## INSTITUTE OF AERONAUTICAL ENGINEERING <br> (Autonomous) <br> Dundigal, Hyderabad - 500043

CIVIL ENGINEERING
TUTORIAL QUESTION BANK

| Course Title | ADVANCED SOLID MECHANICS |  |  |  |  |
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| Course Code | BSTB02 |  |  |  |  |
| Programme | M.Tech |  |  |  |  |
| Semester | STE |  |  |  |  |
| Course Type | Core |  |  |  |  |
| Regulation | IARE - R18 |  |  |  |  |
| Course Structure | Theory |  |  | Practical |  |
|  | Lectures | Tutorials | Credits | Laboratory | Credits |
|  | 3 | - | 3 | - | - |
| Chief Coordinator | Dr. J S R Prasad, Professor, Civil Engineering |  |  |  |  |
| Course Faculty | Dr. J S R Prasad, Professor, Civil Engineering |  |  |  |  |

## I. COURSE OVERVIEW:

This course introduces the principles of elasticity, components of stresses and strains, differential equations of equilibrium, boundary conditions, compatibility conditions and stress function. This course also covers the two dimensional problems in rectangular coordinates and polar coordinates, Fourier series for two dimensional problems stress distribution symmetrical about an axis, pure bending of curved bars, strain components in polar coordinates, displacements for symmetrical stress distributions, simple symmetric and asymmetric problems, analysis of stress strain in three dimensions, torsion of prismatical bars and plasticity. This course in reached to student by power point presentations, lecture notes, and assignment questions, seminars, previous model question papers, and question bank of long and short answers.

## II. COURSE OBJECTIVES:

The course should enable the students to:

| I | Solve advanced solid mechanics problems using classical methods |
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| II | Apply commercial software on select, applied solid mechanics problems. |

## III. COURSE OUTCOMES (COs):

| CO 1 | Understand the theory of elasticity including strain/displacement and Hooke's law <br> relationships |
| :--- | :--- |
| CO 2 | Analyse solid mechanics problems using classical methods and energy methods |
| CO 3 | Solve for stresses and deflections of beams under unsymmetrical loading |
| CO 4 | Obtain stresses and deflections of beams on elastic foundations |
| CO 5 | Apply various failure criteria for general stress states at points |

## IV. COURSE LEARNING OUTCOMES:

Students, who complete the course, will have demonstrated the ability to do the following:

| CLO Code | CLO's | At the end of the course, the student will have the ability to: |
| :---: | :---: | :--- |
| BSTB02.01 | CLO 1 | Understand the Displacement, Strain and Stress Fields |
| BSTB02.02 | CLO 2 | Understand the Constitutive Relations, Cartesian Tensors |
| BSTB02.03 | CLO 3 | Solve the problems on Equations of Elasticity |
| BSTB02.04 | CLO 4 | Know the Elementary Concept of Strain |
| BSTB02.05 | CLO 5 | Understand the Strain at a Point |
| BSTB02.06 | CLO 6 | Know concept of Principal Strains and Principal Axes |
| BSTB02.07 | CLO 7 | Understand the concept of Compatibility Conditions |
| BSTB02.08 | CLO 8 | Understand the concept of Stress at a Point |
| BSTB02.09 | CLO 9 | Develop the Stress Components on an Arbitrary Plane |
| BSTB02.10 | CLO 10 | Understand the concepts on differential Equations of Equilibrium |
| BSTB02.11 | CLO 11 | Know the Hydrostatic and Deviatoric Components. |
| BSTB02.12 | CLO 12 | Understand the Equations of Equilibrium, Strain Displacement and |
| Compatibility Relations |  |  |
| BSTB02.13 | CLO 13 | Understand the formulation of Stress- Strain relations |
| BSTB02.14 | CLO 14 | Concept of Strain Displacement |
| BSTB02.15 | CLO 15 | Understand the solutions for boundary value problems |
| BSTB02.16 | CLO 16 | Know the co-axiality of the Principal Directions |
| BSTB02.17 | CLO 17 | Understand the Plane Stress and Plane Strain Problems |
| BSTB02.18 | CLO 18 | Know the Two-Dimensional Problems in Polar Coordinates |
| BSTB02.19 | CLO 19 | Understand the Saint Venant's Method, Prandtl's Membrane Analogy |
| BSTB02.20 | CLO 20 | Formulation of Torsion of Rectangular Bar and thin plates |
| BSTB02.21 | CLO 21 | Understand the concept of Plastic Stress-Strain Relations |
| BSTB02.22 | CLO 22 | Solution of Principle of Normality and Plastic Potential, Isotropic Hardening |

