

INSTITUTE OF AERONAUTICAL ENGINEERING

(Autonomous)

Dundigal, Hyderabad -500 043

ELECTRONICS AND COMMUNICATION ENGINEERING

COURSE DESCRIPTOR

Course Title	LINEAR A	LINEAR ALGEBRA AND CALCULUS				
Course Code	AHSB02					
Programme	B. Tech					
Semester	I AE	CSE IT ECE	EEE ME C	Е		
Course Type	Foundation					
Regulation	IARE - R18	}				
	Theory Practical					
Course Structure	Lectures	Tutorials	Credits	Laboratory	Credits	
	3	1	4	-	-	
Chief Coordinator	Ms. P Raja	ni, Assistant Pro	fessor			
Course Faculty	Ms. P Rajani, Assistant Professor Dr. M Anita, Professor Dr. S Jagadha, Professor Dr. J Suresh Goud, Assistant Professor Ms. L Indira, Assistant Professor Mr. Ch Somashekar, Assistant Professor Ms. P Srilatha, Assistant Professor Ms. C Rachana, Assistant Professor Ms. V Subba Laxmi, Assistant Professor Ms. B Praveena, Assistant Professor					

I. COURSE OVERVIEW:

The course focuses on more advanced Engineering Mathematics topics which provide with the relevant mathematical tools required in the analysis of problems in engineering and scientific professions. The course includes types of Matrices and its applications, maxima and minima of functions of several variables, solutions of higher order ordinary differential equations, multiple integrals and vector calculus. The mathematical skills derived from this course form a necessary base to analytical and design concepts encountered in the program.

II. COURSE PRE-REQUISITES:

Level	Course Code	Semester	Prerequisites
-	-	ı	Basic Principles of Algebra and Calculus

III. MARKS DISTRIBUTION:

Subject	SEE Examination	CIA Examination	Total Marks
Linear Algebra and Calculus	70 Marks	30 Marks	100

IV. DELIVERY / INSTRUCTIONAL METHODOLOGIES:

•	Chalk & Talk	>	Quiz	>	Assignments	×	MOOCs
~	LCD / PPT	/	Seminars	×	Mini Project	>	Videos
x	X Open Ended Experiments						

V. EVALUATION METHODOLOGY:

The course will be evaluated for a total of 100 marks, with 30 marks for Continuous Internal Assessment (CIA) and 70 marks for Semester End Examination (SEE). Out of 30 marks allotted for CIA during the semester, marks are awarded by taking average of two CIA examinations or the marks scored in the make-up examination.

Semester End Examination (SEE): The SEE is conducted for 70 marks of 3 hours duration. The syllabus for the theory courses is divided into five modules and each module carries equal weightage in terms of marks distribution. The question paper pattern is as follows. Two full questions with "either" or "choice" will be drawn from each module. Each question carries 14 marks. There could be a maximum of two sub divisions in a question.

The emphasis on the questions is broadly based on the following criteria:

50 %	To test the objectiveness of the concept.
50 %	To test the analytical skill of the concept OR to test the application skill of the concept.

Continuous Internal Assessment (CIA):

CIA is conducted for a total of 30 marks (Table 1), with 20 marks for Continuous Internal Examination (CIE), 05 marks for Quiz and 05 marks for Alternative Assessment Tool (AAT).

Table 1: Assessment pattern for CIA

Component		Total Marks		
Type of Assessment	CIE Exam	Quiz	AAT	Total Walks
CIA Marks	20	05	05	30

Continuous Internal Examination (CIE):

Two CIE exams shall be conducted at the end of the 8th and 16th week of the semester respectively. The CIE exam is conducted for 20 marks of 2 hours duration consisting of five descriptive type questions out of which four questions have to be answered where, each question carries 5 marks. Marks are awarded by taking average of marks scored in two CIE exams.

Ouiz - Online Examination

Two Quiz exams shall be online examination consisting of 25 multiple choice questions and are to be answered by choosing the correct answer from a given set of choices (commonly four). Such a question paper shall be useful in testing of knowledge, skills, application, analysis, evaluation and understanding of the students. Marks shall be awarded considering the average of two quiz examinations for every course.

