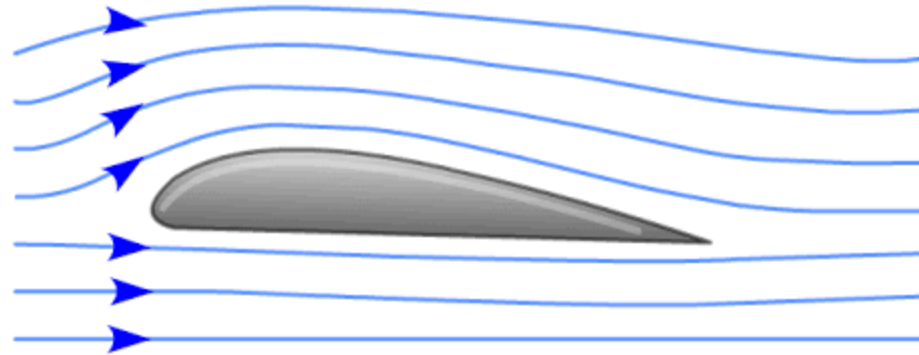


- Nose acceleration and probe support effects may compensate

Wake Blockage



Streamline Curvature Causes



→ The shape of wing forces air to move faster over the top surface.

WIND TUNNEL BALANCE

Load Measurement:

1. Low Speed Wind Tunnel Balances
2. Mechanical & Strain Gauge Types
3. Null Displacement Methods & Strain Method
4. Sensitivity
5. Weigh Beams
6. Steel Yard Type
7. Current Balance Type
8. Balance Linkages
9. Levers and Pivots

Model Support

1. Three Point Wire Support
2. Three Point Strut Support
3. Platform Balance
4. Yoke Balance
5. Strain Gauge
6. 3-component Strain Gauge Balance
7. Description and Application

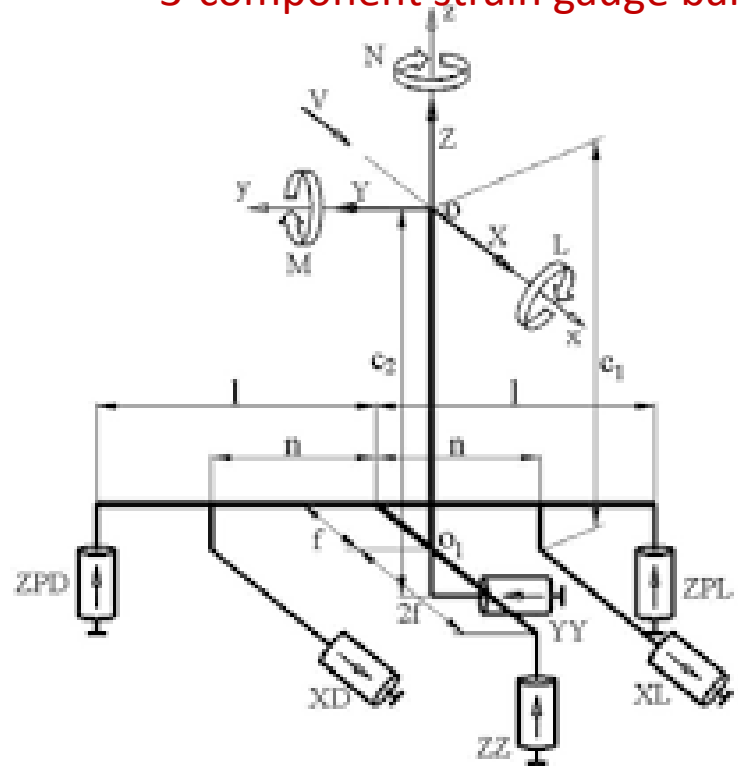
Balance Linkages, Levers And Pivots



Unit-III

Model Support Three Point Wire Support

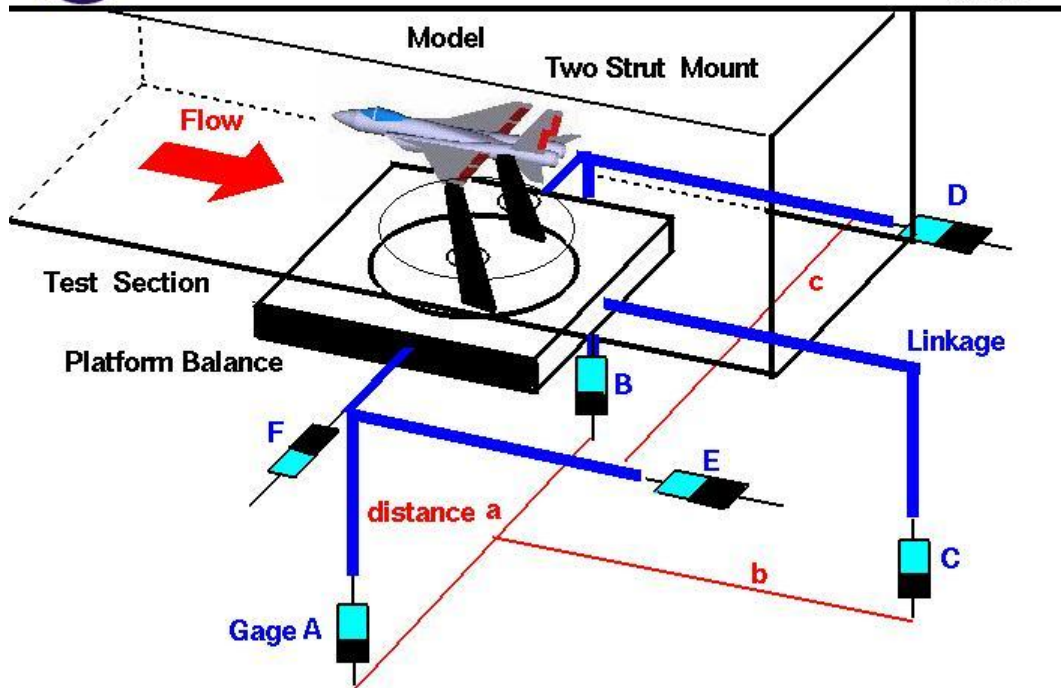
3-component strain gauge balance





External Force Balance

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Model Mounts

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External Balance



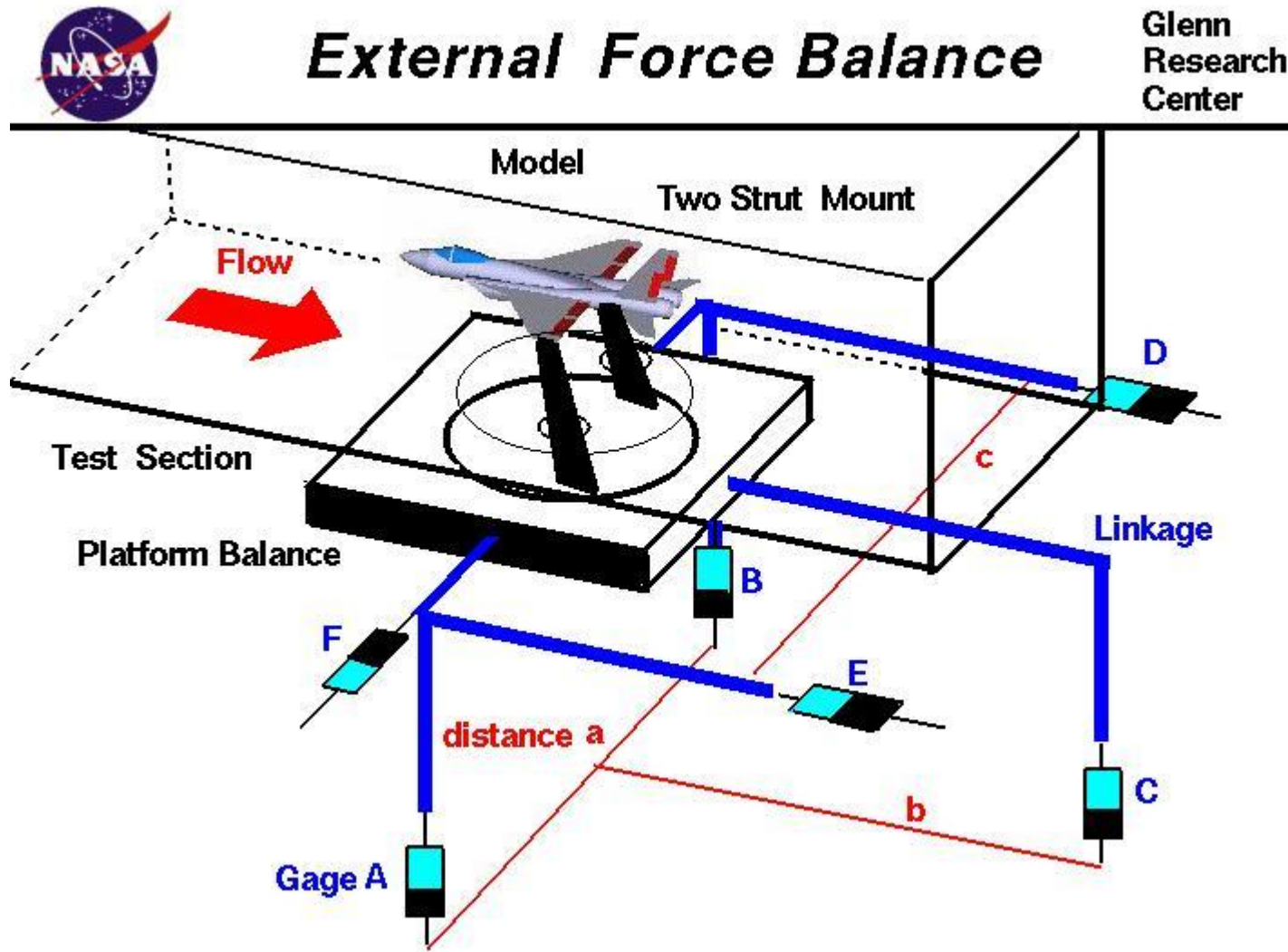
Internal or
External Balance



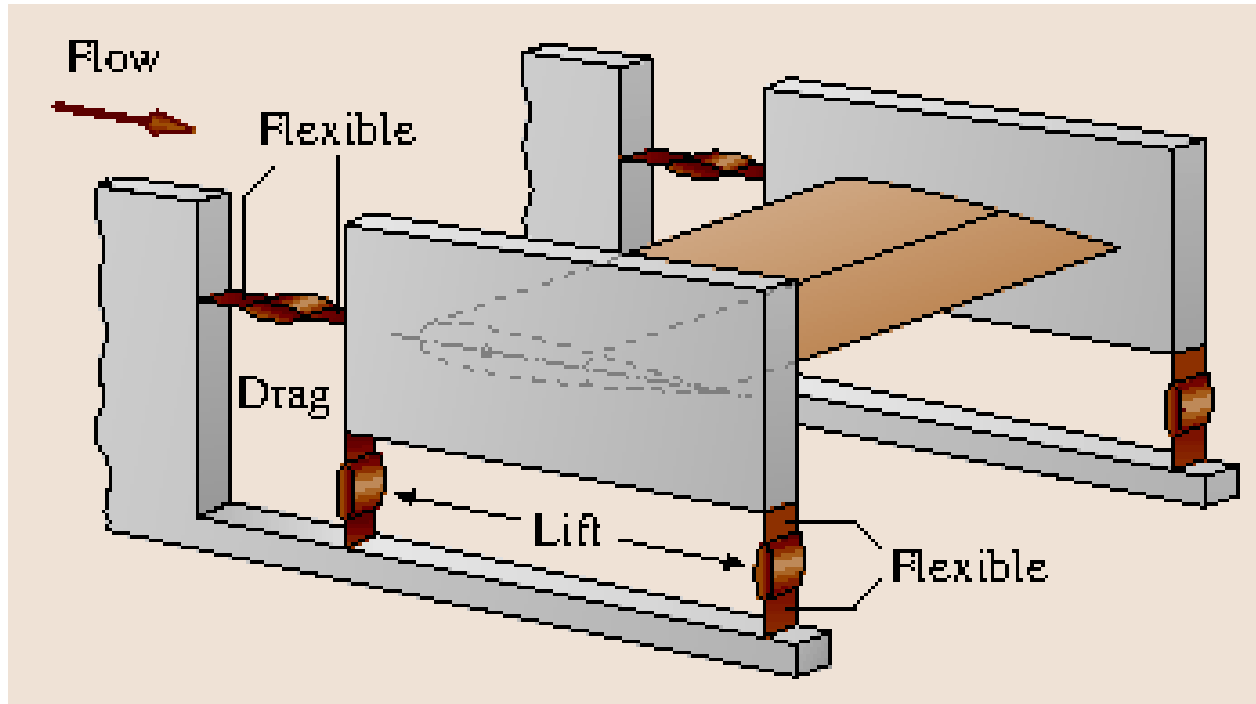
Three Point Strut Support



Platform Balance



Yoke Balance

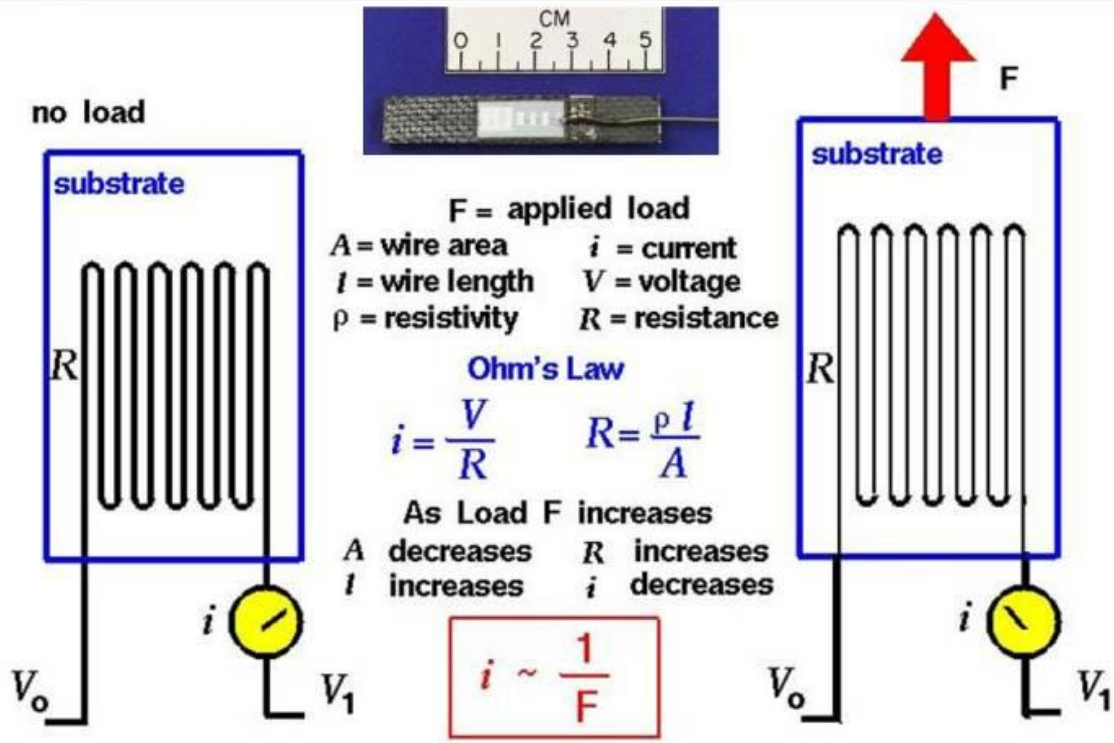


Strain Gauge



Strain Gage

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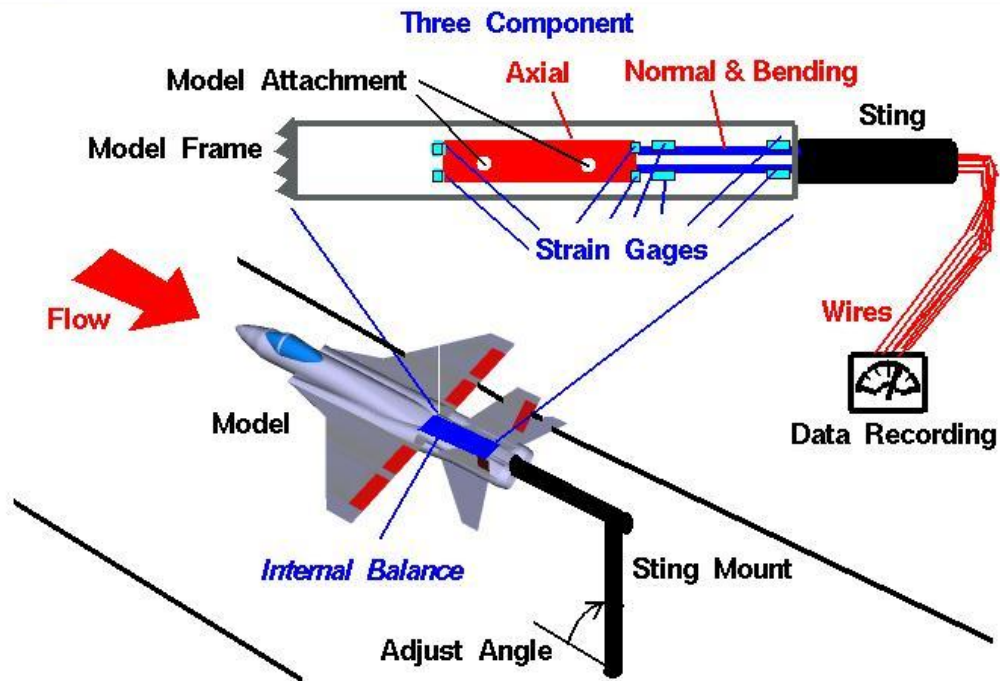


3-component Strain Gauge Balance

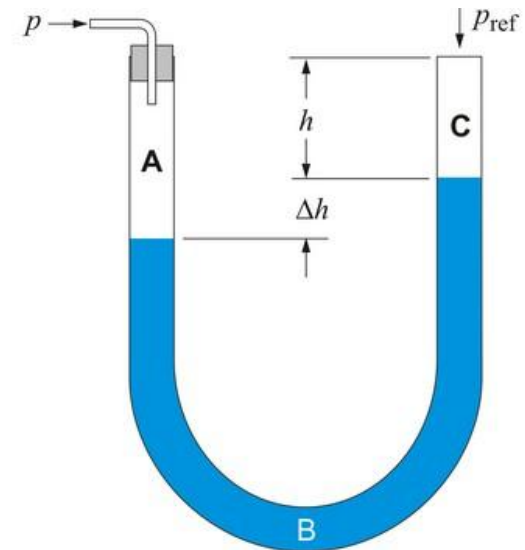
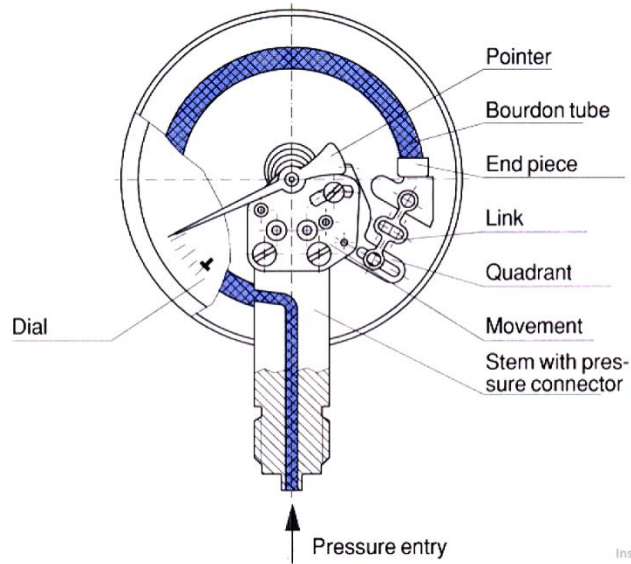