## TUTORIAL QUESTION BANK

| UNIT - I |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| INTRODUCTION TO ELASTICITY: |  |  |  |  |  |  |  |
| Part - A (Short Answer Questions) |  |  |  |  |  |  |  |
| 1 | Give the tensor notations of generalized three dimensional state of stress and strain at a point in an elastic material, with appropriate figures. |  |  |  | Remember | CO 1 | BSTB02.01 |
| 2 | Define Hooke's law and give the three dimensional equations for Hooke's law for an elastic material. |  |  |  | Understand | CO 1 | BSTB02.01 |
| 3 | Give the relationship between the three elastic modulli, namely Young's modulus, rigidity modulus and bulk modulus for an elastic material. |  |  |  | Remember | CO 1 | BSTB02.01 |
| 4 | What are Lame's constants? Give the relationship between stress and strain in terms of Lame's constant and rigidity modulus. |  |  |  | Understand | CO 1 | BSTB02.01 |
| 5 | Define principal planes and principal stresses |  |  |  | Remember | CO 1 | BSTB02.02 |
| 6 | What are stress-invariants? Give the expressions for the three stress-invariants? |  |  |  | Remember | CO 1 | BSTB02.02 |
| 7 | What are strain-invariants? Give the expressions for the three strain-invariants? |  |  |  | Understand | CO 1 | BSTB02.02 |
| 8 | Write the basic equations of equilibrium for a generalized three dimensional stress element? |  |  |  | Remember | CO 1 | BSTB02.02 |
| 9 | Write the strain displacement equations? |  |  |  | Remember | CO 1 | BSTB02.02 |
| 10 | Express the biharmonic equation for plane stress? |  |  |  | Remember | CO 1 | BSTB02.02 |
| Part - B (Long Answer Questions) |  |  |  |  |  |  |  |
| 1 | The state of stress at a point relative to an $x y z$ coordinate system is $\left[\begin{array}{ccc} 400 & 100 & -100 \\ 100 & 0 & 200 \\ -100 & 200 & 0 \end{array}\right] \mathrm{N} / \mathrm{mm}^{2} .$ <br> Determine the complete state of stress relative to an $x^{\prime} y^{\prime} z^{\prime}$ coordinate system if |  |  |  | Apply | CO 1 | BSTB02.01 |
|  |  | $x$ | $y$ | $z$ |  |  |  |
|  | $x^{\prime}$ | $30^{\circ}$ | $60^{\circ}$ | $90^{\circ}$ |  |  |  |
|  | $y^{\prime}$ | $120^{\circ}$ | $30^{\circ}$ | $90^{\circ}$ |  |  |  |
|  | $z^{\prime}$ | $90^{\circ}$ | $90^{\circ}$ | $90^{\circ}$ |  |  |  |
| 2 | The state of stress at a point relative to an $x y z$ coordinate system is $\left[\begin{array}{ccc}200 & 50 & -100 \\ 50 & 0 & 150 \\ -100 & 150 & 0\end{array}\right] \mathrm{N} / \mathrm{mm}^{2}$. Determine the complete state of stress relative to an $x^{\prime} y^{\prime} z^{\prime}$ coordinate system if |  |  |  | Apply | CO 1 | BSTB02.01 |
|  |  | $x$ | $y$ | z |  |  |  |
|  | $x^{\prime}$ | $45^{\circ}$ | $30^{\circ}$ | $90^{\circ}$ |  |  |  |
|  | $y^{\prime}$ | $60^{\circ}$ | $45^{\circ}$ | $90^{\circ}$ |  |  |  |
|  | $z^{\prime}$ | $90^{\circ}$ | $90^{\circ}$ | $90^{\circ}$ |  |  |  |