Alternative Assessment Tool (AAT)

This AAT enables faculty to design own assessment patterns during the CIA. The AAT converts the classroom into an effective learning centre. The AAT may include tutorial hours/classes, seminars, assignments, term paper, open ended experiments, METE (Modeling and Experimental Tools in Engineering), five minutes video, MOOCs etc.

VI. HOW PROGRAM OUTCOMES ARE ASSESSED:

	Program Outcomes (POs)	Strength	Proficiency assessed
			by
PO 1	Engineering knowledge : Apply the knowledge of	3	Presentation on
	mathematics, science, engineering fundamentals, and		real-world problems
	an engineering specialization to the solution of		
	complex engineering problems.		
PO 2	Problem analysis: Identify, formulate, review research	2	Seminar
	literature, and analyze complex engineering problems		
	reaching substantiated conclusions using first		
	principles of mathematics, natural sciences, and		
	engineering sciences		
PO 4	Conduct investigations of complex problems: Use	1	Term Paper
	research-based knowledge and research methods		
	including design of experiments, analysis and		
	interpretation of data, and synthesis of the information		
	to provide valid conclusions.		

3 = High; 2 = Medium; 1 = Low

VII. HOW PROGRAM SPECIFIC OUTCOMES ARE ASSESSED:

	Program Specific Outcomes (PSOs)	Strength	Proficiency assessed by
PSO 1	Professional Skills: An ability to understand the basic	1	Seminar
	concepts in Electronics & Communication Engineering		
	and to apply them to various areas, like Electronics,		
	Communications, Signal processing, VLSI, Embedded		
	systems etc., in the design and implementation of		
	complex systems.		
PSO 2	Problem-Solving Skills: An ability to solve complex	-	-
	Electronics and communication Engineering problems,		
	using latest hardware and software tools, along with		
	analytical skills to arrive cost effective and appropriate		
	solutions.		
PSO 3	Successful Career and Entrepreneurship: An	-	-
	understanding of social-awareness & environmental-		
	wisdom along with ethical responsibility to have a		
	successful career and to sustain passion and zeal for		
	real-world applications using optimal resources as an		
	Entrepreneur.		

^{3 =} High; 2 = Medium; 1 = Low

VIII. COURSE OBJECTIVES (COs):

The cou	The course should enable the students to:				
I	Determine rank of a matrix and solve linear differential equations of second order.				
II	Determine the characteristic roots and apply double integrals to evaluate area.				
III	Apply mean value theorems and apply triple integrals to evaluate volume.				
IV	Determine the functional dependence and extremum value of a function.				
V	Analyze gradient, divergence, curl and evaluate line, surface, volume integrals over a vector field.				

IX. COURSE OUTCOMES (COs):

COs	Course Outcome	CLOs	Course Learning Outcome
CO 1	Determine rank by reducing the matrix to Echelon and Normal forms. Determine inverse of the matrix by Gauss Jordon Method and Solving Second and higher order differential equations with constant coefficients.	CLO 2 CLO 3 CLO 4	Demonstrate knowledge of matrix calculation as an elegant and powerful mathematical language in connection with rank of a matrix. Determine rank by reducing the matrix to Echelon and Normal forms. Determine inverse of the matrix by Gauss Jordon Method. Find the complete solution of a non-homogeneous differential equation as a linear combination of the complementary function and a particular solution. Solving Second and higher order differential
CO 2	Determine a modal matrix, and	CLO 6	equations with constant coefficients. Interpret the Eigen values and Eigen vectors
	reducing a matrix to diagonal form. Evaluate inverse and powers of	CLO	of matrix for a linear transformation and use properties of Eigen values
	matrices by using Cayley- Hamiltontheorem. Evaluate double	CLO 7	Understand the concept of Eigen values in real-world problems of control field where