Internal Force Balance

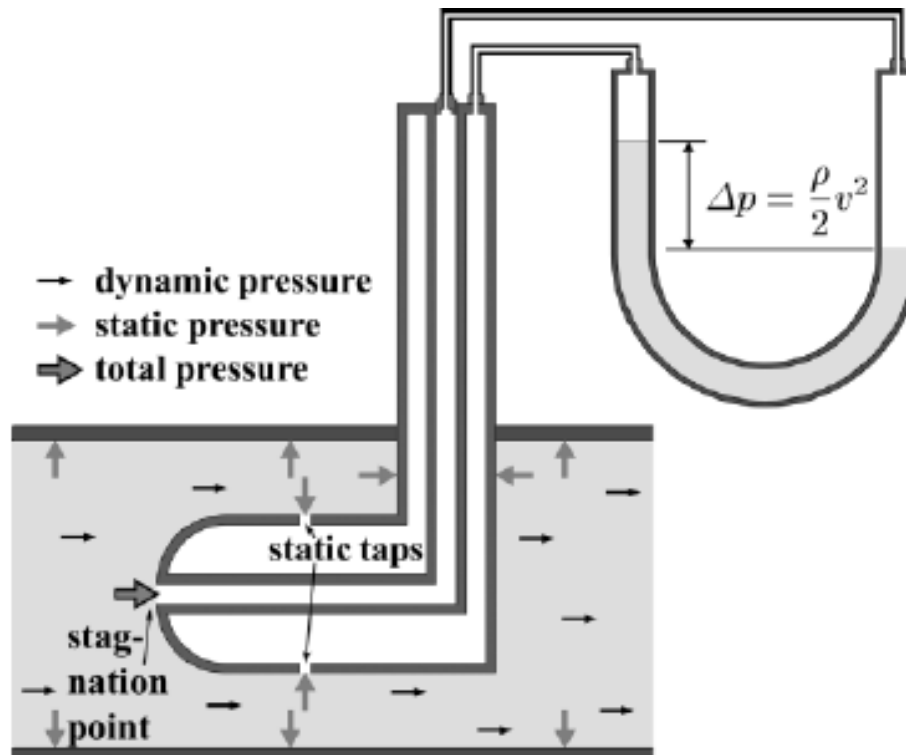
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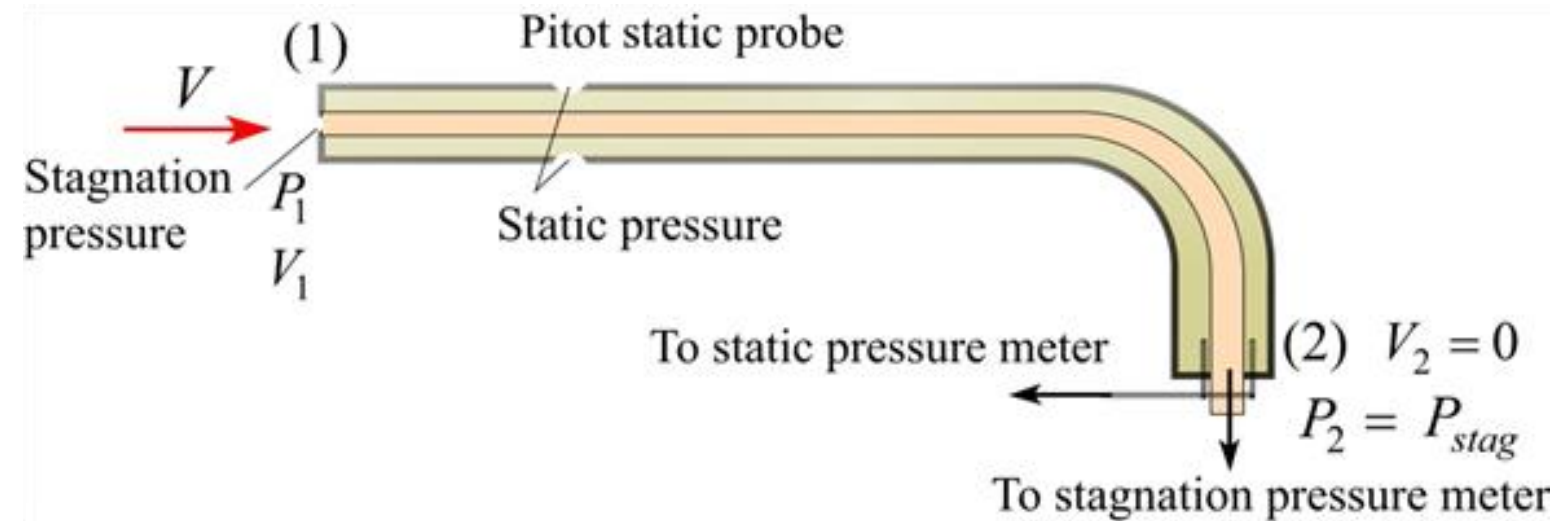
Pressure



Static Pressure



Surface Pressure Orifice

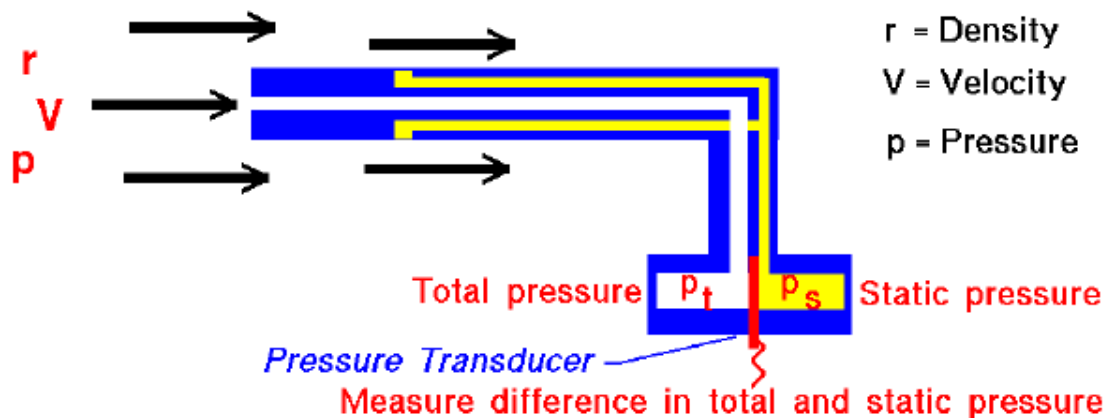


Static Probes



Pitot Tube

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Bernoulli's Equation :

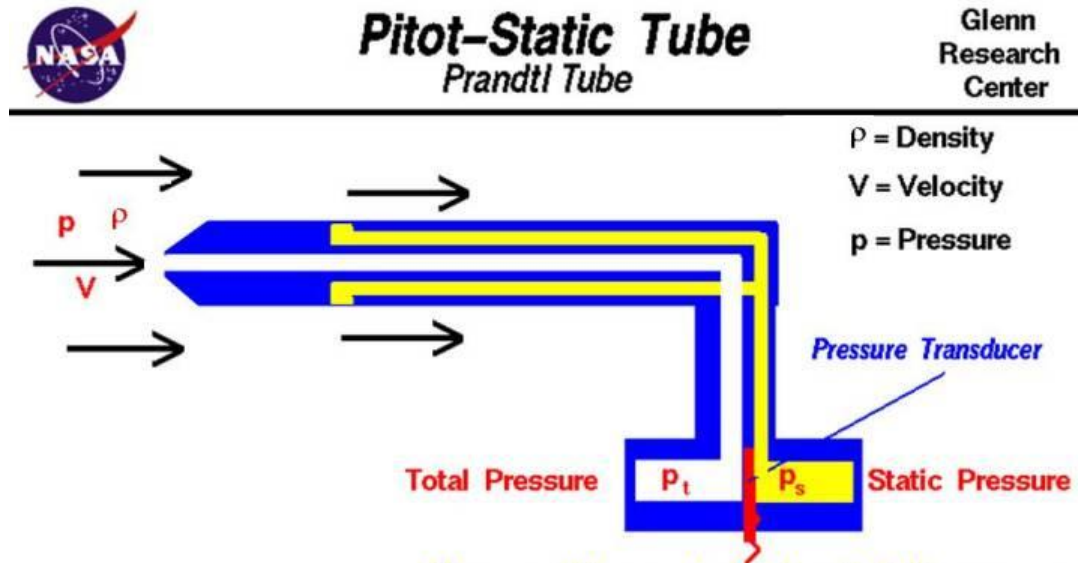
static pressure + dynamic pressure = total pressure

$$(p_s + \frac{r \times V^2}{2}) = p_t$$

Solve for Velocity :

$$V^2 = \frac{2(p_t - p_s)}{r}$$

Pitot Probe For Total Pressure



Bernoulli's Equation:

static pressure + dynamic pressure = total pressure

$$\left(p_s + \rho \times \frac{V^2}{2} \right) = p_t$$

Solve for Velocity:

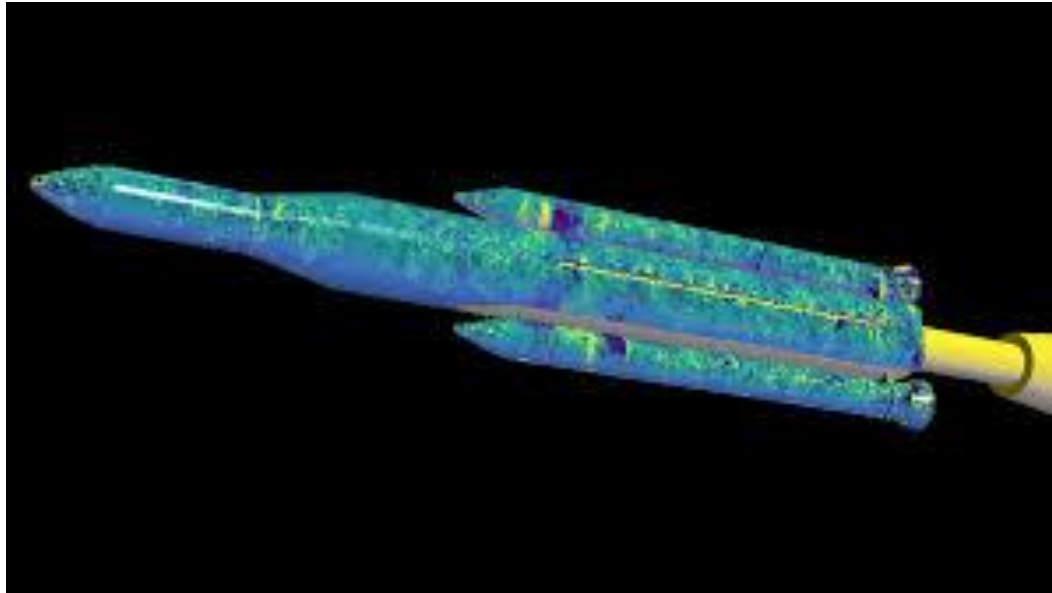
$$V^2 = \frac{2(p_t - p_s)}{\rho}$$

Measure difference in total and static pressure

Static Pressure and Flow Angularity



Pressure Sensitive Paints

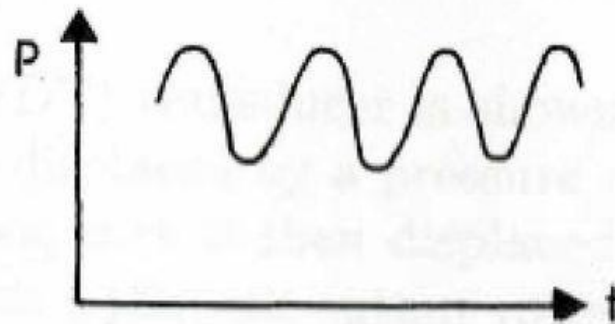
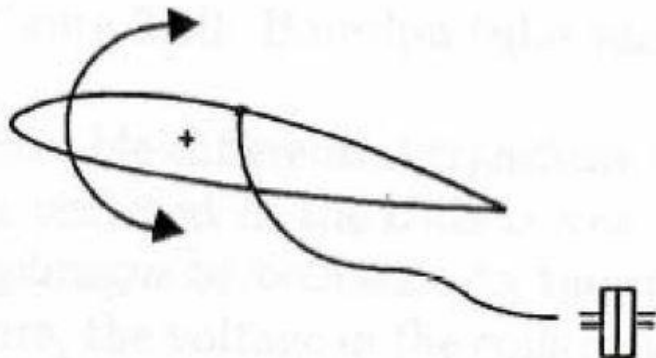


Steady And Unsteady Pressure Measurement

Unsteady Pressure Measurements

An airfoil (or any other body) immersed in an unsteady mainstream, or a steady mainstream but subjected to change of incidence, periodic or not (oscillating airfoil, or subjected to a pitch-up maneuver)