| 3 | The state of stress at a point relative to an $x y z$ coordinate system is $\left[\begin{array}{ccc} 500 & 150 & -200 \\ 150 & 0 & 200 \\ -200 & 200 & 0 \end{array}\right] \mathrm{N} / \mathrm{mm}^{2}$ <br> Determine the complete state of stress relative to an $x^{\prime} y^{\prime} z^{\prime}$ coordinate system if | Apply | CO 1 | BSTB02.01 |
| :---: | :---: | :---: | :---: | :---: |
| 4 | At point Q in a body the state of stress relative to a $x y z$ coordinate system is $\left[\begin{array}{ccc} 500 & 200 & -200 \\ 200 & 0 & 400 \\ -200 & 400 & 300 \end{array}\right] \mathrm{MPa}$ <br> Using the cube shown in Fig., determine the normal and shear stress at point Q for surface parallel to the plane $B C G F$ | Apply | CO 1 | BSTB02.02 |
| 5 | At point Q in a body the state of stress relative to a $x y z$ coordinate system is $\left[\begin{array}{ccc} 400 & 250 & -200 \\ 250 & 0 & 300 \\ -200 & 300 & 200 \end{array}\right] \mathrm{MPa}$ <br> Using the cube shown in Fig., determine the normal and shear stress at point Q for surface parallel to the plane $A B E F$. | Apply | CO 1 | BSTB02.02 |
| 6 | At point Q in a body the state of stress relative to a $x y z$ coordinate system is $\left[\begin{array}{ccc} 600 & 300 & -250 \\ 300 & 0 & 500 \\ -250 & 500 & 400 \end{array}\right] \mathrm{MPa}$ <br> Using the cube shown in Fig., determine the normal and shear stress at point Q for surface parallel to the plane $B G E$. | Apply | CO 1 | BSTB02.02 |


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|  | $\tau_{x y}=-200, \quad \tau_{y z}=100, \quad \tau_{z x}=-300 \mathrm{kPa} .$ <br> Determine the stress invariants. |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Part - C (Problem Solving and Critical Thinking Questions) |  |  |  |  |
| 1 | The given displacement components are: $u_{x}=c x(y+z)^{2}, u_{y}=c y(x+z)^{2}, u_{z}=c z(x+y)^{2}$, where c is a constant. Find <br> (a) the components of linear strain. <br> (b) the components of rotation. | Analyze \& Evaluate | CO 1 | BSTB02.01 |
| 2 | A plate whose thickness is 3 mm is stretched as shown in Fig. Find the principal strains and the maximum shearing strain in the plate. | Analyze \& Evaluate | CO 1 | BSTB02.02 |
| 3 | The stress field on a body is given by $\begin{gathered} \sigma_{x}=20 x^{2}+y^{2}, \quad \sigma_{y}=30 x^{3}+200, \sigma_{z} \\ =30\left(y^{2}+z^{2}\right) \\ \tau_{x y}=z x, \quad \tau_{x z}=y^{2} z, \tau_{y z}=x^{3} y \end{gathered}$ <br> What are the components of the body force required to ensure equilibrium? | Analyze \& Evaluate | CO 1 | BSTB02.02 |
| 4 | The state of stress at a point is given by $\left[\tau_{i j}\right]=10^{2}\left[\begin{array}{ccc} 10 & 5 & -10 \\ 5 & 20 & -15 \\ -10 & -15 & -10 \end{array}\right] \mathrm{MPa}$ <br> Find the magnitude and direction of the stress vector acting on a plane whose normal has direction cosines $(1 / 2,1 / 2,1 / \sqrt{2})$. What are the normal and tangential stresses acting on this plane? | Analyze \& Evaluate | CO 1 | BSTB02.02 |
| 5 | The state of strain at a point within a material is given by: $\left[\begin{array}{ccc} 200 & 100 & 0 \\ 100 & 300 & 400 \\ 0 & 400 & 0 \end{array}\right] \times 10^{-6}$ <br> For $E=200 \mathrm{GPa}$ and $G=80 \mathrm{GPa}$, ascertain the components of stress tensor. | Analyze \& Evaluate | CO 1 | BSTB02.02 |
| 6 | The state of stress at a point is given by $\begin{gathered} \sigma_{x}=100, \sigma_{y}=200, \quad \sigma_{z}=-100 \\ \tau_{x y}=-200, \quad \tau_{y z}=100, \quad \tau_{z x}=-300 \mathrm{kPa} \end{gathered}$ <br> Determine the principal stresses and the direction cosines of the principal planes. | Analyze \& Evaluate | CO 1 | BSTB02.02 |
| 7 | The displacement field in a body is specified as: $\begin{gathered} u_{x}=\left(x^{2}+3\right) \times 10^{-3} \\ u_{y}=3 y^{2} z \times 10^{-3} \\ u_{z}=(x+3 z) \times 10^{-3} \end{gathered}$ <br> Determine the strain components at a point whose co-ordinates are $(1,2,3)$ | Analyze \& Evaluate | CO 1 | BSTB02.02 |
| 8 | The state of stress at a point is given by: $\left[\begin{array}{ccc} 20 & -6 & 10 \\ -6 & 10 & 8 \\ 10 & 8 & 7 \end{array}\right] \mathrm{MPa} .$ <br> Determine the principal stresses and principal directions. | Analyze \& Evaluate | CO 1 | BSTB02.02 |


