Hall Ticket No | | | | | | | | | | | Question Paper Code: BAEB01

INSTITUTE OF AERONAUTICAL ENGINEERING

(Autonomous)

Dundigal, Hyderabad - 500 043

MODEL QUESTION PAPER-I

M. Tech I Semester End Examinations, January - 2020

Regulations: R18

ADVANCED MATHEMATICS IN AEROSPACE ENGINEERING

(AEROSPACE ENGINEERING)

Time: 3 hours **Max. Marks: 70**

Answer ONE Question from each UNIT
All Questions Carry Equal Marks
All parts of the question must be answered in one place only

UNIT – I

1. a) A continuous random variable has the probability density function [7M]

$$f(x)=\begin{cases} kxe^{-\lambda x}, \ for\ x\geq 0, \lambda>0 \\ 0, otherwise \end{cases}$$

Determine (i) k (ii) Mean (iii) Variance.

b) 1000 students have written an examination with the mean of test is 35 and standard deviation is 5. Assuming the distribution to be normal find i) How many students marks like between 25 and 40? ii) How many students get more than 40? iii) How many students get below 20? iv) How many students get more than 50. [7M]

2. a) The no. of automobile accidents per week in a certain area as follows: 12,8,20,2,14,10,15,6,9,4. Are these frequencies in agreement with the belief that accidents were same in the during last 10 weeks. [7M]

b) Time taken by workers in performing a job by method 1 and method 2 is given below. [7M]

Method 1	20	16	27	23	22	26	-
Method 2	27	33	42	35	32	34	38

Does the data show that variances of time distribution from population which these samples are drawn do not differ significantly?

UNIT – II

3. a) The means of two large samples of sizes 1000 and 2000 members are 67.5 inches and 68.0 inches respectively. Can the samples be regarded as drawn from the same population of S.D 2.5 inches [7M]

b) According to norms established for a mechanical aptitude test persons who are 18 years have an average weight of 73.2 with S.D 8.6 if 40 randomly selected persons have average 76.7 test the hypothesis H_0 : μ =73.2 against alternative hypothesis : μ >73.2. [7M]

4. a) A cigarette manufacturing firm claims that brand A line of cigarettes outsells its brand B by 8% .if it is found that 42 out of a sample of 200 smokers prefer brand A and 18 out of another sample of 100 smokers prefer brand B. Test whether 8% difference is a valid claim. [7M]

b) Three different methods of teaching statistics are used on three groups of students. Random samples of size 5 are taken from each group and the results are shown below the grades are on a 10-point scale [7M]

Group A	Group B	Group C
7	3	4
6	6	7
7	5	7
7	4	4
8	7	8

Determine on the basis of the above data whether there is difference in the teaching methods

UNIT – III

5. a) Using Taylor's series method find an approximate value of y at x = 0.2 for the differential equation $y' - 2y = 3e^x, y(0) = 0$. [7M]

b) Apply the 4th order Runge-Kutta method to find an approximate value of y when x=1.2 in steps of 0.1,given that $y' = x^2 + y^2$,y(1)=1.5 [7M]

6. a) Obtain the solution of $y' = x^2(1+y), y(1) = 1$ at $x = 1(0.1)1.2$ by any numerical method and estimate $x = 1.3$ by Adam's method. [7M]

b) Find $y(1.2)$ and $y(1.4)$ by Modified Euler's method given $y' = \log(x+y), y(0) = 2$ taking $h = 0.2.$ [7M]

UNIT – IV

7. a) Find the temperature in a thin metal rod of length L, with both ends insulated and with initial temperature in the rod in $\sin\left(\frac{\pi x}{L}\right)$. [7M]

b) Solve the partial differential equation $(mz - ny)p + (nx - lz)q = (ly - mx)$. [7M]

8. a) Solve $u_{xx} = u_y + 2u$ with $u(0, y) = 0$ and $\frac{\partial u(0, y)}{\partial x} = 1 + e^{-3y}$. [7M]

b) Solve the partial differential equation $(x^2 - yz)p + (y^2 - zx)q = z^2 - xy$ [7M]

UNIT – V

9. a) Write the diagonal five-point formula to solve the Laplace equation $u_{xx} + u_{yy} = 0$ and explain the procedure to solve it. [7M]

b) Find the solution of the parabolic equation $u_{xx} = 2u_t$ when $u(0,t) = u(4,t) = 0$ and $u(x,0) = x(4-x)$, taking $h = 1.$ Find the values upto $t = 5.$ [7M]