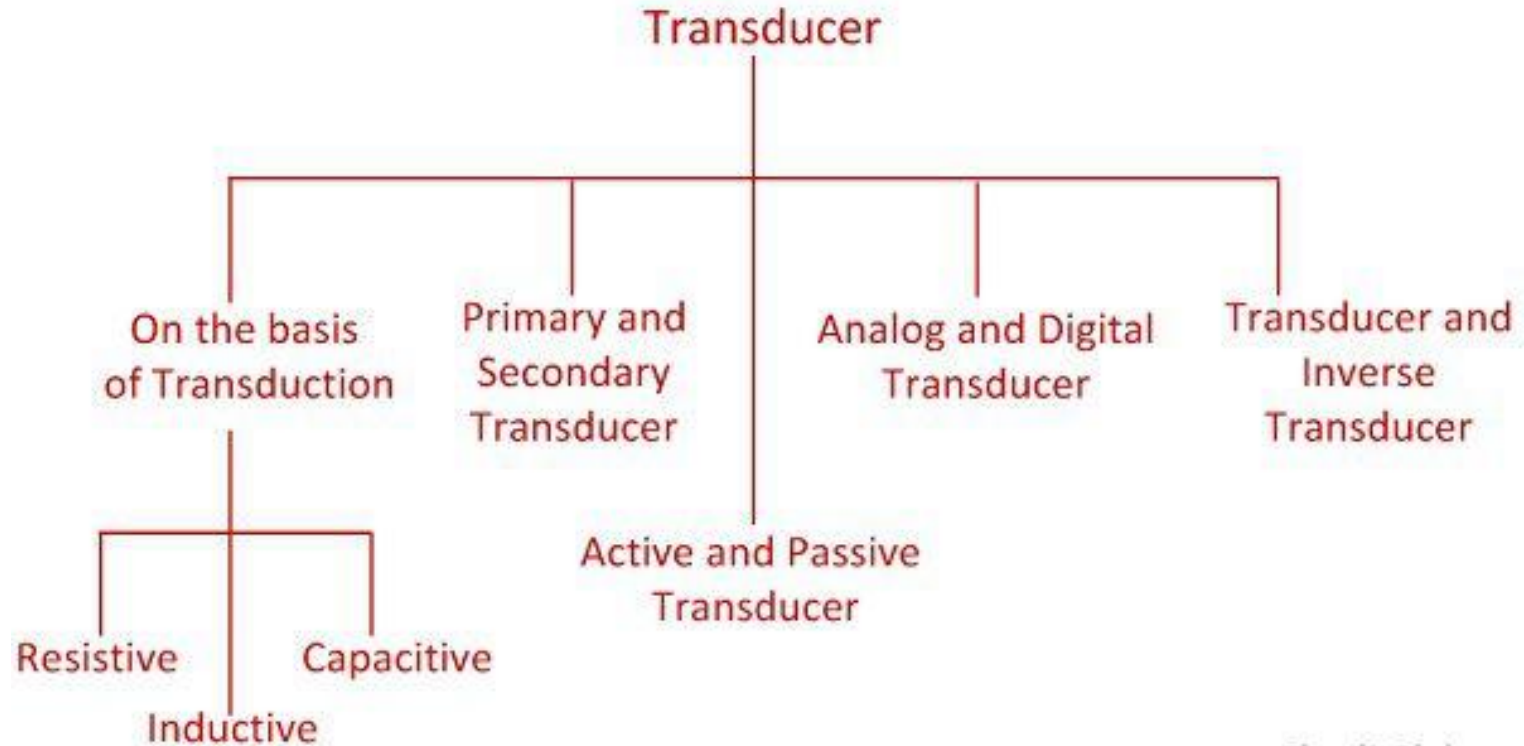
OSCILLATING AIRFOIL



Different cases of occurrence of unsteady pressures

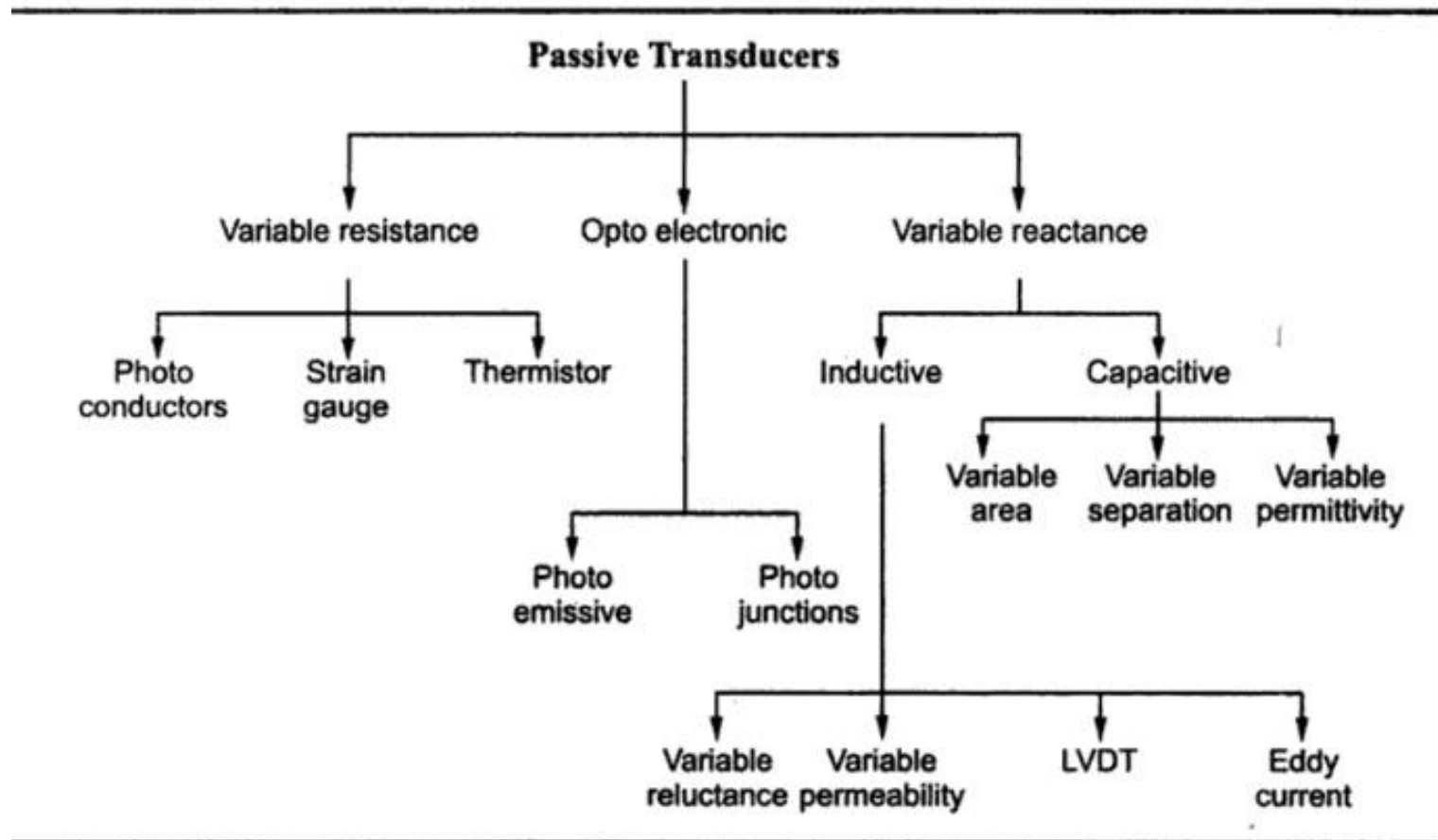
Various Types of Pressure Probes

Transducers

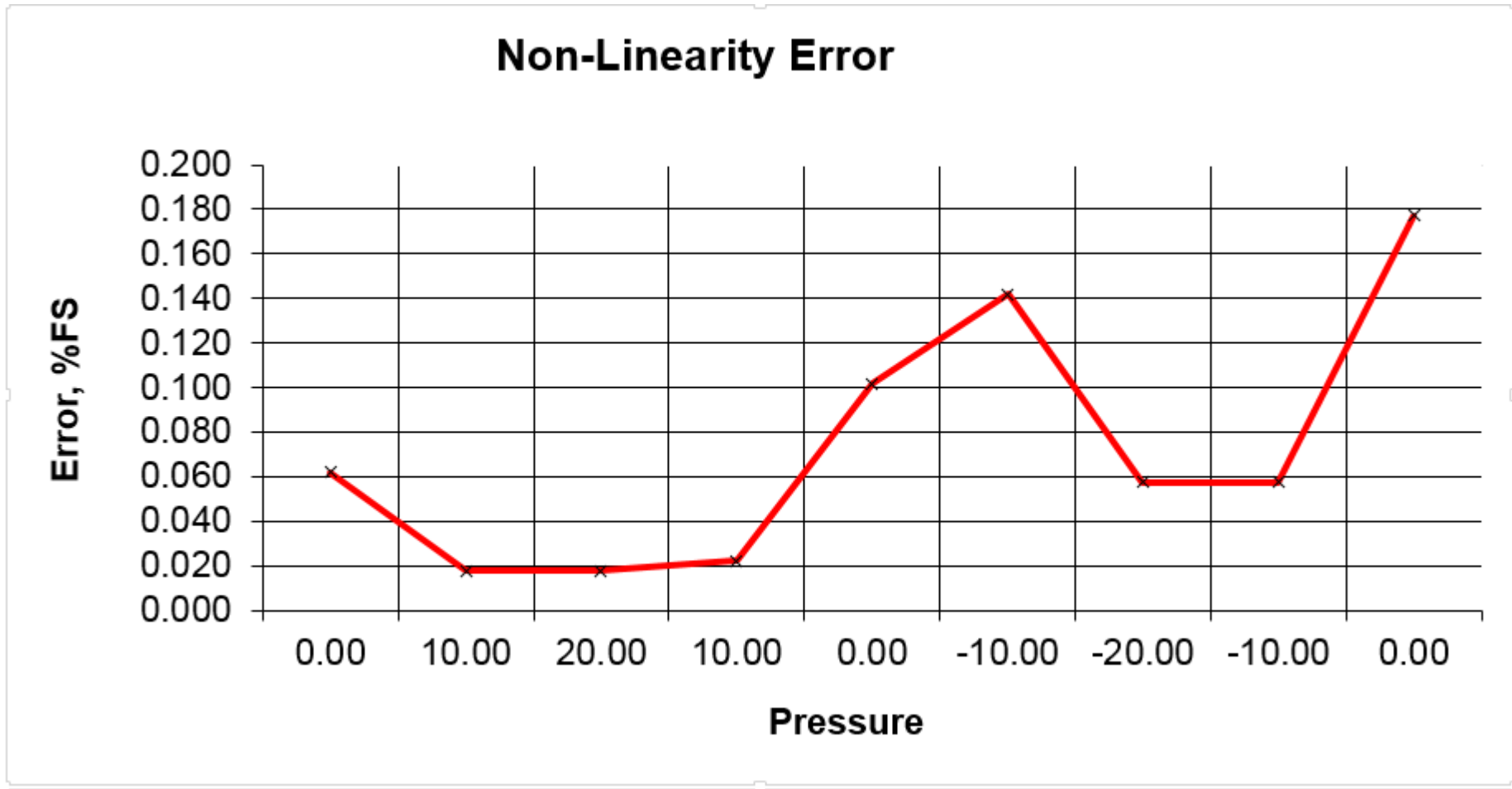


Circuit Globe

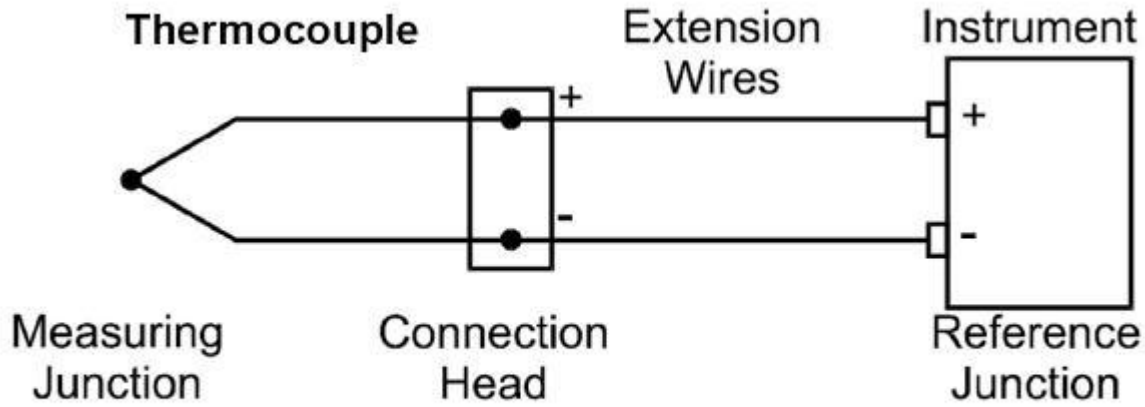
Transducers

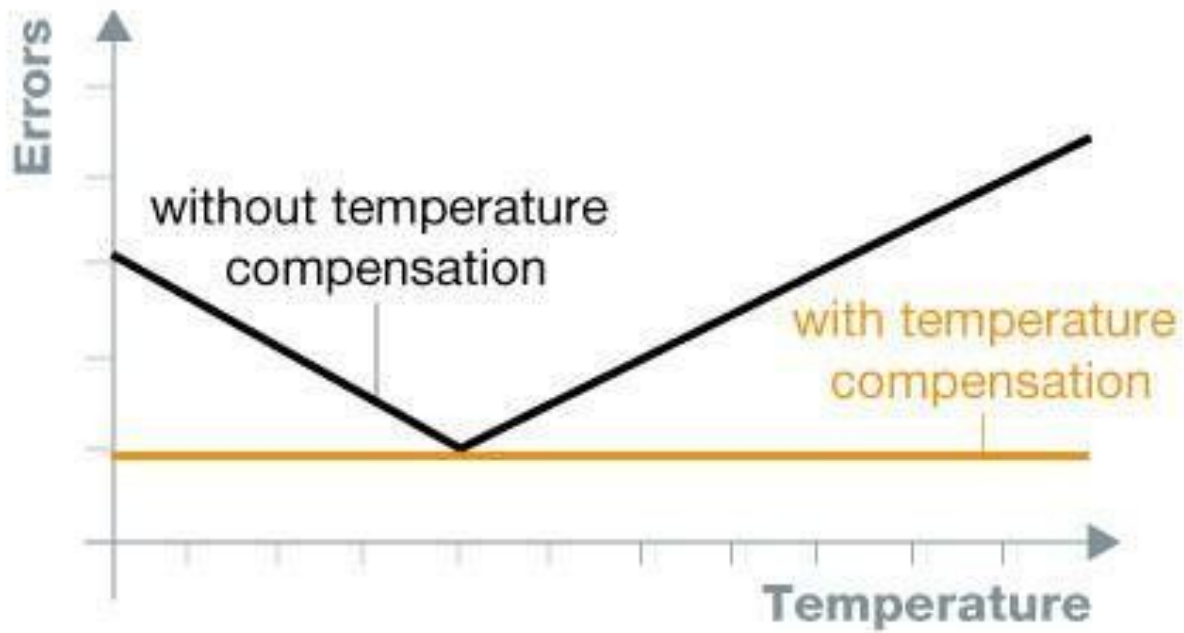


Errors in Pressure Measurement

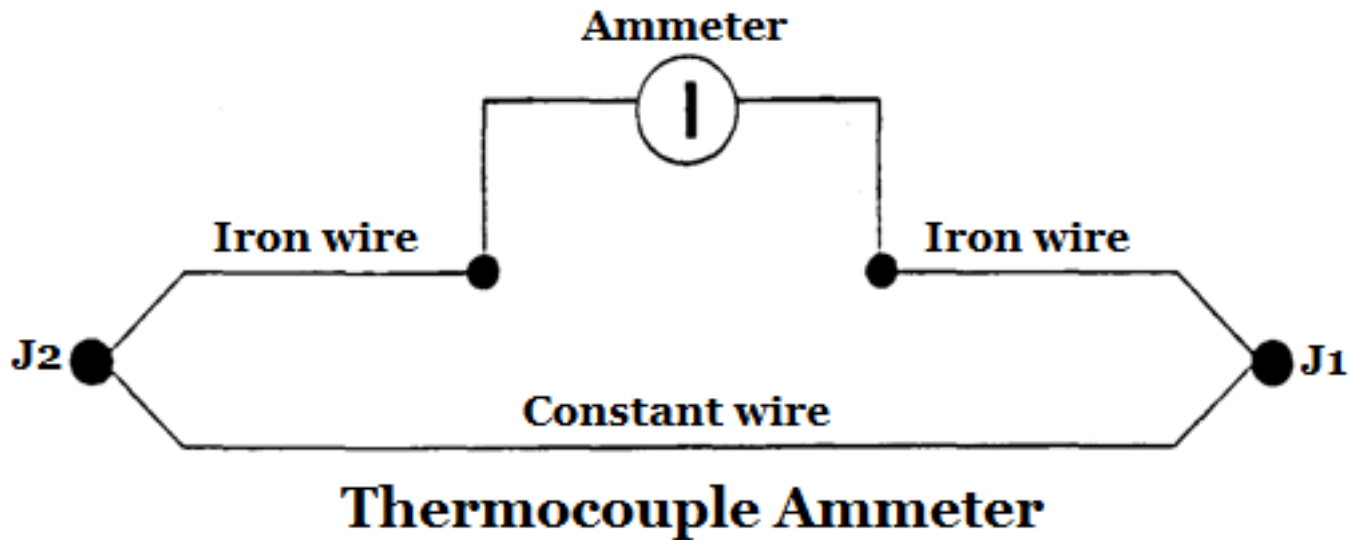


Temperature

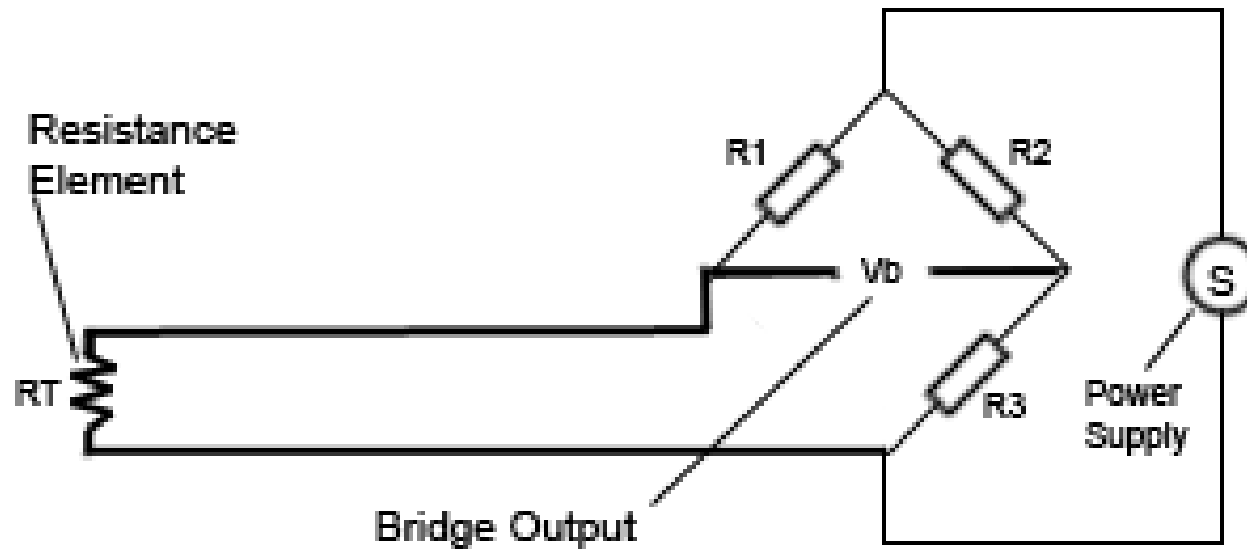




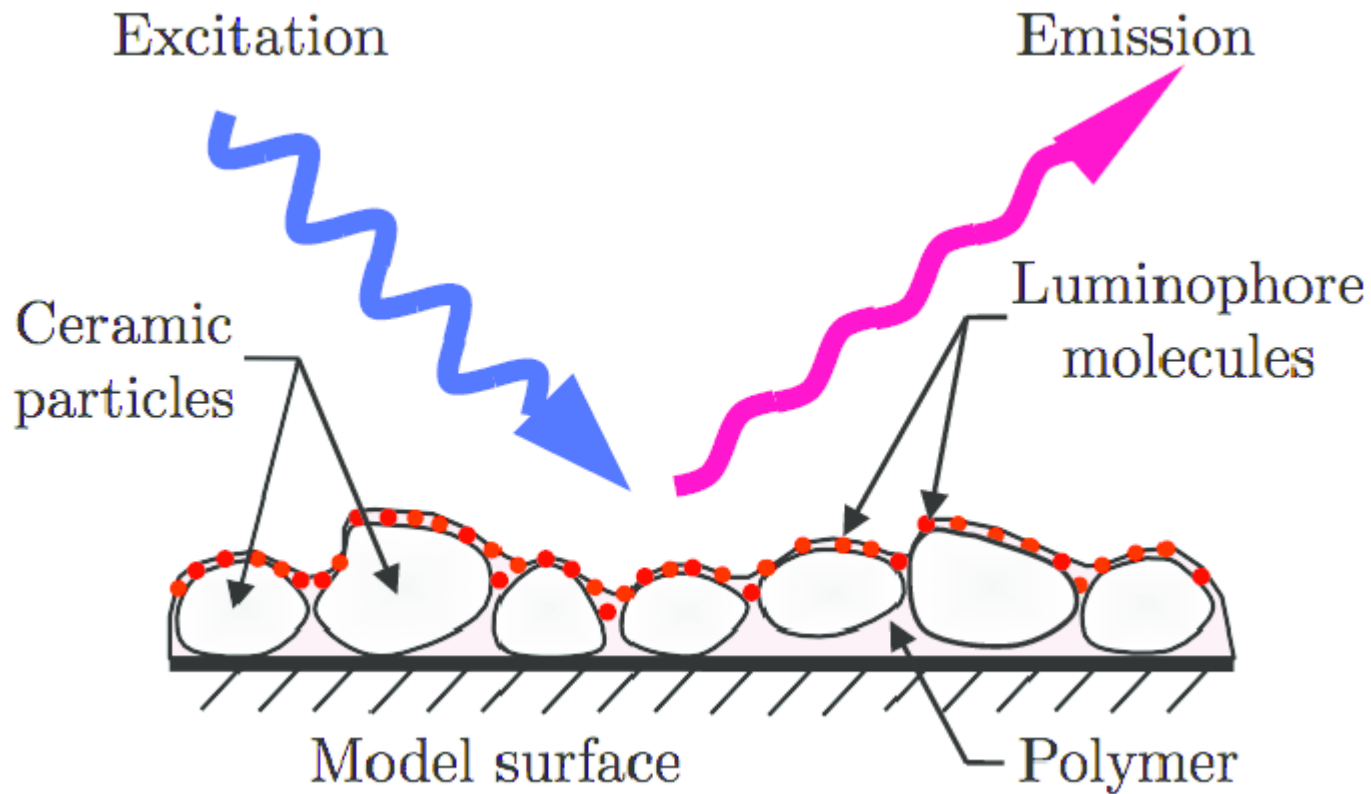
Measurement of Temperature using Thermocouples



Resistance Thermometers

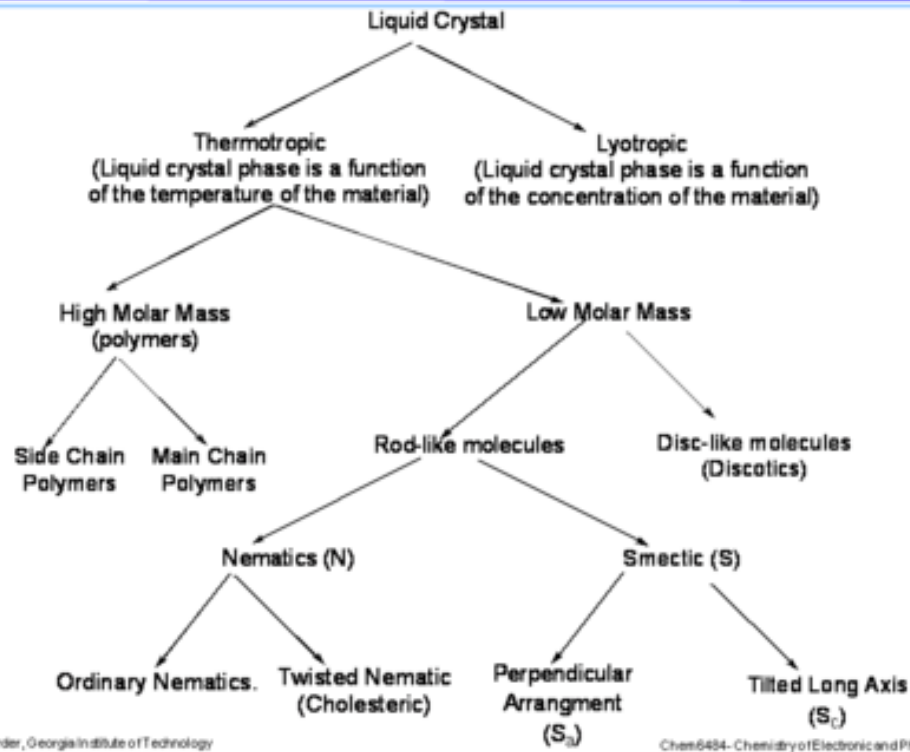


Temperature Sensitive Paints



Liquid Crystals

Classification of Liquid Crystals

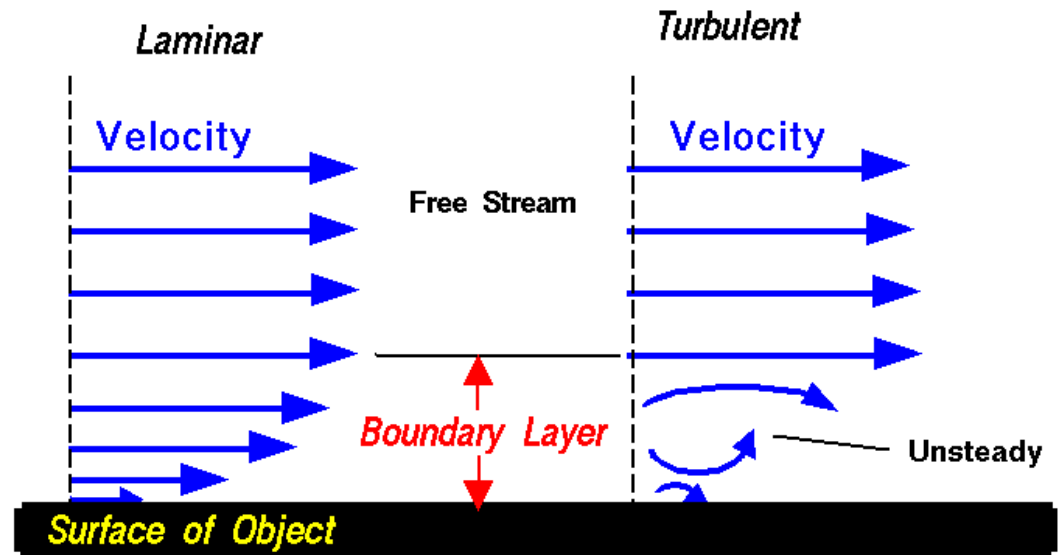
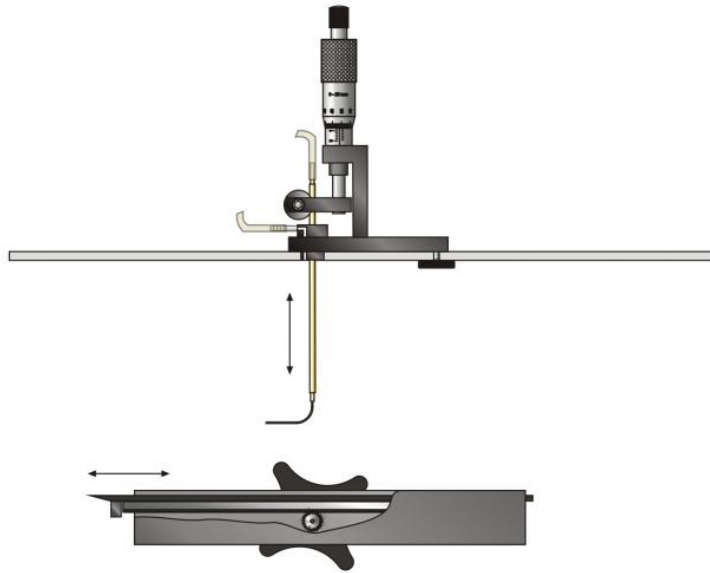