COs	Course Outcome	CLOs	Course Learning Outcome
	integral. Utilize the concept of		they are pole of closed loop system.
	change order of integration and	CLO 8	Apply the concept of Eigen values in real-
	change of variables to evaluate		world problems of mechanical systems
	double integrals. Determine the		where Eigen values are natural frequency and
	area.		mode shape.
		CLO 9	Use the system of linear equations and
			matrix to determine the dependency and
		CI O 10	independency.
		CLO 10	Determine a modal matrix, and reducing a
		CLO 11	matrix to diagonal form. Evaluate inverse and powers of matrices by
		CLOTI	using Cayley-Hamiltontheorem.
		CLO 12	Apply double integrals to evaluate area of a
		CLO 12	given function.
		CLO 13	Utilize the concept of change order of
		020 10	integration and change of variables to
			evaluate double integrals.
CO 3	Apply the Mean value theorems	CLO 14	Apply the Mean value theorems for the
	for the single variable functions.		single variable functions.
	Apply triple integrals to evaluate	CLO 15	Apply triple integrals to evaluate volume of a
	volume.		given function.
CO 4	Determine the maxima and minima	CLO 16	Find partial derivatives numerically and
	for a function of several variable		symbolically and use them to analyze and
	with and without constraints.		interpret the way a function varies.
		CLO 17	Understand the techniques of
			multidimensional change of variables to
			transform the coordinates by utilizing the Jacobian. Determine Jacobian for the
			coordinate transformation.
		CLO 18	Apply maxima and minima for functions of
		CLO 10	several variable's and Lagrange's method of
			multipliers.
CO 5	Analyze scalar and vector fields	CLO 19	Analyze scalar and vector fields and compute
	and compute the gradient,		the gradient, divergence and curl.
	divergence and curl. Evaluate line,	CLO 20	Understand integration of vector function
	surface and volume integral of	GY C 21	with given initial conditions.
	vectors. Use Vector integral theorems to facilitate vector	CLO 21	Evaluate line, surface and volume integral of
	integration.	CL C 22	vectors.
	megranon.	CLO 22	Use Vector integral theorems to facilitate
			vector integration.

X. COURSE LEARNING OUTCOMES (CLOs):

CLO Code	CLO's	At the end of the course, the student will have the ability to:	PO's Mapped	Strength of Mapping
AHSB02.01	CLO 1	Demonstrate knowledge of matrix calculation as an elegant and powerful mathematical language in connection with rank of a matrix	PO 1	3
AHSB02.02	CLO 2	Determine rank by reducing the matrix to Echelon and Normal forms.	PO 1 PO 2	3
AHSB02.03	CLO 3	Determine inverse of the matrix by Gauss Jordon Method.	PO 1	3
AHSB02.04	CLO 4	Find the complete solution of a non-homogeneous differential equation as a linear combination of the complementary function and a particular solution.	PO 1 PO 2	3

CLO Code	CLO's	At the end of the course, the student will have the ability to:	PO's Mapped	Strength of Mapping
AHSB02.05	CLO 5	Solving Second and higher order differential	PO 1	3
1115002.03	CLOS	equations with constant coefficients.	PO 2	3
AHSB02.06	CLO 6	Interpret the Eigen values and Eigen vectors of	PO 1	2
711151502.00	CLO	matrix for a linear transformation and use	101	2
		properties of Eigen values		
AHSB02.07	CLO 7	Understand the concept of Eigen values in real-	PO 4	1
		world problems of control field where they are		
		pole of closed loop system.		
AHSB02.08	CLO 8	Apply the concept of Eigen values in real-world	PO 4	1
		problems of mechanical systems where Eigen		
		values are natural frequency and mode shape.		
AHSB02.09	CLO 9	Use the system of linear equations and matrix to	PO 1	1
		determine the dependency and independency.	_	
AHSB02.10	CLO 10	Determine a modal matrix, and reducing a matrix	PO 1	3
		to diagonal form.	PO2	
AHSB02.11	CLO 11	Evaluate inverse and powers of matrices by using	PO 1	3
		Cayley-Hamilton theorem.		
AHSB02.12	CLO 12	Apply double integrals to evaluate area of a given	PO 2	2
		function.	_	
AHSB02.13	CLO 13	Utilize the concept of change order of integration	PO 1	3
		and change of variables to evaluate double	PO 2	
		integrals.	_	
AHSB02.14	CLO 14	Apply the Mean value theorems for the single	PO	2
		variable functions.	1	
AHSB02.15	CLO 15	Apply triple integrals to evaluate volume of a	PO 1	3
		given function.		
AHSB02.16	CI O 16	Find partial derivatives numerically and	PO 1	3
A115D02.10	CLO 10	symbolically and use them to analyze and	PO 2	3
		interpret the way a function varies.	102	
AHSB02.17	CI O 17	Understand the techniques of multidimensional	PO 1	3
Alisbuz.17	CLO 17	change of variables to transform the coordinates	PO 2	3
		by utilizing the Jacobian. Determine Jacobian for	102	
		the coordinate transformation.		
AHSB02.18	CLO 18		PO 1	3
A113B02.16	CLO 16	variable's and Lagrange's method of multipliers.	PO 2	3
AHSB02.19	CI O 10	Analyze scalar and vector fields and compute the	PO 1	3
Ansbuz.19	CLO 19	gradient, divergence and curl.	PO 1 PO 2	3
AHSB02.20	CLO 20	· ·	PO 1	3
A113D02.20	CLO 20	given initial conditions.	PO 1 PO 2	3
AHSB02.21	CI O 21	-	PO 2 PO 1	3
ADSB02.21	CLO 21	Evaluate line, surface and volume integral of	FUI	3
A H S D 02 22	CI () 22	Vectors. Use Vector integral theorems to facilitate vector	DO 1	2
AHSB02.22	CLO 22	_	PO 1	3
	1	integration.		