10. a) Solve $y_{tt} = y_{xx}$ upto t=0.5 with a spacing 0.1 subject to $y(0,t) = 0, y(1,t) = 0, y_t(x,0) = 0$ and $y(x,0) = 10 + x(1-x).$ [7M]

b) The traverse displacement u of a point at a distance x from one end and at any time t of a vibrating string satisfies the equation $\frac{\partial^2 u}{\partial t^2} = 4\frac{\partial^2 u}{\partial x^2}$, with boundary conditions $u = 0$ at $x = 0,\ t > 0$ and initial conditions $u = x(4-x)$ and $\frac{\partial u}{\partial t} = 0$ at $t = 0, 0 \le x \le 4$. Solve this equation numerically for one half period of vibration, taking $h = 1$ and $k = \frac{1}{2}$. [7M]

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COURSE OBJECTIVES:

The course should enable the students to:

I	Develop a basic understanding of a range of mathematics tools with emphasis on engineering applications.
II	Solve problems with techniques from advanced linear algebra, ordinary differential equations and multivariable differentiation.
III	Develop skills to think quantitatively and analyze problems critically.

COURSE OUTCOMES (COs):

CO 1	Describe the basic concepts of probability, discrete, continuous random variables and determine probability distribution, sampling distribution of statistics like t, F and chi-square.
CO 2	Understand the foundation for hypothesis testing to predict the significance difference in the sample means and the use of ANOVA technique.
CO 3	Determine Ordinary linear differential equations solvable by nonlinear ODE's.
CO 4	Explore First and second order partial differential equations.
CO 5	Analyze the methods for partial differential equations.

COURSE LEARNING OUTCOMES (CLOs):

BAEB01.01	Describe the basic concepts of probability, discrete and continuous random variables
BAEB01.02	Determine the probability distribution to find mean and variance.
BAEB01.03	Discuss the concept of sampling distribution of statistics like t, F and chi-square.
BAEB01.04	Understand the foundation for hypothesis testing.
BAEB01.05	Apply testing of hypothesis to predict the significance difference in the sample means.
BAEB01.06	Understand the assumptions involved in the use of ANOVA technique.
BAEB01.07	Solve differential equation using single step method.
BAEB01.08	Solve differential equation using multi step methods.
BAEB01.09	Understand the concept of non- linear ordinary differential equations.
BAEB01.10	Understand partial differential equation for solving linear equations.
BAEB01.11	Solving the first order ordinary differential equations subject to boundary conditions.
BAEB01.12	Solving the higher order ordinary differential equations subject to boundary conditions.
BAEB01.13	Understand the concept of methods for elliptic partial differential equations.
BAEB01.14	Understand the concept of Neumann and mixed problems.
BAEB01.15	Analyze the concept of parabolic and hyperbolic partial differential equations.

MAPPING OF SEMESTER END EXAMINATION - COURSE OUTCOMES

SEE Question No		Course Learning Outcomes		Course Outcomes	Blooms Taxonomy Level
1	a	BAEB01.01	Describe the basic concepts of probability, discrete and continuous random variables	CO 1	Understand
	b	BAEB01.02	Determine the probability distribution to find mean and variance.	CO 1	Understand
2	a	BAEB01.03	Discuss the concept of sampling distribution of statistics like t, F and chi-square.	CO 1	Understand
	b	BAEB01.03	Discuss the concept of sampling distribution of statistics like t, F and chi-square.	CO 1	Understand
3	a	BAEB01.05	Apply testing of hypothesis to predict the significance difference in the sample means.	CO 2	Understand
	b	BAEB01.05	Apply testing of hypothesis to predict the significance difference in the sample means.	CO 2	Remember
4	a	BAEB01.05	Apply testing of hypothesis to predict the significance difference in the sample means.	CO 2	Understand
	b	BAEB01.06	Understand the assumptions involved in the use of ANOVA technique.	CO 2	Understand
5	a	BAEB01.07	Solve differential equation using single step method.	CO 3	Understand
	b	BAEB01.08	Solve differential equation using multi step methods.	CO 3	Understand
6	a	BAEB01.08	Solve differential equation using multi step methods.	CO 3	Understand
	b	BAEB01.08	Solve differential equation using multi step methods.	CO 3	Understand
7	a	BAEB01.11	Solving the first order ordinary differential equations subject to boundary conditions.	CO 4	Understand
	b	BAEB01.10	Understand partial differential equation for solving linear equations.	CO 4	Understand
8	a	BAEB01.12	Solving the higher order ordinary differential equations subject to boundary conditions.	CO 4	Understand
	b	BAEB01.10	Understand partial differential equation for solving linear equations.	CO 4	Understand
9	a	BAEB01.13	Understand the concept of methods for elliptic partial differential equations.	CO 5	Remember
	b	BAEB01.15	Analyze the concept of parabolic and hyperbolic partial differential equations.	CO 5	Understand
10	a	BAEB01.15	Analyze the concept of parabolic and hyperbolic partial differential equations.	CO 5	Understand
	b	BAEB01.15	Analyze the concept of parabolic and hyperbolic partial differential equations.	CO 5	Understand

Signature of Course Coordinator **HOD, AE**