Boundary Layer Profile Using Pitot Static Probe



Boundary Layer

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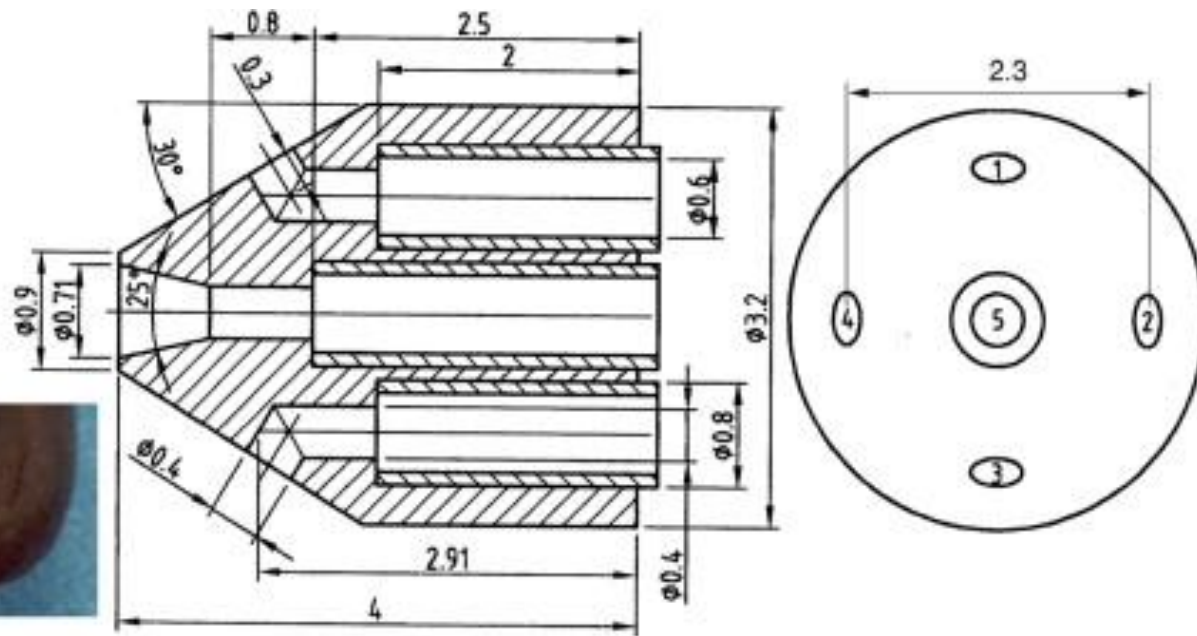
Velocity is zero at the surface (no - slip)

5 Hole Probe Yaw Meter

front view



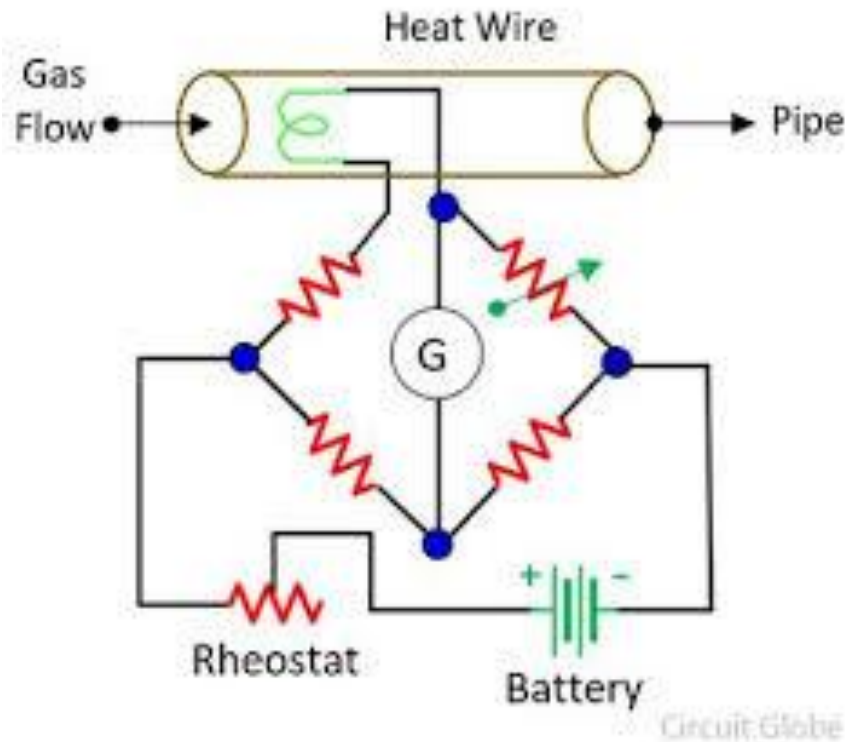
lateral view



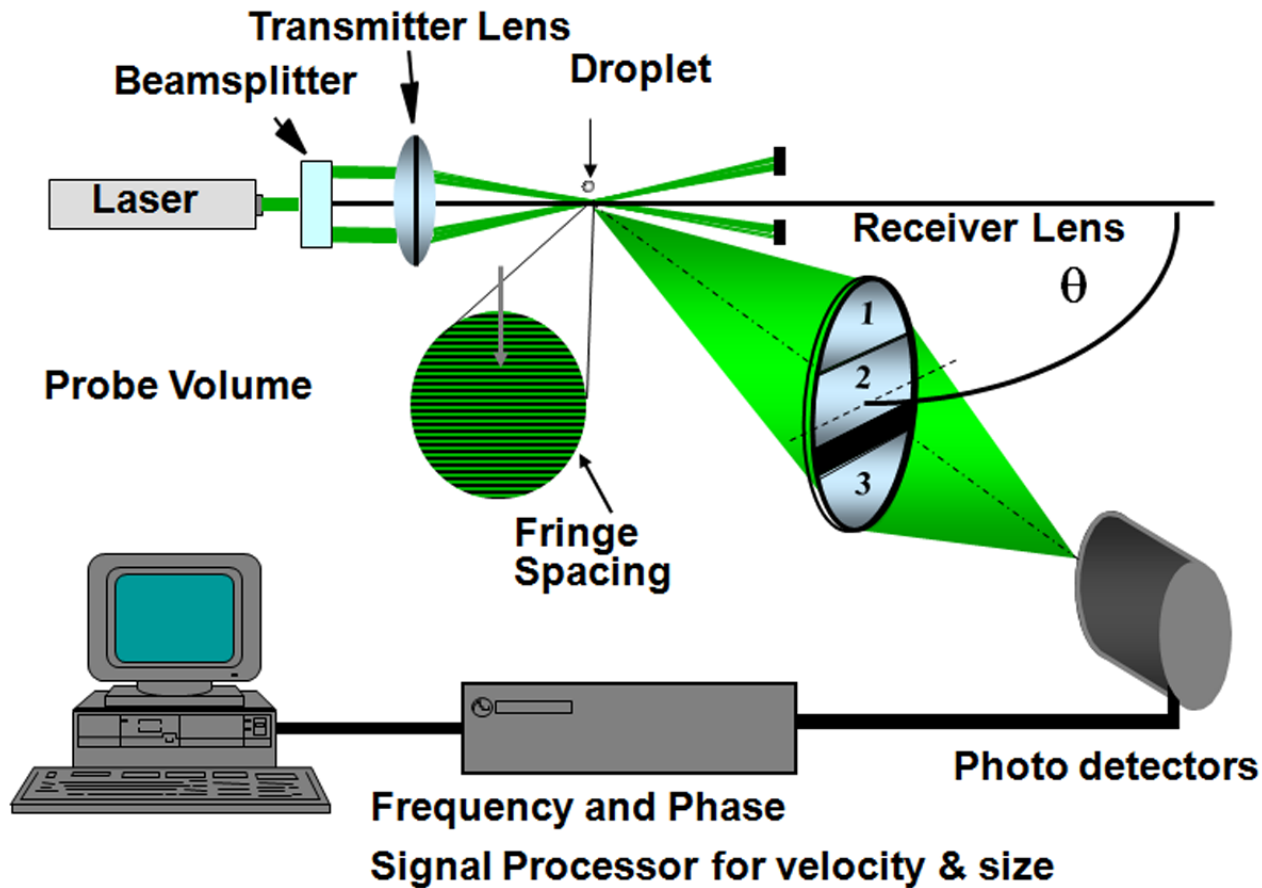
Total Head Rake



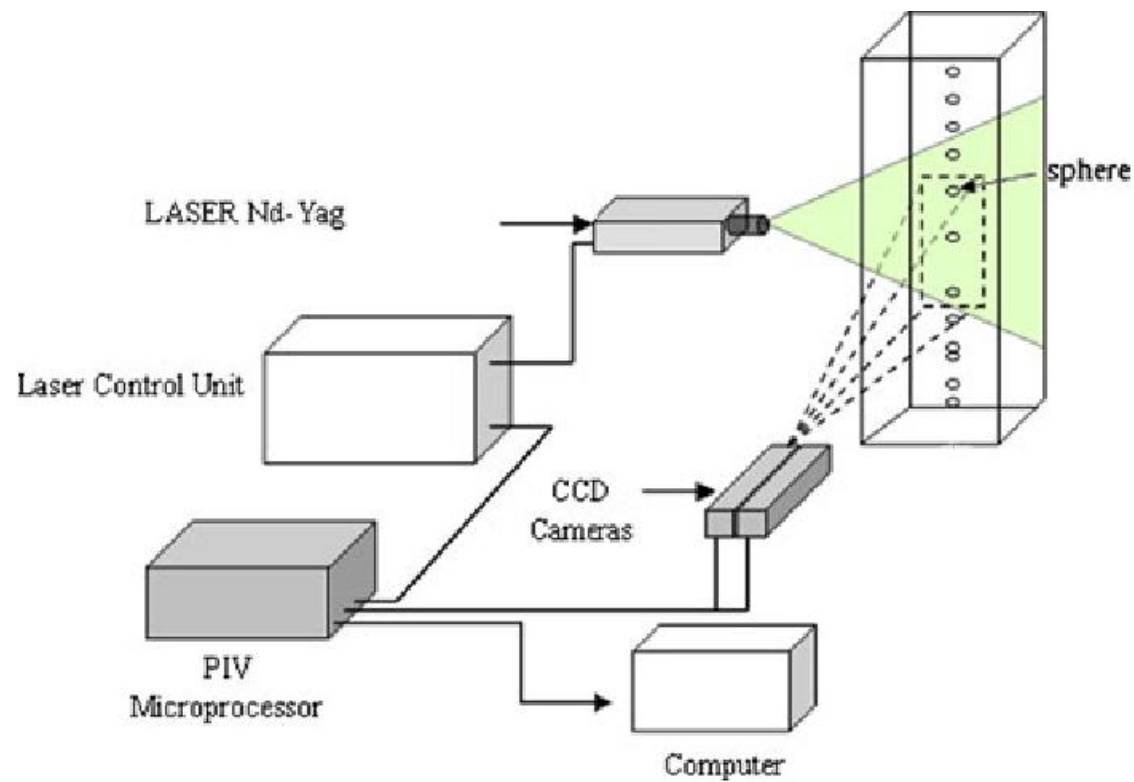
Hot Wire Anemometry



Laser Doppler Anemometry



Particle Image Velocimetry



Vector Visualization

- ⦿ Data set is given by a vector component and its magnitude
- ⦿ often results from study of fluid flow or by looking at derivatives (rate of change) of some quantity
- ⦿ trying to find out what to see and how!
- ⦿ Many visualization techniques proposed

Vector Visualization - Techniques

- **Hedgehogs/glyphs**
- **Particle tracing**
- **stream-, streak-, time- & path-lines**
- **stream-ribbon, stream-surfaces, stream-polygons, stream-tube**
- **hyper-streamlines**
- **Line Integral Convolution**

Vector Visualization - Origin

- ◎ **Where are those methods coming from??**
- ◎ **Rich field of Fluid Flow Visualization**
- ◎ **Hundreds of years old!!**
- ◎ **Modern domain - Computational Field Simulations**

Flow Visualization

- ◎ **Gaseous flow:**
 - development of cars, aircraft, spacecraft
 - design of machines - turbines, combustion engines
- ◎ **Liquid Flow:**
 - naval applications - ship design
 - civil engineering - harbor design, coastal protection
- ◎ **Chemistry - fluid flow in reactor tanks**
- ◎ **Medicine - blood vessels, SPECT, fMRI**

Flow Visualization (2)

- ⦿ **What is the problem definition?**
- ⦿ **Given (typically):**
 - **physical position (vector)**
 - **pressure (scalar),**
 - **density (scalar),**
 - **velocity (vector),**
 - **entropy (scalar)**
- ⦿ **steady flow - vector field stays constant**
- ⦿ **unsteady - vector field changes with time**

Flow Visualization - traditionally

- ◎ **Traditionally - Experimental Flow Vis**
- ◎ **How? - Three basic techniques:**
 - adding foreign material
 - optical techniques
 - adding heat and energy

Experimental Flow Visualize.

⦿ **Problems:**

- **the flow is affected by experimental technique**
- **not all phenomena can be visualized**
- **expensive (wind tunnels, small scale models)**
- **time consuming**

⦿ **That's where computer graphics and YOU come in!**

Vector Field Visualization Techniques

Local technique: Advection based methods -

Display the trajectory starting from a particular location

- streamlines
- contours

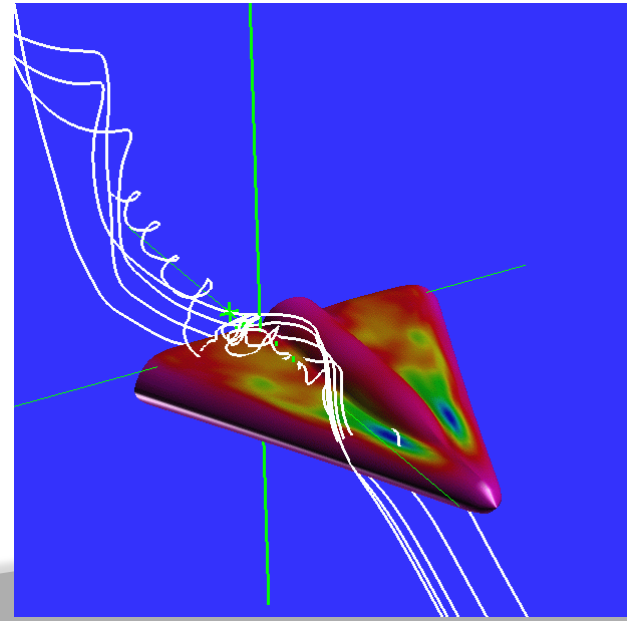
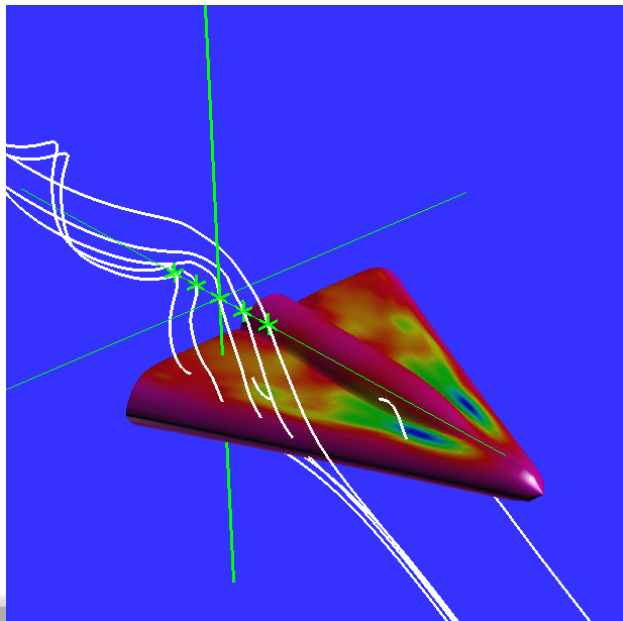
Global technique: Hedgehogs, Line Integral Convolution, Texture Splats etc.

Display the flow direction everywhere in the field

Local technique - Streamline

- Basic idea: visualizing the flow directions by releasing particles and calculating a series of particle positions based on the vector field -- streamline

$$\frac{d\bar{x}}{ds} = v(\bar{x}, t_0) \quad \text{or} \quad \bar{x} = \bar{x}(s) + \int \bar{v} ds$$



Numerical Integration

$$\frac{d\bar{x}}{ds} = v(\bar{x}, t_0) \quad \text{or} \quad \bar{x} = \bar{x}(s) + \int \bar{v} ds$$

⊙ Euler

$$\bar{x}(s + \Delta s) = \bar{x}(s) + \bar{v}(\bar{x}(s))\Delta s$$

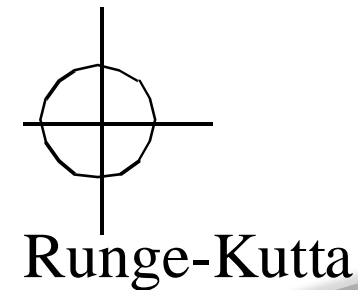
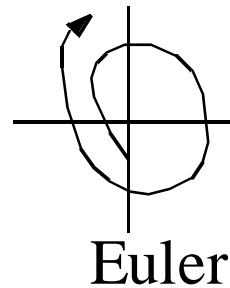
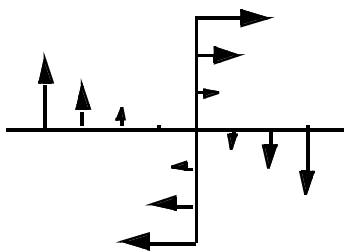
- **not good enough, need to resort to higherorder methods**

Numerical Integration

⊙ 2nd order Runge-Kutta

$$\bar{x}^*(s + \Delta s) = \bar{x}(s) + \bar{v}(\bar{x}(s))\Delta s$$

$$\bar{x}(s + \Delta s) = \bar{x}(s) + \frac{(\bar{v}(\bar{x}(s)) + \bar{v}(\bar{x}^*(s + \Delta s)))}{2} \Delta s$$



Numerical Integration

◎ 4th order Runge-Kutta

$$\bar{x}(s + \Delta s) = \bar{x}_0 + \frac{1}{6} (\bar{v}(\bar{x}_0) + 2\bar{v}(\bar{x}_1) + 2\bar{v}(\bar{x}_2) + \bar{v}(\bar{x}_3))$$

$$x_0 = \bar{x}(s)$$

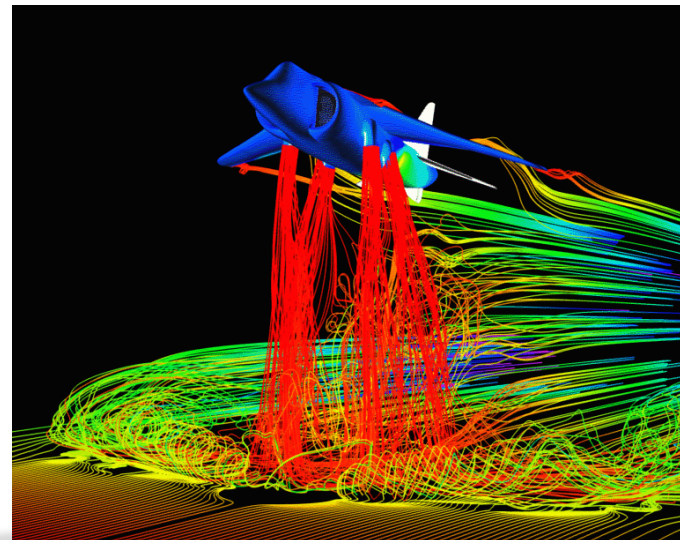
$$x_1 = \bar{x}(s) + \frac{1}{2} \bar{v}(\bar{x}_0) \Delta s$$

$$x_2 = \bar{x}(s) + \frac{1}{2} \bar{v}(\bar{x}_1) \Delta s$$

$$x_3 = \bar{x}(s) + \bar{v}(\bar{x}_2) \Delta s$$

Streamlines

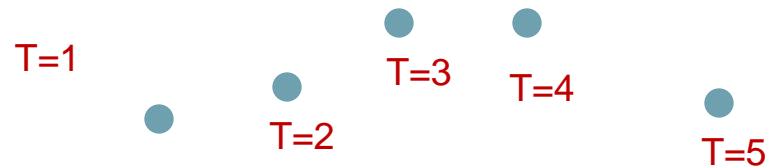
- Displaying streamlines is a local technique because you can only visualize the flow directions initiated from one or a few particles
- When the number of streamlines is increased, the scene becomes cluttered
- You need to know where to drop the particle seeds
- Streamline computation is expensive