3= High; 2 = Medium; 1 = Low

XI. MAPPING COURSE OUTCOMES LEADING TO THE ACHIEVEMENT OF PROGRAM OUTCOMES

Course	Program Outcomes (POs)						
Outcomes (COs)	PO 1	PO 2	PO 4	PSO1			
CO 1	3	2		1			
CO 2		2	1				

CO 3	3	2	1
CO 4	3	2	1
CO 5	3	2	

XII. MAPPING COURSE LEARNING OUTCOMES LEADING TO THE ACHIEVEMENT OF PROGRAM OUTCOMES AND PROGRAM SPECIFIC OUTCOMES:

Course Learning	Program Outcomes (POs)							Program Specific Outcomes (PSOs)							
Outcomes (CLOs)	PO1	PO2	PO3	PO4	PO5	PO6	PO7	PO8	PO9	PO10	PO11	PO12	PSO1	PSO2	PSO3
CLO 1	3												1		
CLO 2	3	2													
CLO 3	3														
CLO 4	3	2											1		
CLO 5	3	2													
CLO 6	3														
CLO 7				1											
CLO 8				1											
CLO 9	3												1		
CLO 10	3	2													
CLO 11	3														
CLO 12	3	2											1		
CLO 13	3	2													
CLO 14	2												1		
CLO 15	3														
CLO 16	3	2											1		
CLO 17	2	2											1		
CLO 18	3	2											1		
CLO 19	3	2											1		
CLO 20	3	1											1		
CLO21	2														
CLO22	3			N. 1.									1		

3 =High; 2 =Medium; 1 =Low

XIII. ASSESSMENT METHODOLOGIES – DIRECT

CIE Exams	PO1, PO2, PO4,PSO1	SEE Exams	PO1, PO2, PO4,PSO1	Assignments	ı	Seminars	PO1, PO2, PO4,PSO1
Laboratory Practices	-	Student Viva	-	Mini Project	-	Certification	-
Term Paper	PO1, PO2, PO4,PSO1						

XIV. ASSESSMENT METHODOLOGIES - INDIRECT

~	Early Semester Feedback	/	End Semester OBE Feedback
×	Assessment of Mini Projects by Experts		

XV. SYLLABUS

	Madula I	THEORY OF MATRICES AND HIGHER ORDER LINEAR	Classes 00
Module-I	DIFFERENTIAL EQUATIONS	Classes: 09	

THEORY OF MATRICES: Real matrices: Symmetric, skew-symmetric and orthogonal matrices; Complex matrices: Hermitian, Skew-Hermitian and unitary matrices; Elementary row and column transformations; Rank of a matrix: Echelon form and normal form; Inverse by Gauss-Jordan method.

HIGHER ORDER LINEAR DIFFERENTIAL EQUATIONS: Linear differential equations of second and higher order with constant coefficients, non-homogeneous term of the type $f(x) = e^{ax}$, $\sin ax$, $\cos ax$ and $f(x) = x^n$, $e^{ax}v(x)$, xv(x); Method of variation of parameters.