| 9 | The stress field in a continuous body is given by: $\left[\tau_{i j}\right]=\left[\begin{array}{ccc} 1 & 0 & 2 y \\ 0 & 1 & 4 x \\ 2 y & 4 x & 1 \end{array}\right] \mathrm{kPa} .$ <br> Find the stress vector at point $P(1,2,3)$,acting on a plane $x+y+z=6$. | Analyze \& Evaluate | CO 1 | BSTB02.02 |
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| 10 | The given displacement components are: $u_{x}=c x(y+z)^{2}, u_{y}=$ $c y(x+z)^{2}, u_{z}=c z(x+y)^{2}$, where c is a constant. Find the principal strains at a point whose co-ordinates are ( $1,1,1$ ). | Analyze \& Evaluate | CO 1 | BSTB02.02 |
| UNIT - II |  |  |  |  |
| STRAIN AND STRESS FIELD: |  |  |  |  |
| Part - A (Short Answer Questions) |  |  |  |  |
| 1 | Express the stress function in the form of a doubly infinite power series. | Remember | CO 2 | BSTB02.03 |
| 2 | Express the stress compatibility equation for plane stress case. | Remember | CO 2 | BSTB02.03 |
| 3 | Express the stress compatibility equation for plane strain case. | Remember | CO 2 | BSTB02.03 |
| 4 | Give the equations relating to bending of a beam by uniform load. | Understand | CO 2 | BSTB02.04 |
| 5 | What are conjugate harmonic functions and analytic functions? Give the property of the analytic functions. | Remember | CO 2 | BSTB02.04 |
| 6 | Give the Cauchy-Riemann equations for a stress field. What is the significance of the Cauchy-Riemann equations? | Remember | CO 2 | BSTB02.05 |
| 7 | Express the displacement and stress configurations in terms of complex potentials. | Remember | CO 2 | BSTB02.06 |
| 8 | How does the stress function satisfies the biharmonic equation? | Remember | CO 2 | BSTB02.06 |
| 9 | Express the stresses acting in a Tapering beam | Understand | CO 2 | BSTB02.06 |
| 10 | Express the stresses acting in an infinite wedge. | Remember | CO 2 | BSTB02.07 |
| 11 | Express the stress components in terms of an Airy stress function | Remember | CO 2 | BSTB02.07 |
| 12 | Express the equilibrium equations in polar co-ordinates. | Remember | CO 2 | BSTB02.07 |
| Part - B (Long Answer Questions) |  |  |  |  |
| 1 | A cantilever beam of rectangular cross-section 40 mm wide and 60 mm thick is 800 mm in length. It carries a load of 500 N at the free end. Determine the stresses in the cantilever at mid-length. | Apply | CO 2 | BSTB02.03 |
| 2 | A rectangular beam 80 mm wide and 100 mm thick is of 600 mm in length. It carries a uniformly distributed load of intensity 10 $\mathrm{N} / \mathrm{mm}$ throughout its length. Plot the variation of stresses in the beam at mid-span. | Apply | CO 2 | BSTB02.03 |
| 3 | A cantilever of length $l$ in x-dimension and depth 2C along the $y$ dimension is loaded with a load P at the free end. The support conditions at $x=l$ are given as: $\begin{array}{lll} \text { At } & x=l, y=0 & : u_{x}=u_{y}=0 \\ \text { At } & x=l, y= \pm C & : u_{x}=0 \end{array}$ <br> Show that the deflection is now $\left(u_{y}\right)_{x=y=0}=\frac{P l^{3}}{3 E l}\left[1+\frac{1}{2}(4+5 v) \frac{C^{2}}{l^{2}}\right]$ | Apply | CO 2 | BSTB02.04 |
| 4 | Show that $\left(A e^{\alpha y}+B e^{-\alpha y}+C y e^{\alpha y}+D y e^{-\alpha y}\right) \sin \alpha x$ is a stress function in two dimensional stress field. | Apply | CO 2 | BSTB02.04 |
| 5 | Derive series expressions for the stresses in a semi-infinite plate, $y>0$, with normal pressure on the straight edge $(y=0)$ having the distribution | Apply | CO 2 | BSTB02.04 |