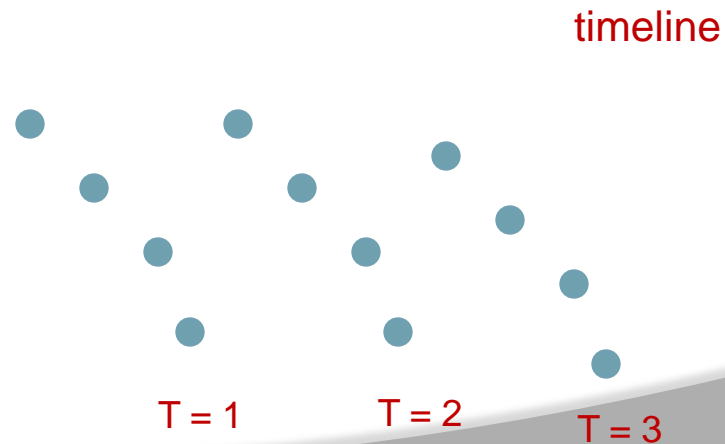
Pathlines, Timelines

-Extension of streamlines for time-varying data (unsteady flows)

Pathlines:

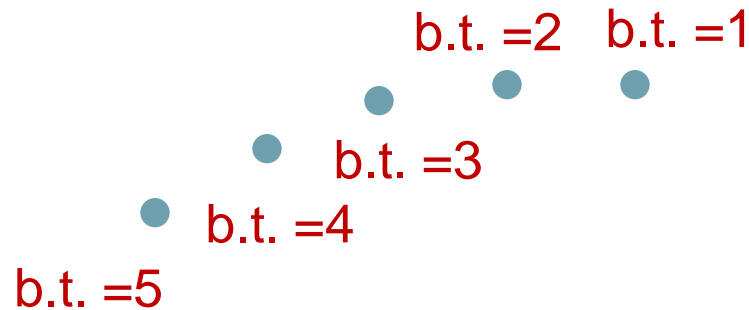


Timelines:

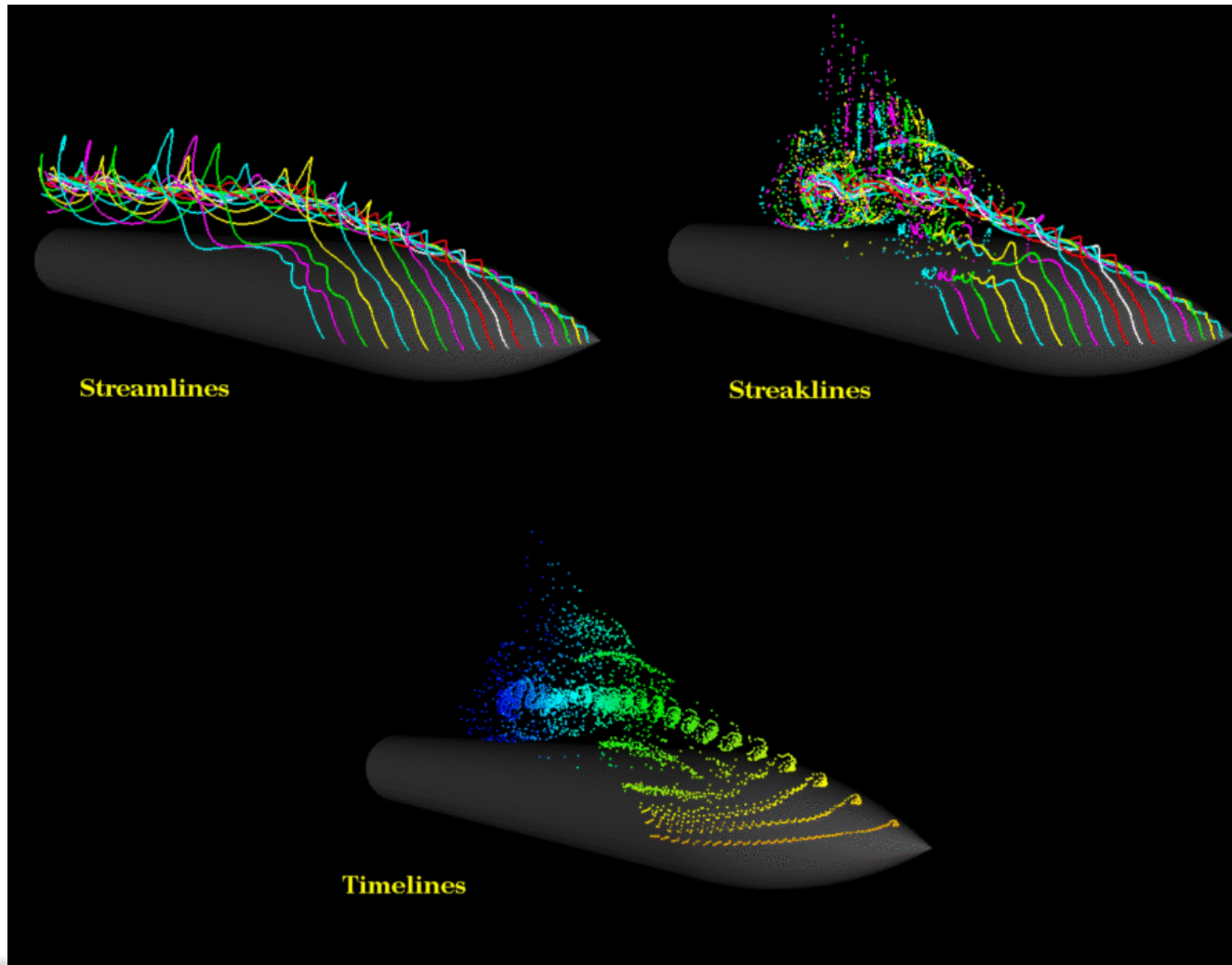


Streakline

- For unsteady flows also
- Continuously injecting a new particle at each time step, advecting all the existing particles and connect them together into a *streakline*



Advection methods comparison

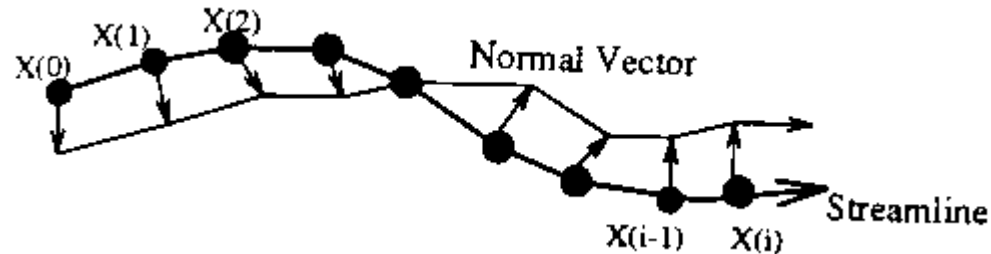


Stream-ribbon

- ⦿ **We really would like to see vorticities, I.e. places where the flow twists.**
- ⦿ **A point primitive or an icon can hardly convey this**
- ⦿ **idea: trace neighboring particles and connect them with polygons**
- ⦿ **shade those polygons appropriately and one will detect twists**

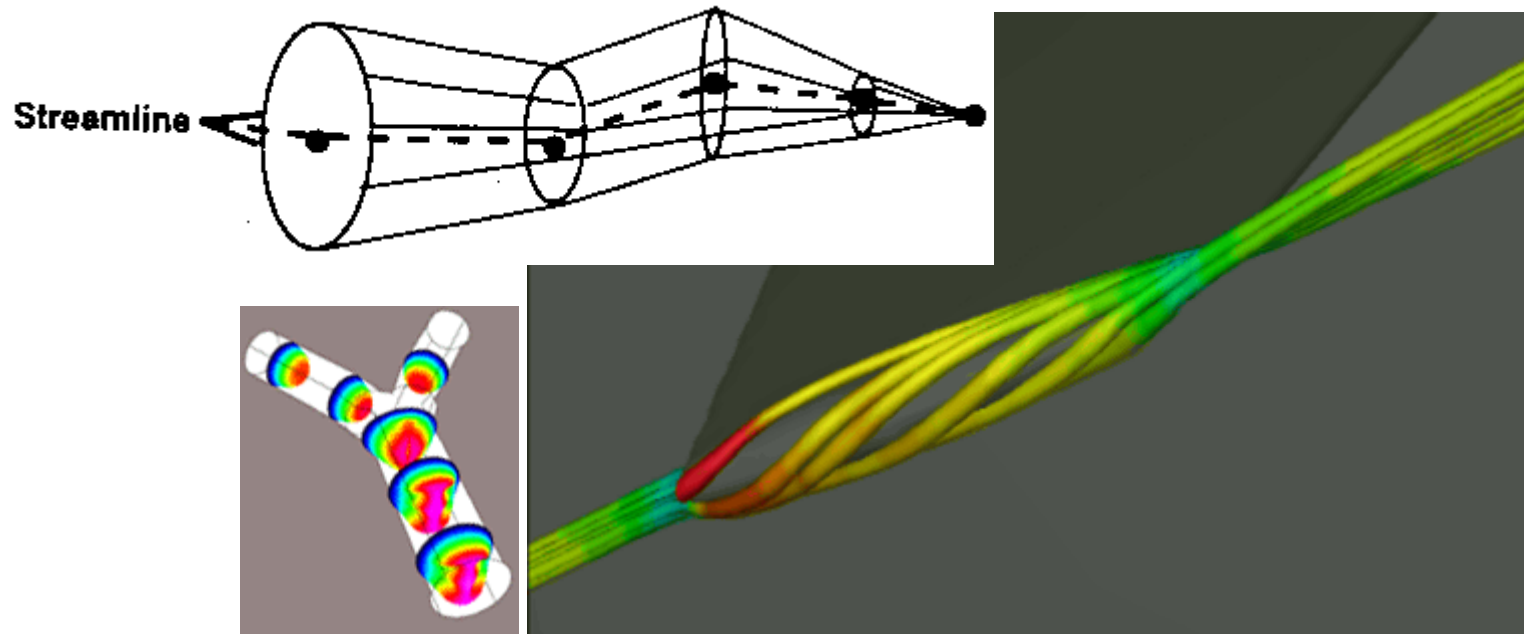
Stream-ribbon

- ⦿ **Problem - when flow diverges**
- ⦿ **Solution: Just trace one streamline and a constant size vector with it:**



Stream-tube

- Generate a stream-line and connect circular crossflow sections along the stream-line

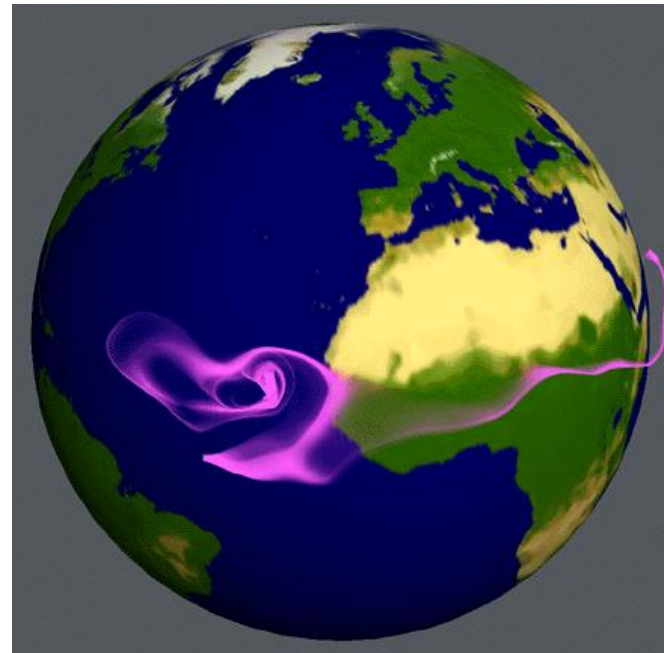
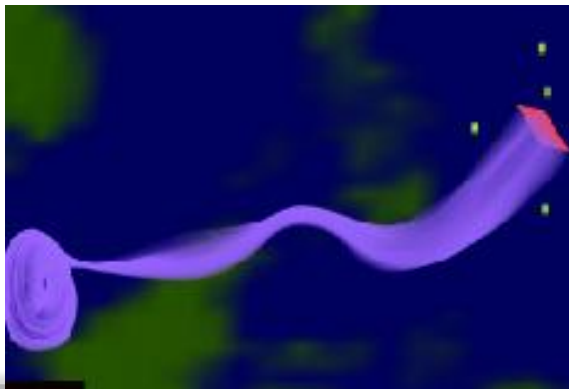
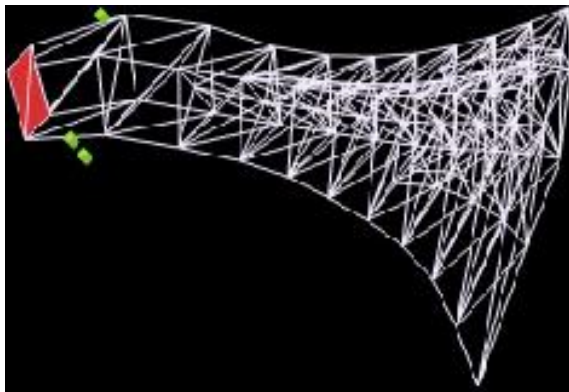


Stream-balls

- ◎ **Another way to get around diverging stream-lines**
- ◎ **simply put implicit surface primitives at particle traces - at places where they are close they'll merge elegantly ...**

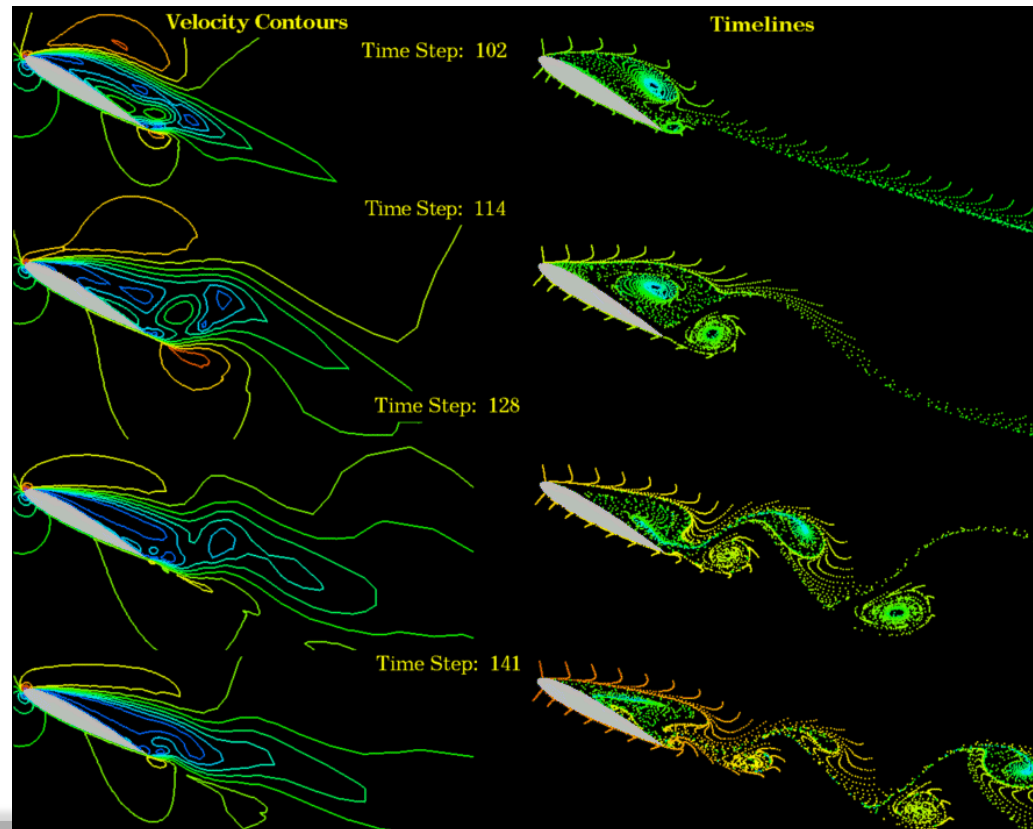
Flow Volumes

- ⦿ **Instead of tracing a line - trace a small polyhedra**



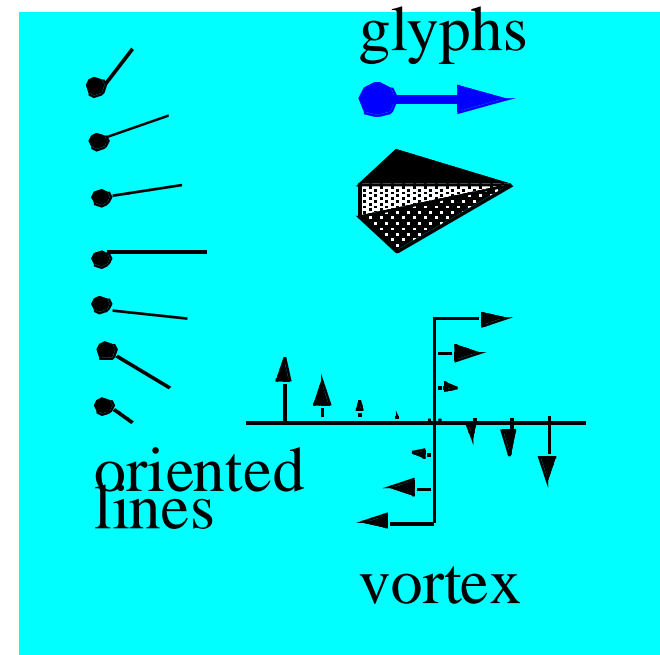
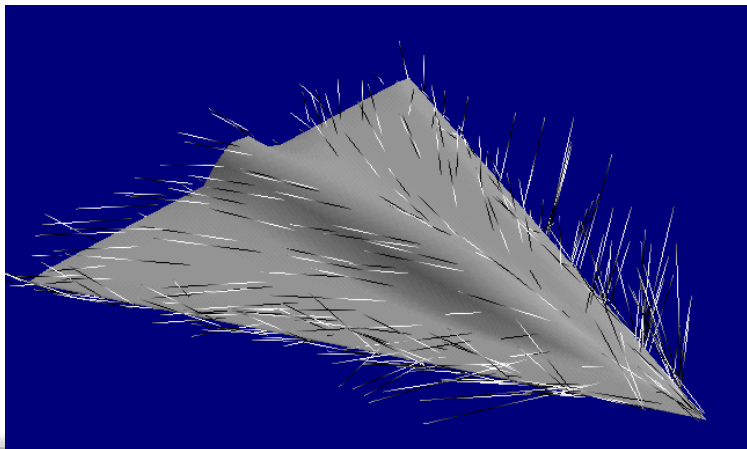
Contours

- Contour lines can measure certain quantities by connecting same values along a line



Mappings - Hedgehogs, Glyphs

- ◎ **Put “icons” at certain places in the flow**
 - e.g. arrows - represent direction & magnitude
- ◎ **other primitives are possible**

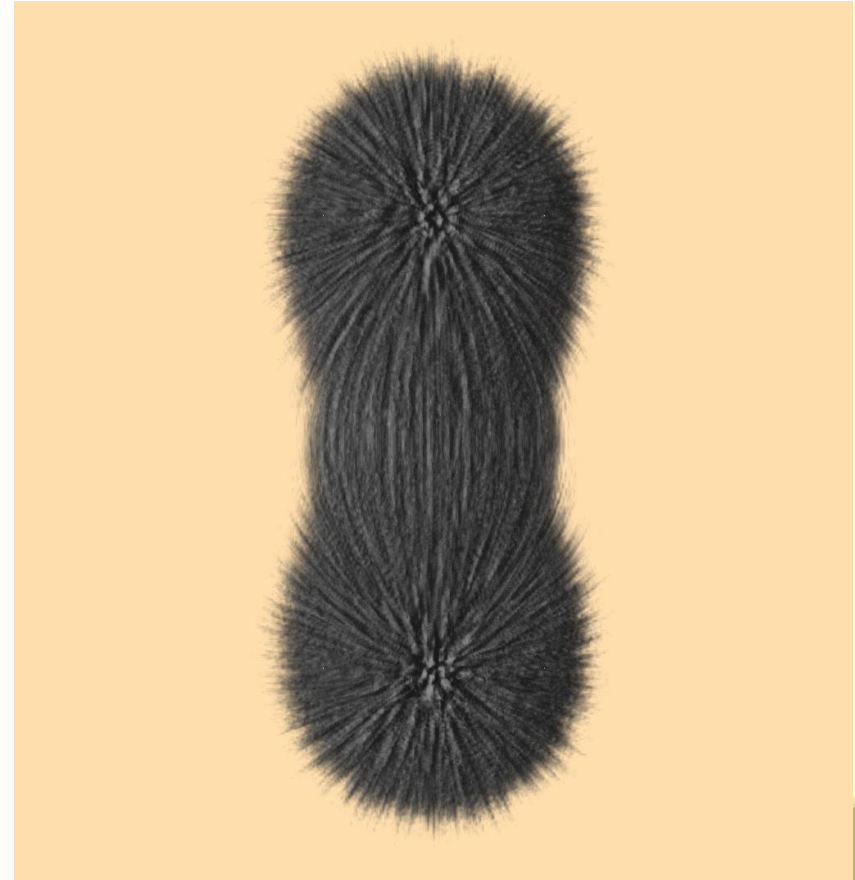


Mappings - Hedgehogs, Glyphs

- ⦿ **analogous to tufts or vanes from experimental flow visualization**
- ⦿ **clutter the image real quick**
- ⦿ **maybe ok for 2D**
- ⦿ **not very informative**