Module-II L	LINEAR TRANSFORMATIONS AND DOUBLE INTEGRALS	Classes: 09
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LINEAR TRANSFORMATIONS: Cayley-Hamilton theorem: Statement, verification, finding inverse and powers of a matrix; Linear dependence and independence of vectors; Eigen values and Eigen vectors of a matrix and Properties (without proof); Diagonalization of matrix by linear transformation.

DOUBLE INTEGRALS: Evaluation of double integrals in Cartesian coordinates and Polar coordinates; Change of order of integration; Area as a double integral; Transformation of coordinate system.

Modulo III	FUNCTIONS OF SINGLE VARIABLES AND TRIPLE	Classes 00
Module-III	INTEGRALS	Classes: 09

FUNCTIONS OF SINGLE VARIABLES: Mean value theorems: Rolle's theorem, Lagrange's theorem, Cauchy's theorem-without proof and geometrical interpretation.

TRIPLE INTEGRALS: Evaluation of triple integrals in Cartesian coordinates; volume of a region using triple integration.

M - 1-1- TX7	FUNCTIONS OF SEVERAL VARIABLES AND EXTREMA OF A	CI00
Module-IV	FUNCTION	Classes: 09

FUNCTIONS OF SEVERAL VARIABLES: Partial differentiation, functional dependence, Jacobian.

EXTREMA OF A FUNCTION: Maxima and minima of functions of two variables without constraints and with constraints; Method of Lagrange multipliers.

Classes: 09

VECTOR DIFFERENTIAL CALCULUS: Scalar and vector point functions; Definitions of Gradient, divergent and curl with examples; Solenoidal and irrotational vector point functions; Scalar potential function.

VECTOR INTEGRAL THEOREMS: Line integral, surface integral and volume integral, Green's theorem in a plane, Stoke's theorem and Gauss divergence theorem without proofs.

Text Books:

- 1. B.S. Grewal, Higher Engineering Mathematics, Khanna Publishers, 36th Edition, 2010.
- 2. N.P. Bali and Manish Goyal, A text book of Engineering Mathematics, Laxmi Publications, Reprint, 2008.
- 3. Ramana B.V., Higher Engineering Mathematics, Tata McGraw Hill New Delhi, 11th Reprint 2010.

Reference Books:

- 1. Erwin Kreyszig, Advanced Engineering Mathematics, 9th Edition, John Wiley & Sons, 2006.
- 2. Veerarajan T., Engineering Mathematics for first year, Tata McGraw-Hill, New Delhi, 2008.
- 3. D. Poole, Linear Algebra: A Modern Introduction, 2nd Edition, Brooks/Cole, 2005.
- 4. Dr. M Anita, Engineering Mathematics-I, Everest Publishing House, Pune, 1st Edition, 2016.

XVI. COURSE PLAN:

The course plan is meant as a guideline. Probably there may be changes.

Lecture No	Topics to be covered	Course Learning Outcomes (CLOs)	Reference
1	Define types of matrices.	CLO 1	T2:32.1 R1:4.1
2	Apply Elementary row and column transformation.	CLO 2	T2:32.1 R1:4.2
3	Determine the Rank of a matrix, by Echelon form and Normal form.	CLO 2	T2:32.1 R1:4.3
4	Apply Gauss Jordan method to find inverse.	CLO 3	T2:32.1 R1:4.3
5	Determine complementary function for homogeneous higher order linear differential equations.	CLO 4	T3-2.9 R1:2.1
6	Solving non-homogeneous higher order linear differential equations: methods of finding particular integral.	CLO 5	T3-2.5 R1:2.8
7	Determine particular non-homogeneous term of the type $f(x) = e^{ax}$	CLO 5	T3-2.5 R1:2.8
8	Determine particular non-homogeneous term of the type $f(x) = \sin ax$, $\cos ax$	CLO 5	T3-2.5 R1:2.8
9	Determine particular for non-homogeneous term of the type $f(x) = x^n$	CLO 5	T3-2.5 R1:2.8
10	Determine of finding particular for non-homogeneous term of the type $f(x) = e^{ax}v(x)$	CLO 5	T3-2.5 R1:2.8
11	Determine of finding particular integral for non-homogeneous term of the type $f(x) = x^n v(x)$	CLO5	T3-2.5 R1:2.8
12	Solving second order linear differential equations using method of variation of parameters.	CLO 5	T3-2.61 R1:2.10
13	Apply Cayley-Hamilton theorem to find inverse of matrix.	CLO 11	T2:32.5 R1:4.6
14	Distinguish Linear dependency and independencey of vectors.	CLO 7	T2:32.5 R1:4.6

