COMPUTATIONAL MATHEMATICS AND INTEGRAL CALCULUS

I Semester: CSE /ECE/ EEE/ IT II Semester: AE /CE/ ME								
Course Code	Category	Hours / Week			Credits	Maximum Marks		
AHS003	Foundation	L	T	P	C	CIA	SEE	Total
		3	1	-	4	30	70	100
Contact Classes: 45	Tutorial Classes: 15	Practical Classes: Nil				Total Classes: 60		

OBJECTIVES:

The course should enable the students to:

- I. Enrich the knowledge of solving Algebraic, transcendental equations by numerical methods.
- II. Apply multiple integration to evaluate mass, area and volume of the plane.
- III. Analyze gradient, divergence and curl to evaluate the integration over a vector field.
- IV. Understand the Bessel's equation to solve them under special conditions with the help of series solutions.

COURSE LEARNING OUTCOMES (CLOs):

- 1. Solve the Algebraic and transcendental equations using Bisection method, Method of False position and Newton-Raphson method.
- 2. Apply numerical methods to interpolate the functions of values for equal intervals using finite differences.
- 3. Understand the Newton-Raphson method to the real-world problem for a finite barrier quantum well
- 4. Evaluate the functional value by using Lagrange's interpolation formula for unequal intervals.
- 5. Understand the Lagrange's interpolation in real- world problem for neural network learning.
- 6. Apply method of least squares to fit linear and non linear curves.
- 7. Solve differential equation using single step method- Taylor's series.
- 8. Solve differential equation using multi step methods- Euler's, Modified Euler's and Runge Kutta methods.
- 9. Understand the multistep methods in real-world problem for real time Aircraft dynamics.
- 10. Understand the Runge-Kutta method in real- world problem for embedding the sensor signals into the iterative computation.
- 11. Evaluate double integral and triple integrals.
- 12. Utilize the concept of change order of integration to evaluate double integrals.
- 13. Determine the area and volume of a given curves using double and triple integration.
- 14. Understand transformation of co-ordinate system from plane to plane.
- 15. Analyze scalar and vector fields and compute the gradient, divergence and curl.
- 16. Understand integration of vector function.
- 17. Evaluate line, surface and volume integral of vectors.
- 18. Use Vector integral theorems to facilitate vector integration .
- 19. Analyze the concept of vector calculus in real- world problem for fluid dynamics.
- 20. Solve the Differential Equations by series solutions.
- 21. Understand Gamma function to evaluate improper integrals.
- 22. Analyze Bessel's function and study its properties.
- 23. Analyze Bessel's function as a Solution to Schrödinger equation in a cylindrical function of the second kind.
- 24. Understand gamma function to find application diverse areas as quantum physics.
- 25. Possess the knowledge and skills for employability and to succeed in national and International level competitive examinations.

UNIT-I ROOT FINDING TECHNIQUES AND INTERPOLATION

Root finding techniques: Solving algebraic and transcendental equations by Bisection method, Method of False position, Newton-Raphson method; Interpolation: Finite differences, forward differences, backward differences and central differences; Symbolic relations; Newton's forward interpolation, Newton's backward interpolation; Gauss forward central difference formula, Gauss backward central difference formula; Interpolation of unequal intervals: Lagrange,'s interpolation.

Classes: 10

Classes: 08

UNIT -II CURVE FITTING AND NUMERICAL SOLUTION OF ORDINARY DIFFERENTIAL EQUATIONS

Fitting a straight line; Second degree curves; Exponential curve, power curve by method of least squares; Taylor's series method; Step by step methods: Euler's method, modified Euler's method and Runge-Kutta method for first order differential equations.

UNIT-III MULTIPLE INTEGRALS Classes: 10

Double and triple integrals; Change of order of integration. Transformation of coordinate system; Finding the area of a region using double integration and volume of a region using triple integration.

UNIT -IV VECTOR CALCULUS Classes: 09

Scalar and vector point functions; Gradient, divergence, curl and their related properties; Solenoidal and irrotational vector point functions; Scalar potential function; Laplacian operator; Line integral, surface integral and volume integral; Vector integral theorems: Green's theorem in a plane, Stoke's theorem and Gauss divergence theorem without proofs.

UNIT -V SPECIAL FUNCTIONS Classes: 08

Gamma function, properties of gamma function; Ordinary point and regular singular point of differential equations; Series solutions to differential equations around zero, Frobenius method about zero; Bessel's differential equation: Bessel functions properties, recurrence relations, orthogonality, generating function, trigonometric expansions involving Bessel functions.

Text Books:

- 1.Kreyszig, "Advanced Engineering Mathematics", John Wiley & Sons Publishers, 10th Edition, 2010
- 2. B. S. Grewal, "Higher Engineering Mathematics", Khanna Publishers, 43rd Edition, 2015.

Reference Books:

- 1.T.K.V Iyengar, B.Krishna Gandhi, "Engineering Mathematics I", S. Chand & Co., 12th Edition, 2015.
- 2. T.K.V Iyengar, B.Krishna Gandhi, "Mathematical Methods", S. Chand & Co., 7th Edition, 2015
- 3. S. S. Sastry, "Introduction Methods of Numerical Analysis", Prentice-Hall of India Private Limited, 5th Edition, 2012.

Web References:

- 1. http://www.efunda.com/math/math_home/math.cfm
- 2. http://www.ocw.mit.edu/resourcs/#Mathematics
- 3. http://www.sosmath.com
- 4. http://www.mathworld.wolfram.com

E-Text Books:

- $1.\ http://www.keralatechnologicaluniversity.blogspot.in/2015/06/erwin-kreyszig-advanced-engineering-mathematics-ktu-ebook-download.html$
- 2. http://www.faadooengineers.com/threads/13449-Engineering-Maths-II-eBooks