Global Methods

- ◎ **Spot Noise**
(van Wijk 91)
- ◎ **Line Integral Convolution**
(Cabral 93)
- ◎ **Texture Splats**
(Crawfis 93)

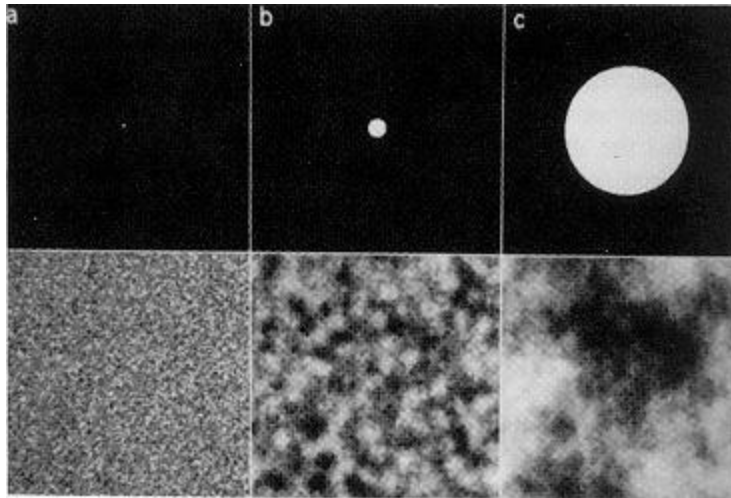


Spot Noise

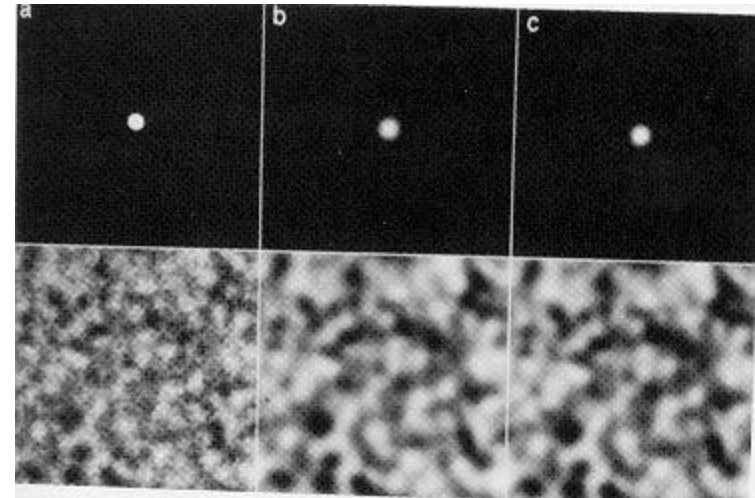
- ① **Uses small motion blurred particles to visualize flows on stream surfaces**
- ① **Particles represented as ellipses with their long axes oriented along the direction of the flow**
- ① **I.e. we multiply our kernel h with an amplitude and add a phase shift!**
- ① **Hence - we convolve a spot kernel in spatial domain with a random sequence (white noise)**

Rendering - Spot Noise

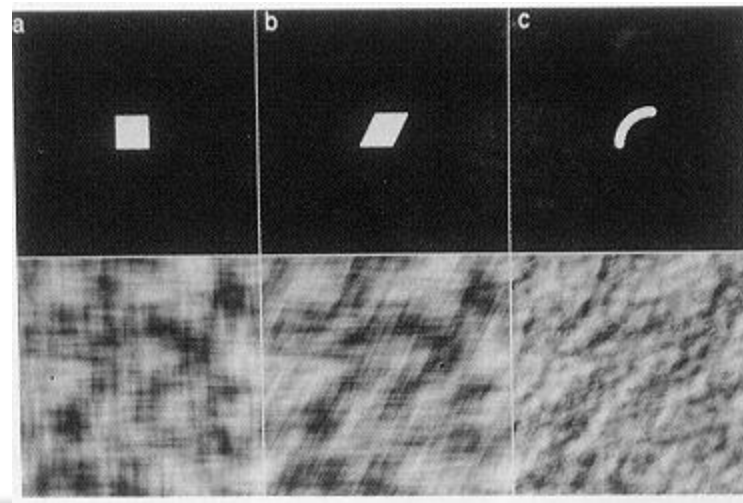
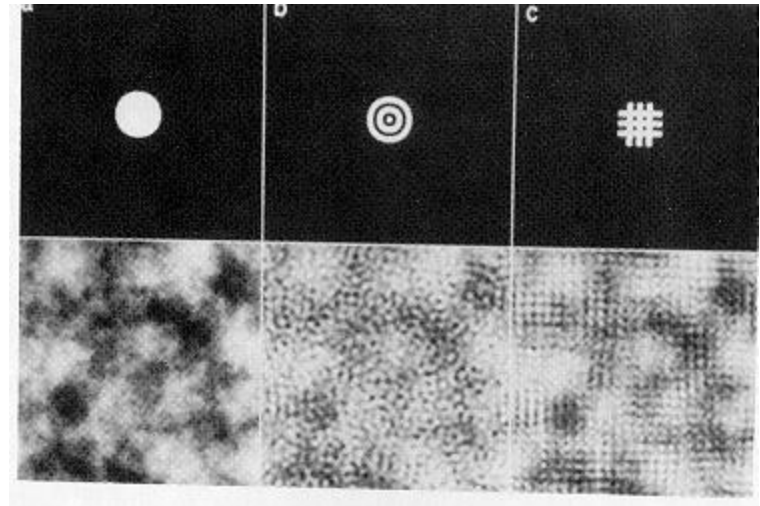
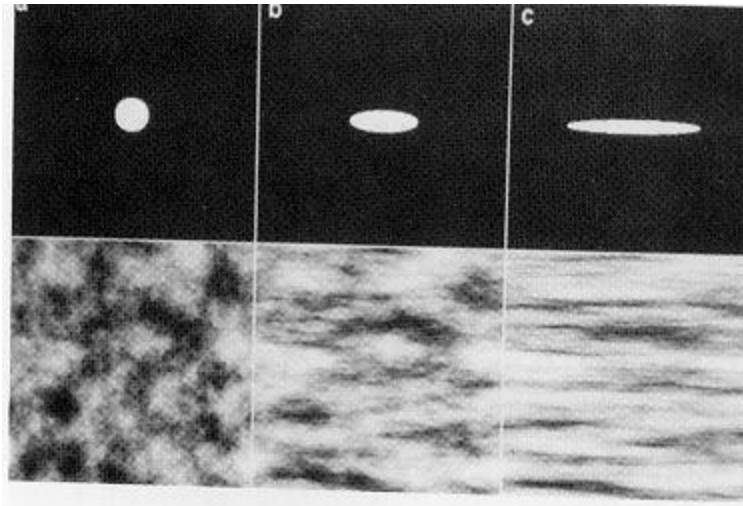
Different size



Different profiles

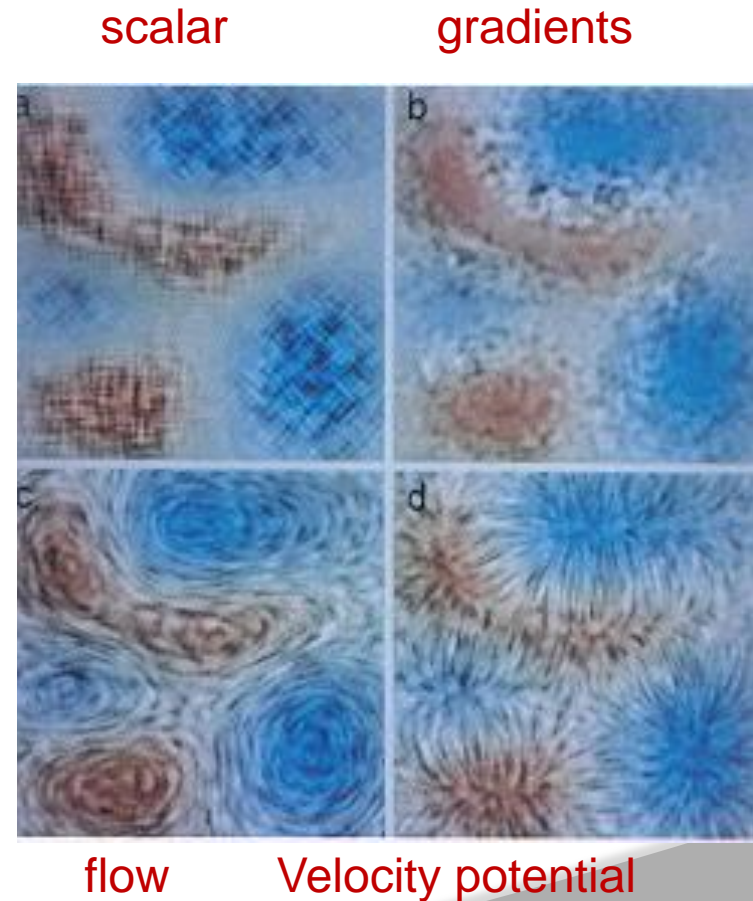


Rendering - Spot Noise



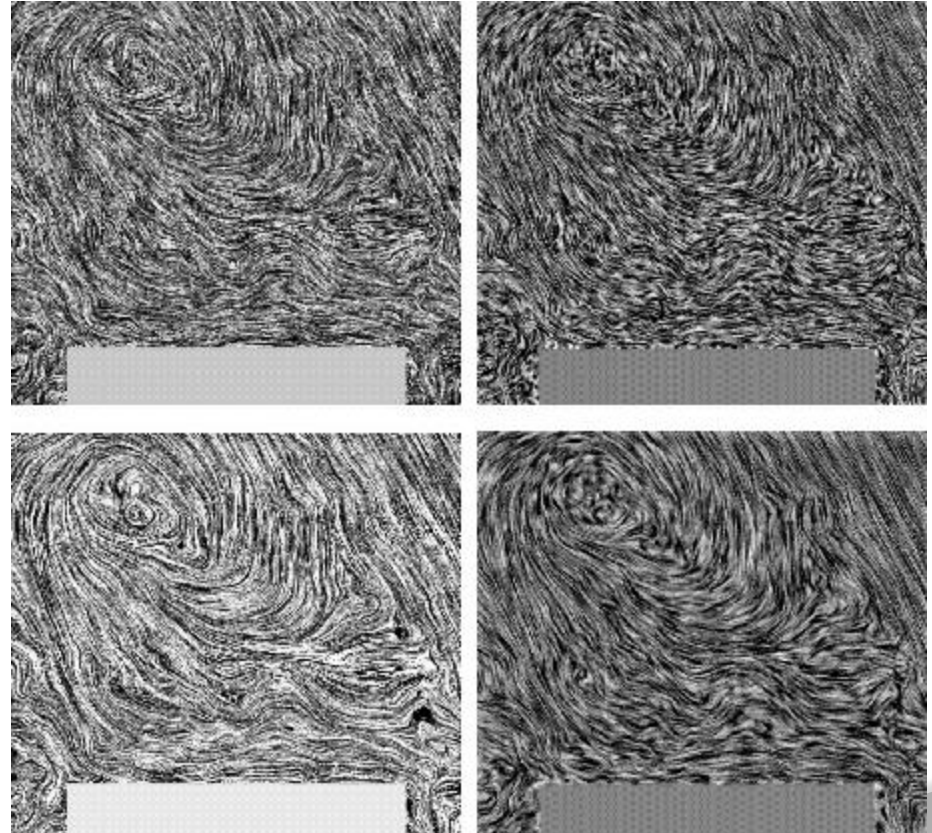
Rendering - Spot Noise

- ◎ **Scalar** - use +-shape for positive values, x-shape for negative values
- ◎ **change the size of the spot according to the norm of the gradient**
- ◎ **vector data** - use an ellipse shaped spot in the direction of the flow ...



Rendering - LIC

- **Similar to spot noise**
- **embed a noise texture under the vector field**
- **difference - integrates along a streamline**



LIC

Spot Noise

Texture Splats

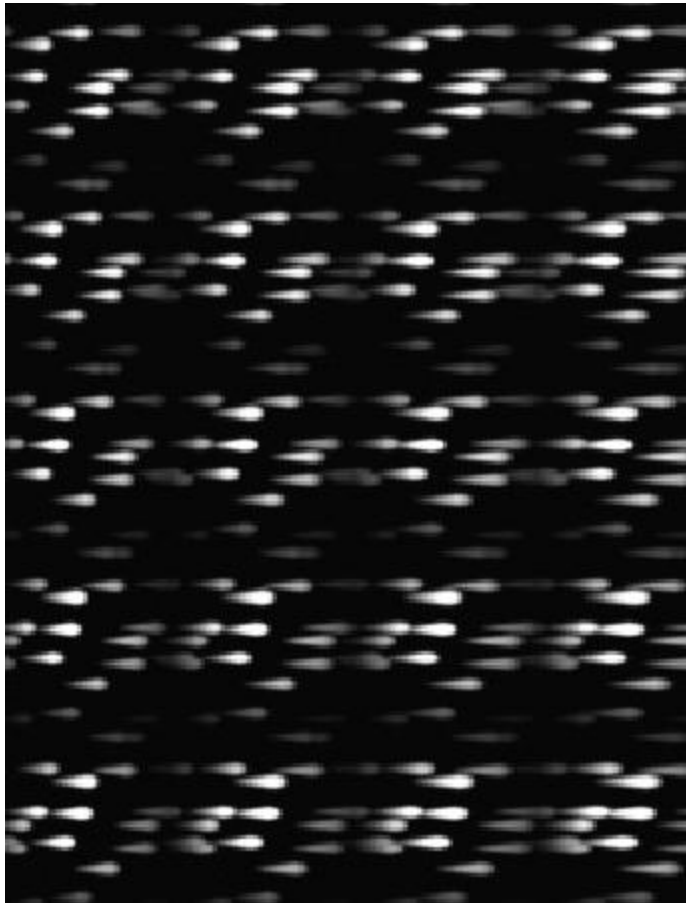
- ◎ **Crawfis, Max 1993**
- ◎ **extended splatting to visualize vector fields**
- ◎ **used simple idea of “textured vectors” for visualization of vector fields**

Texture Splats - Vector Viz

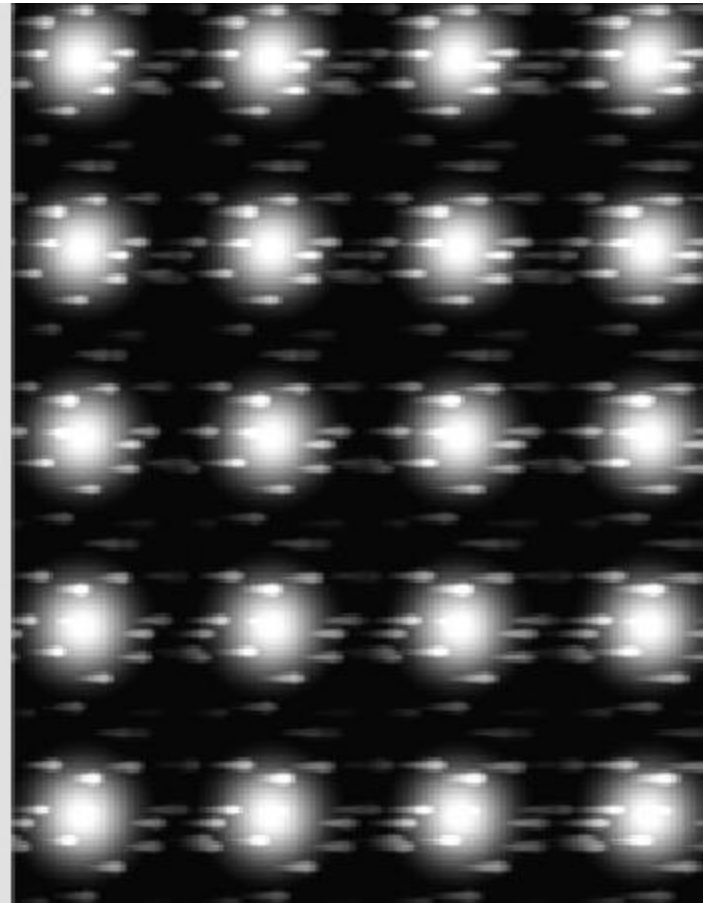
- ◎ **The splat would be a Gaussian type texture**
- ◎ **how about setting this to an arbitrary image?**
- ◎ **How about setting this to an image including some elongated particles representing the flow in the field?**
- ◎ **Texture must represent whether we are looking at the vector head on or sideways**

Texture Splats

Texture images



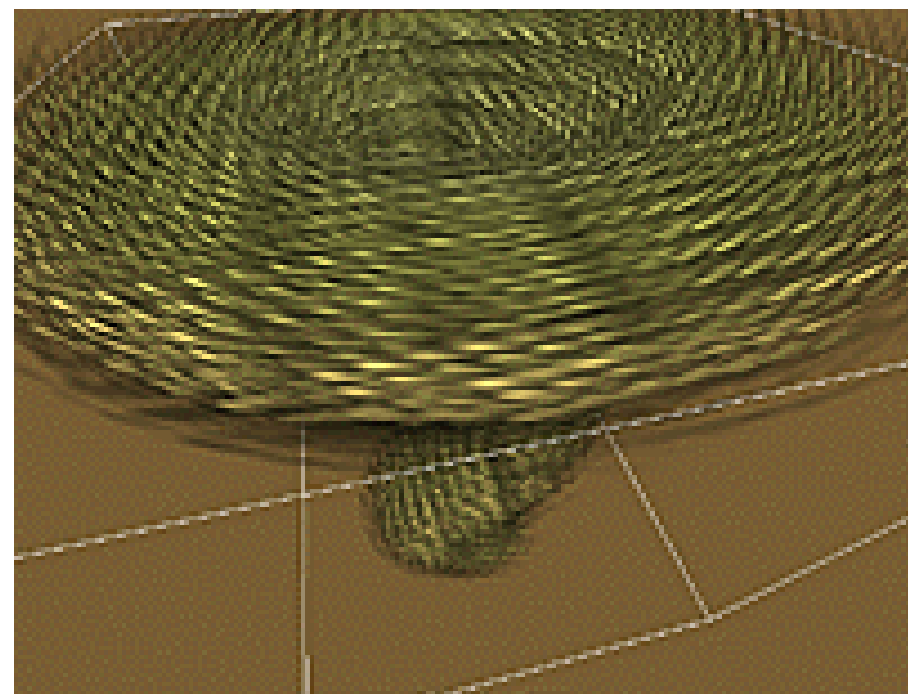
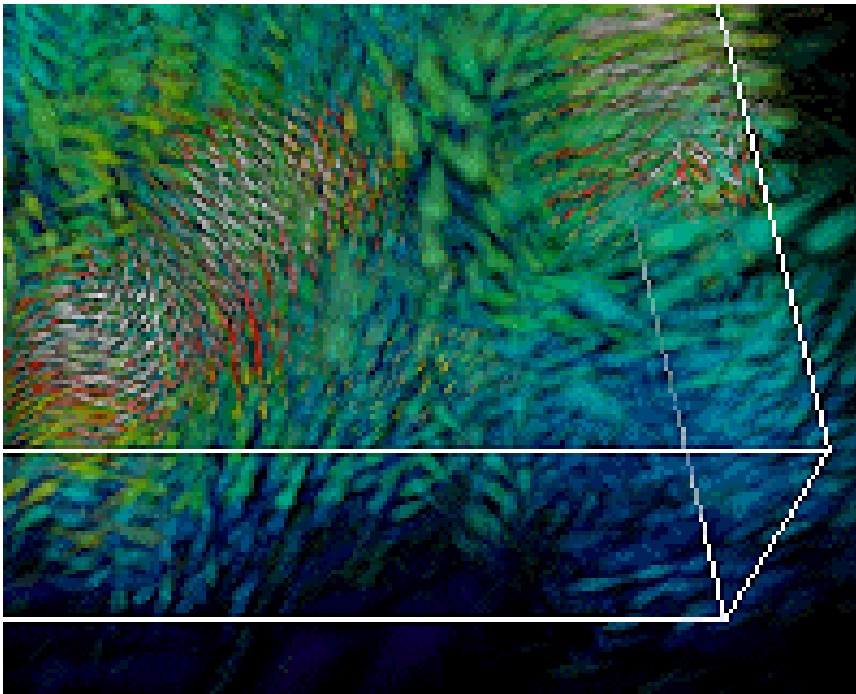
Appropriate opacities