Lecture No	Topics to be covered	Course Learning Outcomes (CLOs)	Reference
15	Define and find Eigen values and Eigen vectors.	CLO 6	T2:32.4 R1:4.5
16	Define and apply the properties of Eigen values and Eigen vectors.	CLO 6	T2:32.4 R1:4.5
17	Use diagonalisation to diagonalise a square matrix and find higher powers of a matrix.	CLO 10	T2:32.7 R1:4.8
18	Calculate double integrals of a function in Cartesian form.	CLO 12	T2:15.5 R1:7.5
19	Calculate double integral of a function in polar form.	CLO 12	T2-16.5 R1:7.6
20	Use the Change of order of integrations Cartesian and polar form.	CLO 13	T2-16.5 R1:7.6
21	Use the Change of order of integrations Cartesian and polar form.	CLO 13	T2-16.5 R1:7.6
22	Use transformation of coordinate system to evaluate double integral.	CLO 13	T2-16.5 R1:7.6
23	Apply the Rolle's theorem.	CLO 14	T2-7.1 R1:7.4
24	Apply Lagrange's Mean Value Theorem.	CLO 14	T2-7.1 R1:7.4
25	Apply Cauchy's Mean Value Theorem.	CLO 14	T2-7.1 R1:7.4
26	Calculate triple integrals in Cartesian form .	CLO 15	T2-11.1 R2:6.15
27	Apply triple integration for finding the volume.	CLO 15	T2-11.1 R2:6.16
28	Find partial derivatives.	CLO16	T3:4.10
29	Apply Jacobian transformation.	CLO17	T3:4.42
30	Apply Jacobian transformation.	CLO17	T3:4.42
31	Determine maximum and minimum of a function of several variables.	CLO18	T2:7.1 R1:7.4
32	Determine maximum and minimum of a function of several variables.	CLO18	T2:7.1 R1:7.4
33	Use the Lagrange multiplier method to find extreme of functions with constraints.	CLO18	T2:7.1 R1:7.4
34	Define vector calculus and vector fields and their properties.	CLO19	T2:11.1 R2:6.15
35	Determine Solenoidal and irrotational vector point function.	CLO20	T2:10.1 R1:16.1
36	Determine Scalar potential function.	CLO20	T2:10.1 R1:16.2
37	Calculate line integral along smooth path and find work done.	CLO21	T2:10.3 R1:16.4
38	Calculate the surface area of field.	CLO21	T2:11.3 R1:16.5
39	Calculate volume of field.	CLO21	T2:11.3
40	Use Green's theorem to evaluate line integrals along simple	CLO22	R1:16.5 T2:11.3
41	closed contours on the plane. Use Green's theorem to evaluate line integrals along simple closed contours on the plane.	CLO22	R1:16.5 T2:11.3 R1:16.5

Lecture No	Topics to be covered	Course Learning Outcomes (CLOs)	Reference
42	Use the divergence theorem to give a physical interpretation of the divergence of a vector field.	CLO22	T2: 11.4
43	Use the divergence theorem to give a physical interpretation of the divergence of a vector field.	CLO22	R1:16.8
44	Use Stokes' theorem to give a physical interpretation of the curl of a vector field.	CLO22	T2: 11.3 R1:16.9
45	Use Stokes' theorem to give a physical interpretation of the curl of a vector field.	CLO22	T2: 11.3 R1:16.19

XVII. GAPS IN THE SYLLABUS - TO MEET INDUSTRY / PROFESSION REQUIREMENTS:

S No	Description	Proposed Actions	Relevance With POs	Relevance With PSOs
1	Matrices and its applications, applications of maxima and minima of functions of single and several variable.	Seminars	PO 1	PSO 1
2	Change of order of integration, geometrical interpretation of vector integral theorems and properties of gamma and Bessel differential equation.	Seminars / NPTEL	PO 2	PSO 1
3	Encourage students to solve real time applications and prepare towards competitive examinations.	NPTEL	PO 2	PSO 1

Prepared by:

Ms. P Rajani, Assistant Professor

HOD, ECE