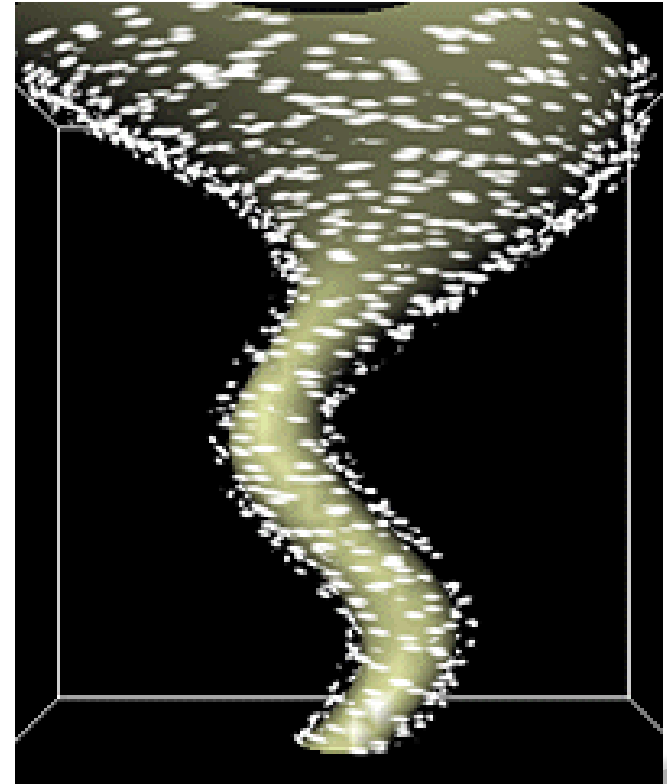
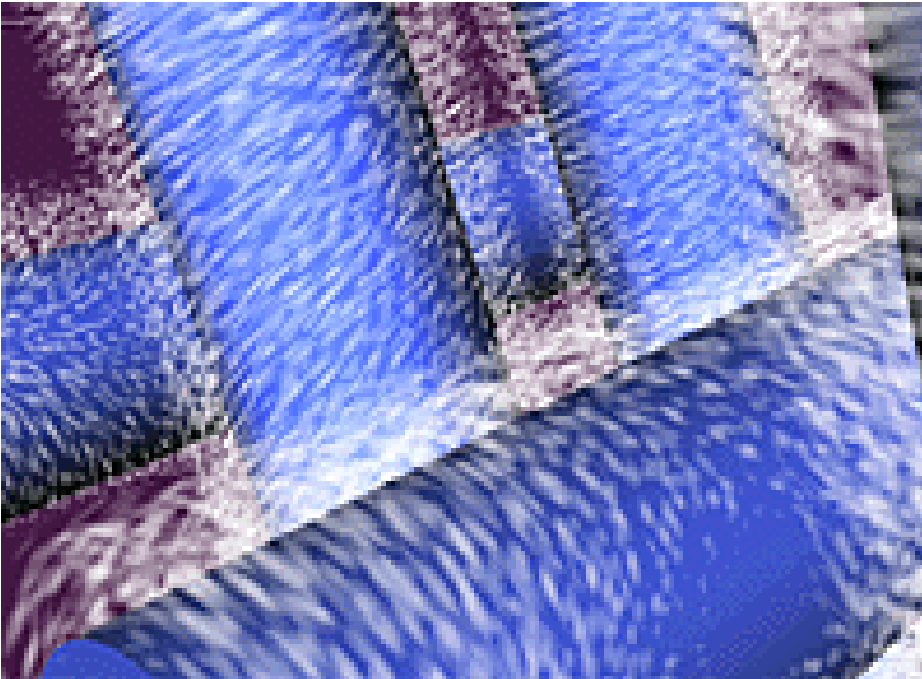
- ① **How do you get them to “move”?**
- ① **Just cycle over a periodic number of different textures (rows)**

More global techniques

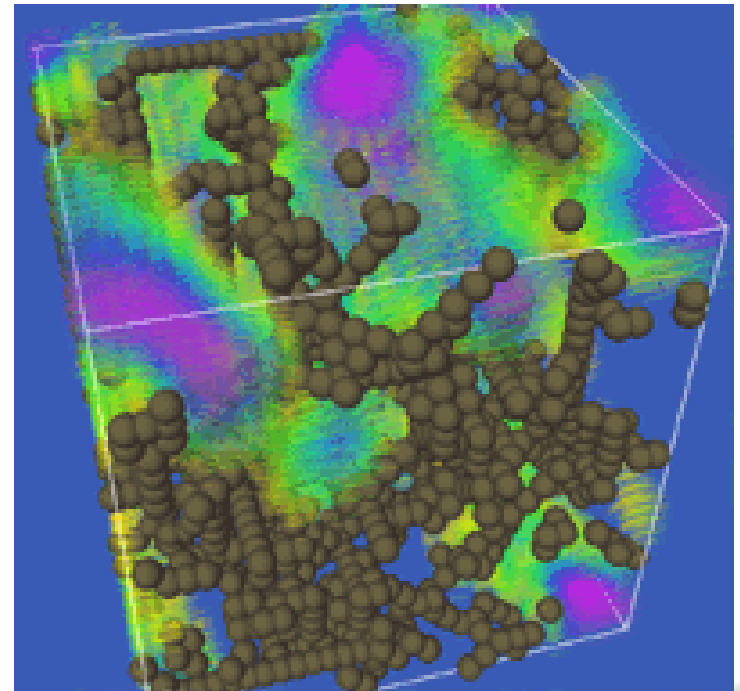
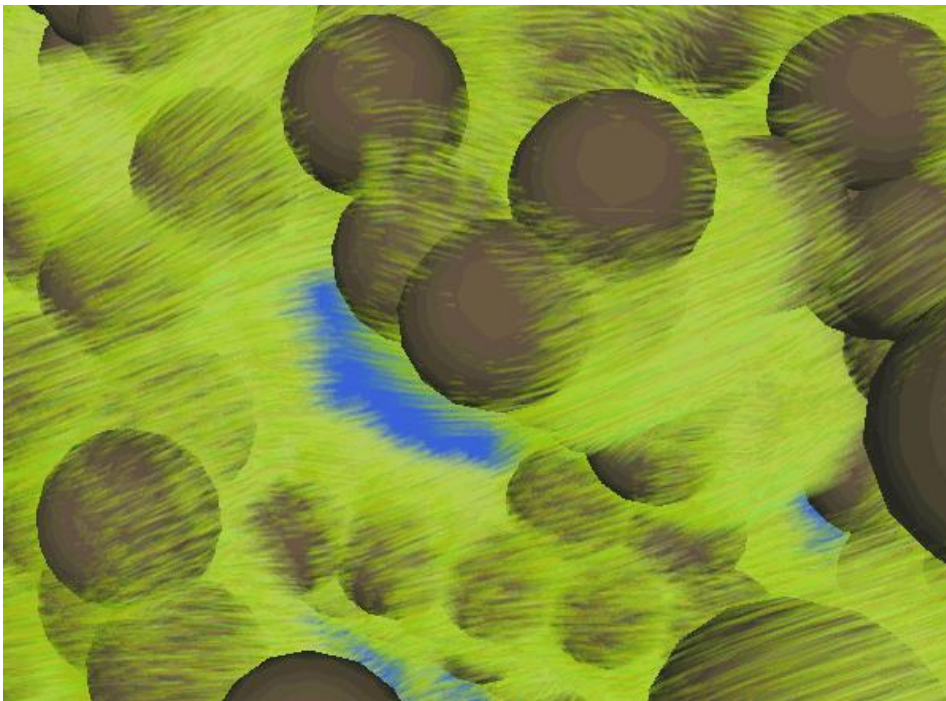
Texture Splats



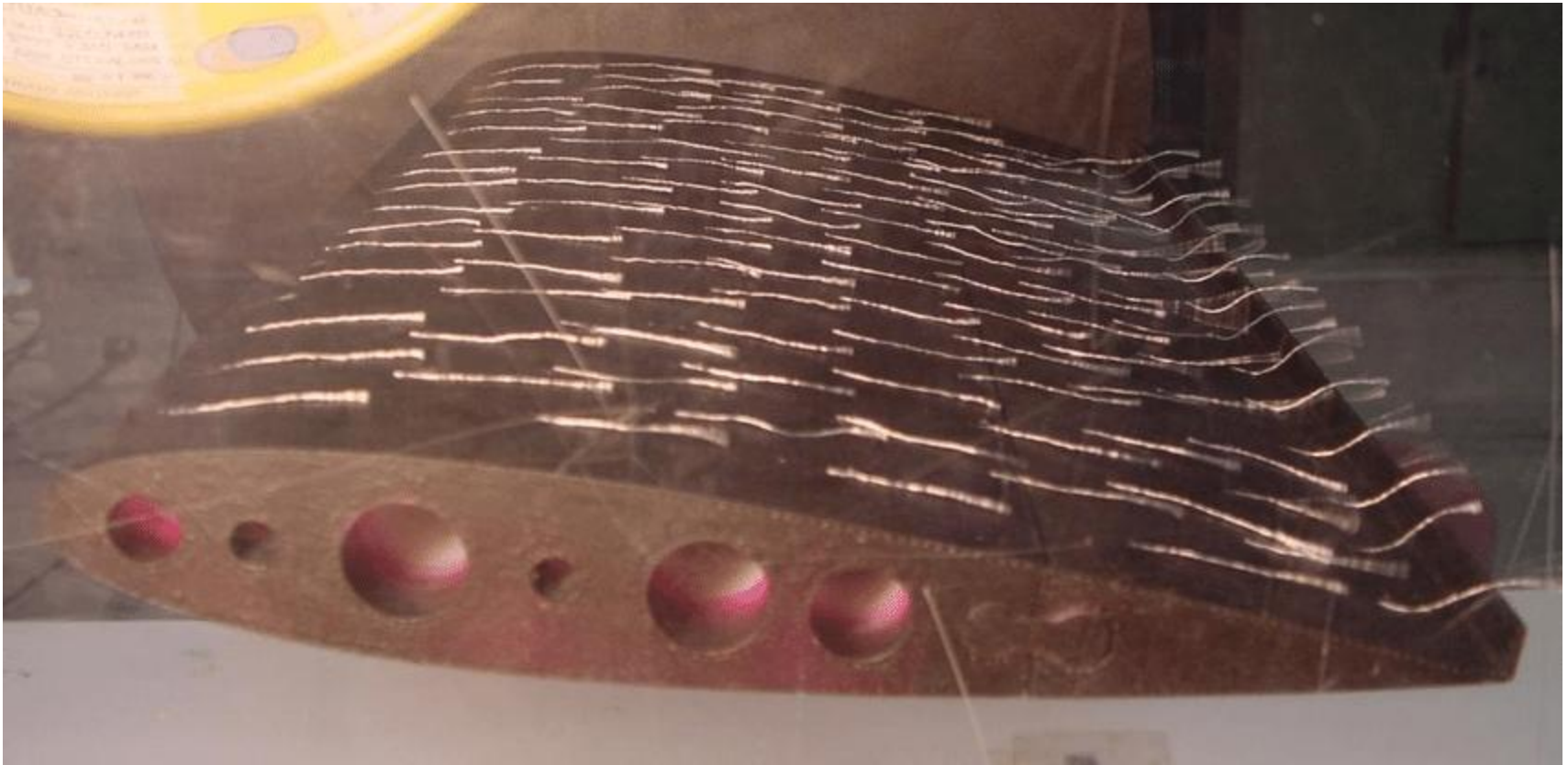
Spot Noise



Line bundles



Time Lines, Tufts

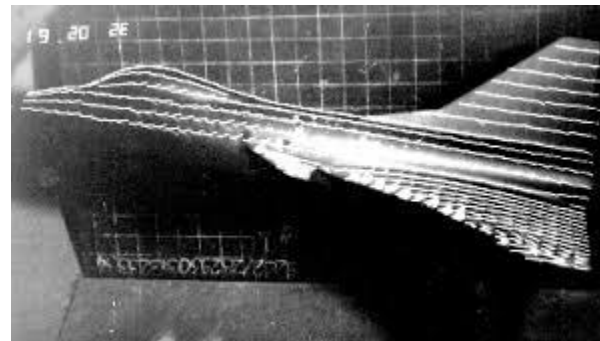
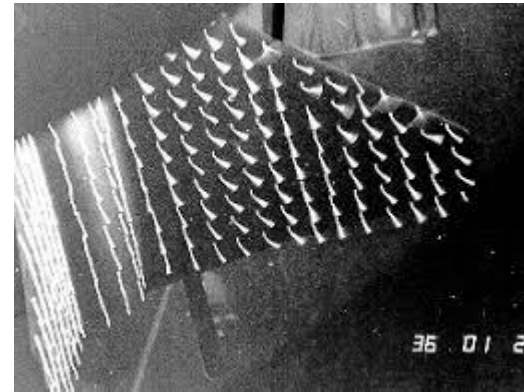
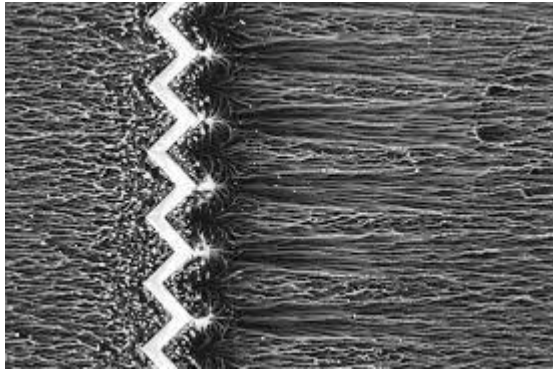


China Clay

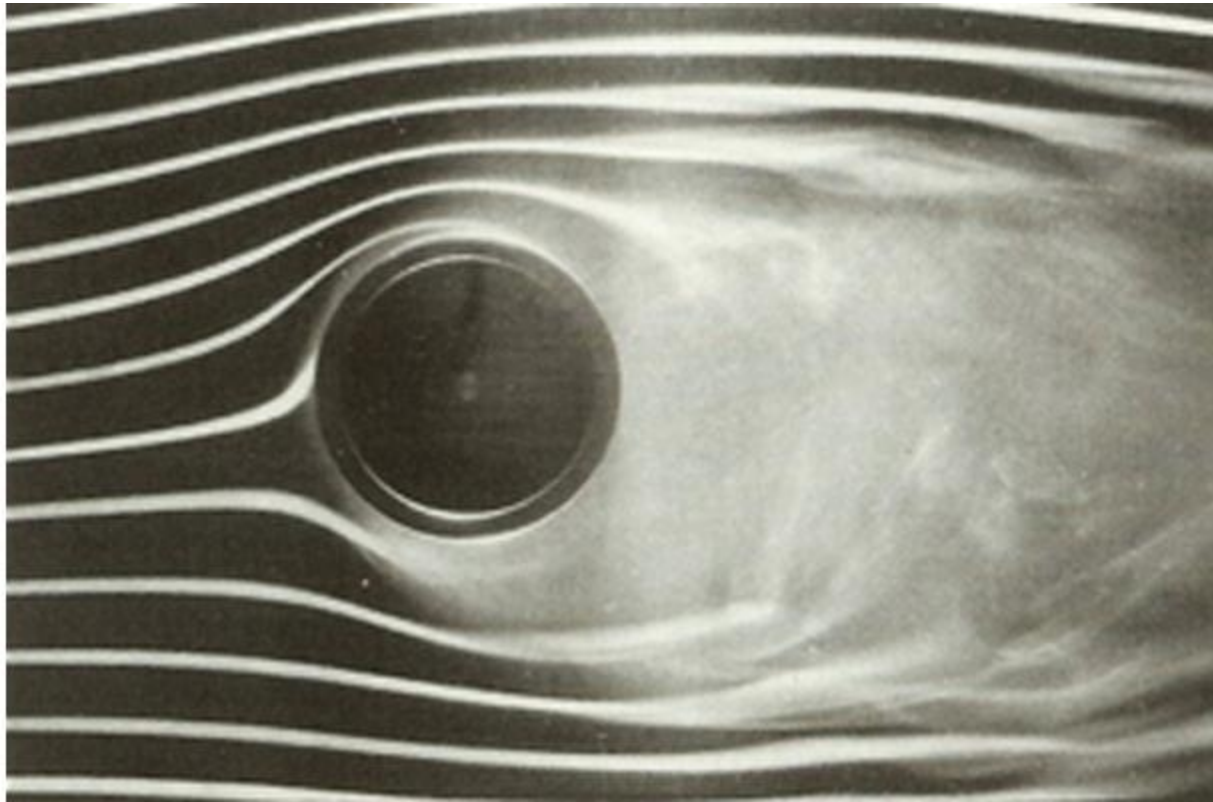


Unit-V

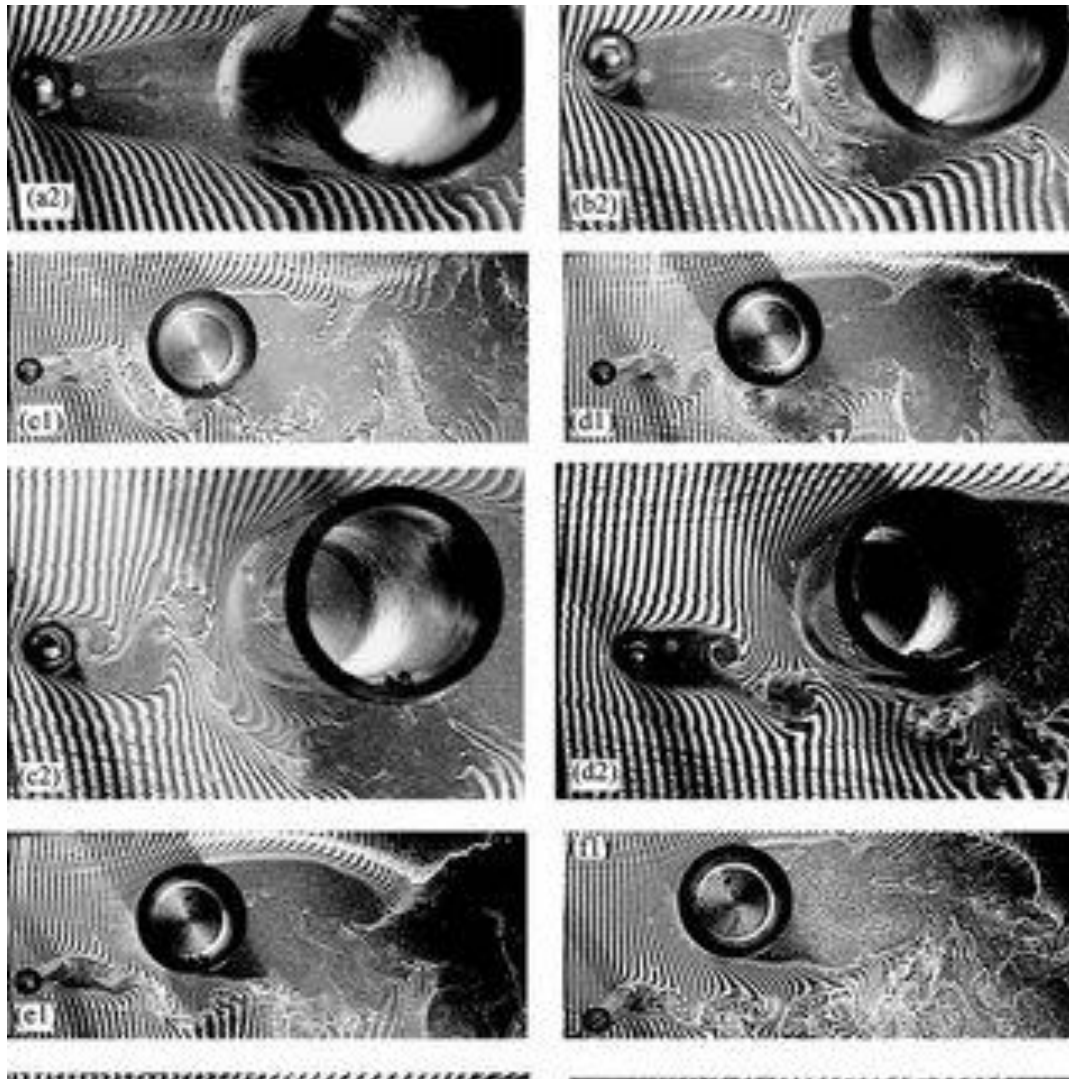
Oil Film



Smoke



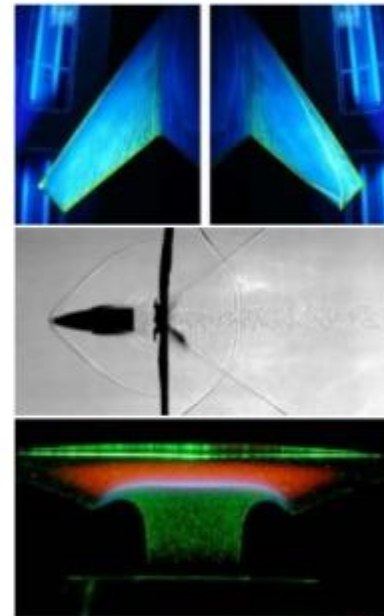
Hydrogen Bubble



Optical Methods:

Flow Visualization Techniques

- Surface Flow Visualization
- Optical Methods
 - Shadowgraph
 - Schlieren
 - Laser Induced Fluorescence
 - Particle Tracer Method
 - Laser Doppler Velocimetry
 - Particle Image Velocimetry

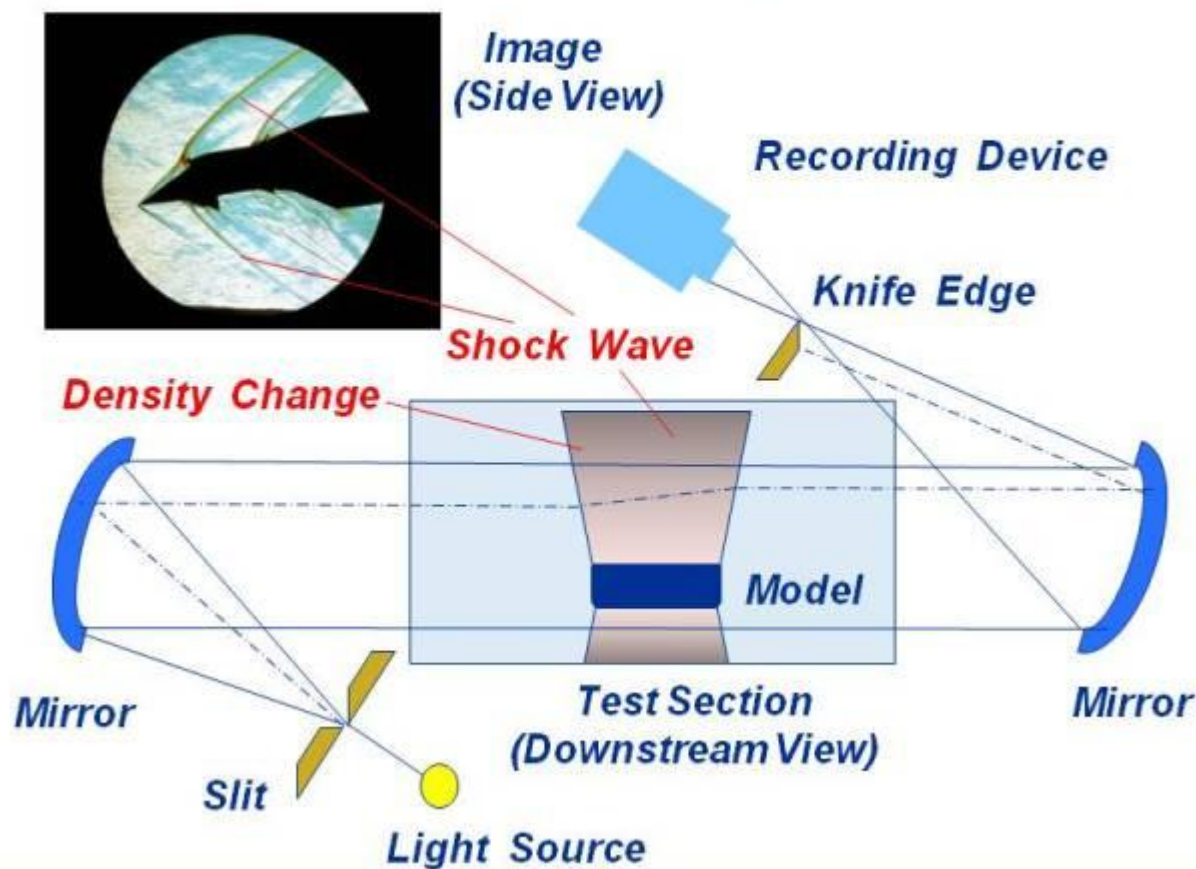


Density and Refractive Index

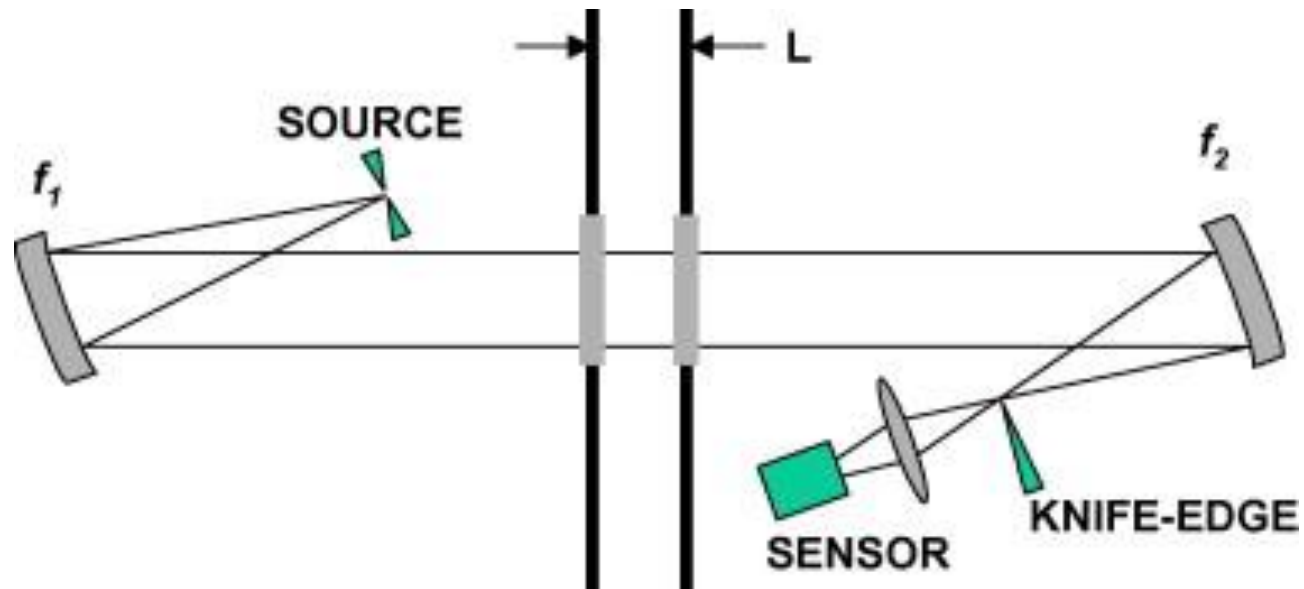
National Aeronautics and Space Administration



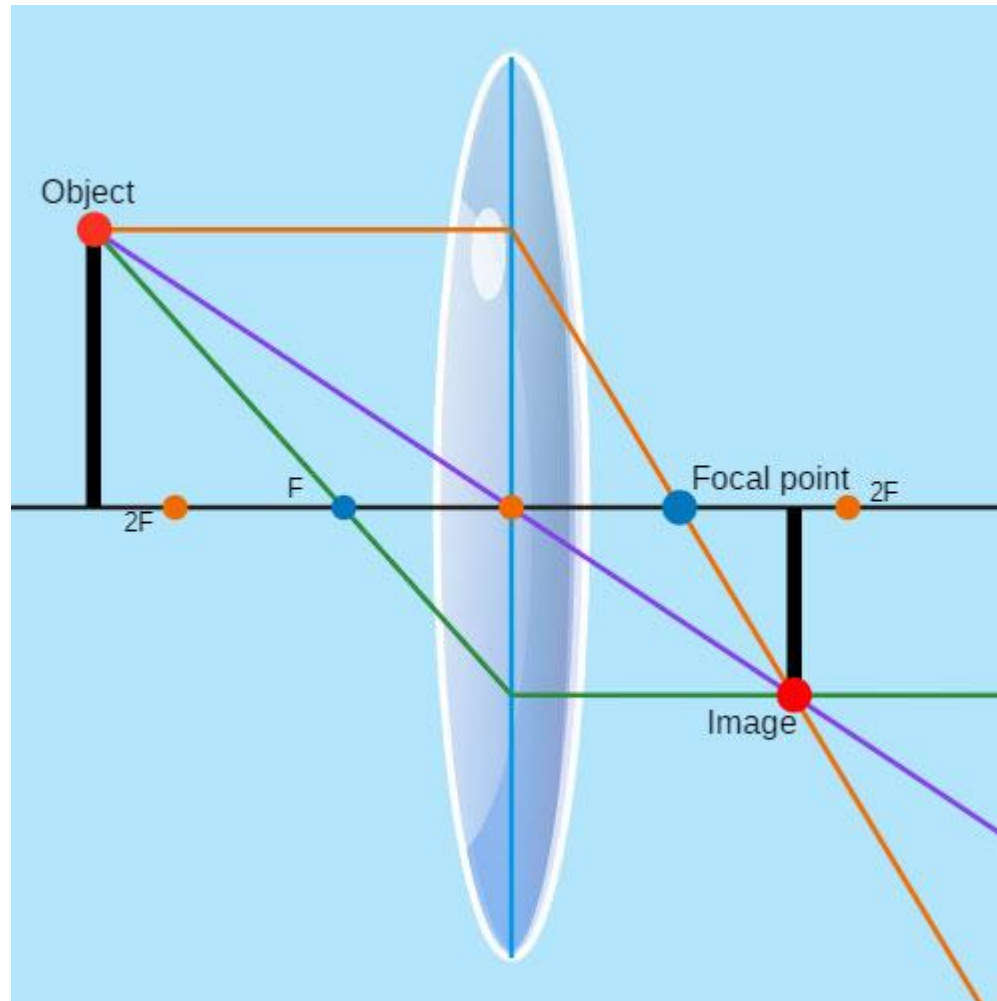
Schlieren System



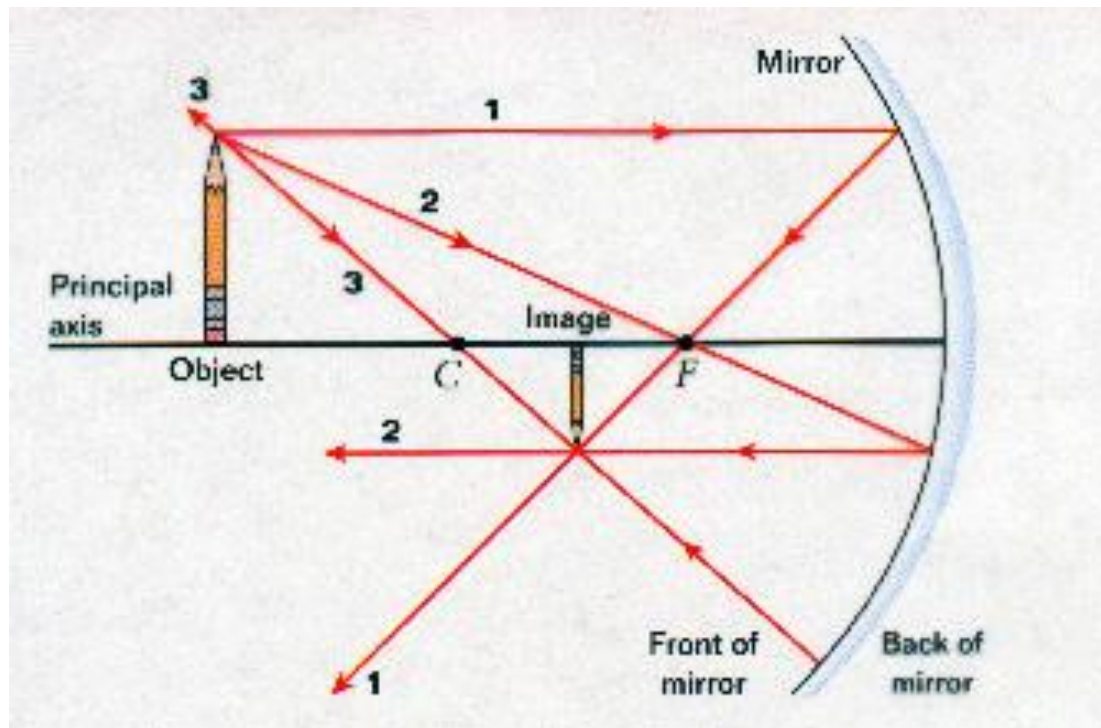
Schlieren System



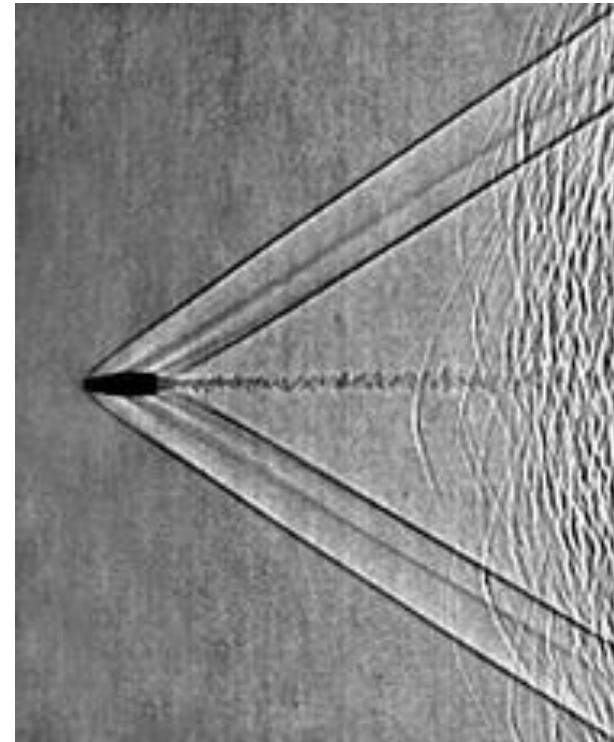
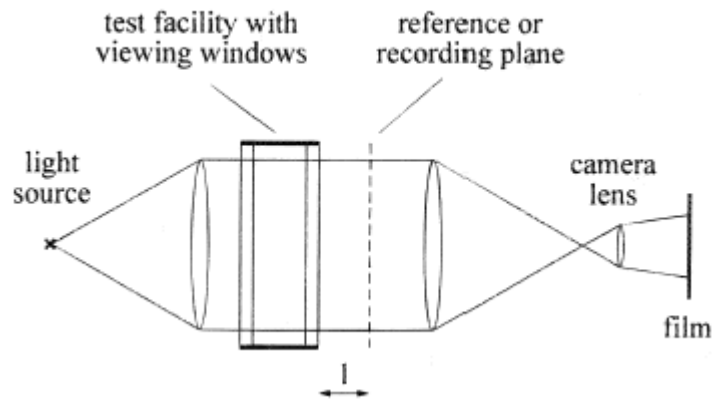
Convex Lenses



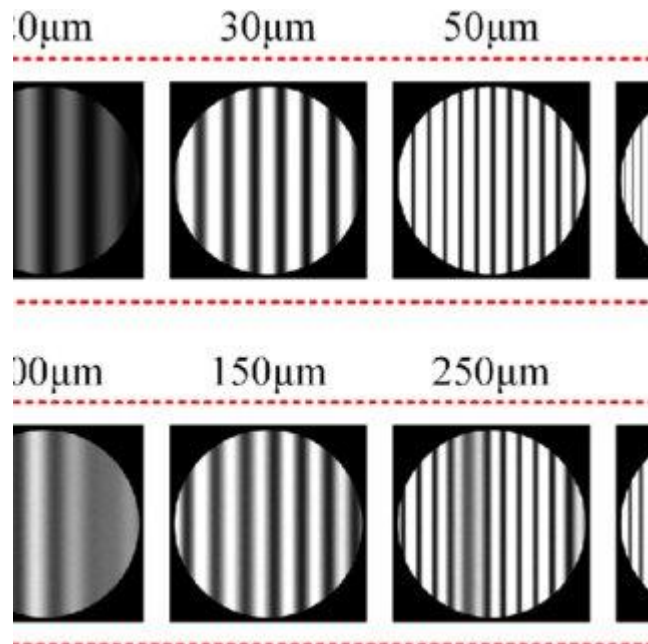
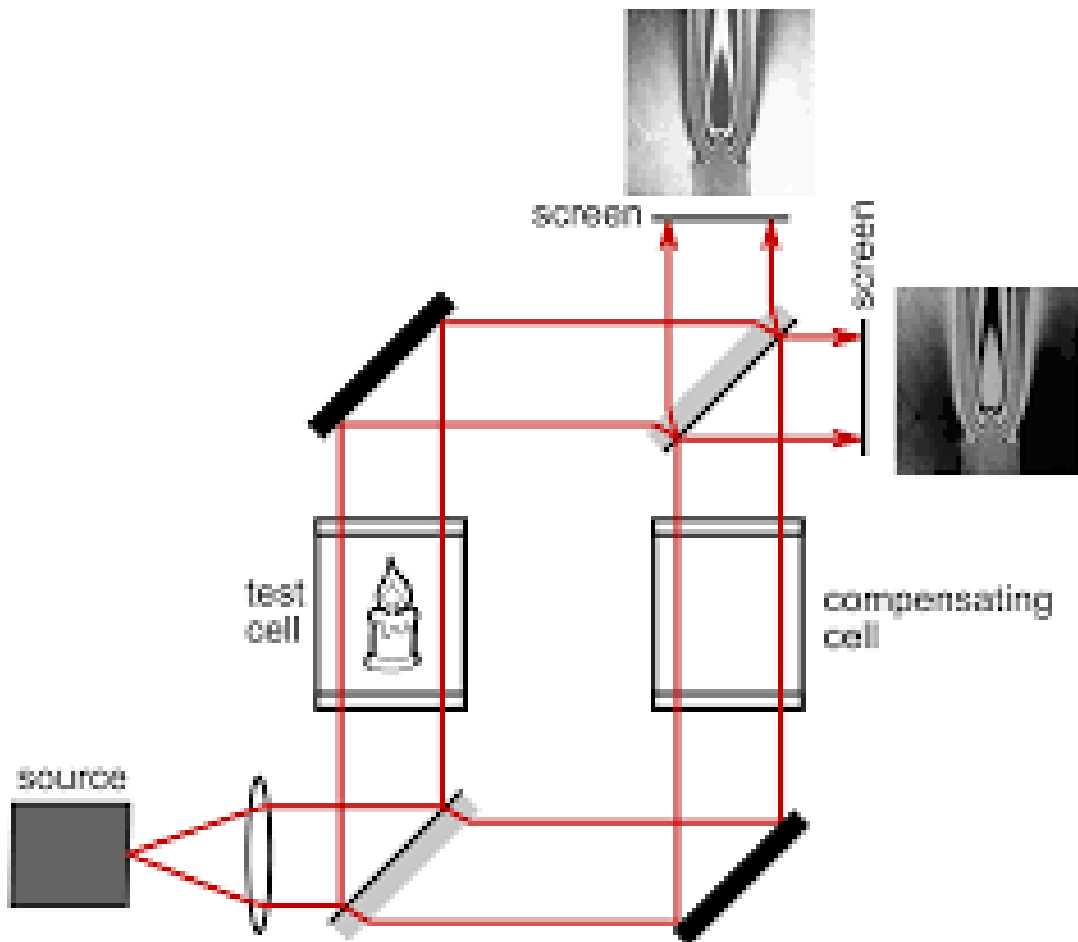
Concave Mirrors



Shadowgraph



Interferometry





Thank you