|  | $\sum_{m=1}^{\infty} b_{m} \sin \frac{m \pi x}{l}$ |  |  |  |
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| 6 | Show that if $V$ is a plane harmonic function, i.e. it satisfies the Laplace equation $\nabla^{2} V=0$, then the functions $x V, y V,\left(x^{2}+y^{2}\right) V$ satisfy the bilharmonic equation and so can be used as stress functions. | Apply | CO 2 | BSTB02.05 |
| 7 | Determine the stress fields that arise from the following stress functions: <br> i. $\quad \phi=C y^{2}$ <br> ii. $\quad \phi=A x^{2}+B x y+C y^{2}$ | Apply | CO 2 | BSTB02.06 |
| 8 | Determine the stress fields that arise from the following stress function: $\phi=A x^{3}+B x^{2} y+C x y^{2}+D y^{3}$ | Apply | CO 2 | BSTB02.06 |
| 9 | A cantilever of length $l$ in $x$-dimension and depth 2C along the $y-$ dimension is loaded with a load P at the free end. The stress field for this cantilever considering bending and transverse shear effects are: $\sigma_{x}=-\frac{P x y}{I}, \sigma_{y}=0, \quad \tau_{x y}=-\frac{P}{2 I}\left(C^{2}-y^{2}\right)$ <br> Verify that this stress field satisfies the equilibrium equations. | Apply | CO 2 | BSTB02.07 |
| 10 | Find the stress and displacement fields corresponding to the complex potentials $\varphi(z)=\alpha+i A z, \psi(z)=\beta$ where $\alpha$ and $\beta$ are complex constants and A is real. Interpret this displacement field. | Apply | CO 2 | BSTB02.07 |
| Part - C (Problem Solving and Critical Thinking Questions) |  |  |  |  |
| 1 | Show that the complex potentials $\varphi(z)=\alpha z, \quad \psi(z)=\beta$ <br> Correspond to a uniform stress field. Find $\alpha$ and $\beta$ so that $\sigma_{x}=X, \quad \tau_{x y}=S, \quad \sigma_{y}=Y$ | Analyze \& Evaluate | CO 2 | BSTB02.03 |
| 2 | Determine the stress and displacement fields in an infinite medium due to equal and opposite point forces acting at different points along their common line of action. | Analyze \& Evaluate | CO 2 | BSTB02.03 |
| 3 | Consider the effect of a point force $X+i Y$ acting at an internal point $Z_{0}$ of the half plane $S^{+}$when the boundary $y=0$ is unstressed. Determine the normal displacement on $y=0$. | Analyze \& Evaluate | CO 2 | BSTB02.04 |
| 4 | Using Fourier integral method, determine the solution of biharmonic equation in Cartesian co-ordinates. | Analyze \& Evaluate | CO 2 | BSTB02.04 |
| 5 | A semi-infinite elastic medium is subjected to a normal pressure of intensity $p$ distributed over a circular area of radius $\alpha$ at $x=0$. <br> Determine the stress distribution by using Fourier integral method. | Analyze \& Evaluate | CO 2 | BSTB02.04 |
| 6 | Show that the stress function $\phi=C\left[\left(x^{2}+y^{2}\right) \tan ^{-1} \frac{y}{x}-x y\right]$ <br> provides the solution to the problem of the semi-infinite elastic medium acted upon by a uniform pressure $q$ on one side of the origin | Analyze \& Evaluate | CO 2 | BSTB02.04 |
| 7 | Investigate the plane stress problem represented by the Airy's stress function | Analyze \& Evaluate | CO 2 | BSTB02.06 |


|  | $\phi=\frac{3 F}{4 h}\left(x y-\frac{x y^{3}}{3 h^{2}}\right)+\frac{P}{2} y^{2}$ <br> where h is half depth of the beam and $F$ is the concentrated load. |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| 8 | A cantilever beam loaded at its free end has a stress function $\phi=A x y+B \frac{x y^{3}}{6}$ <br> Determine an expression for the vertical deflection curve. | Analyze \& Evaluate | CO 2 | BSTB02.06 |
| ${ }^{9}$ | Using Airy's stress function, $\phi=B\left(y^{3}+\frac{3}{4} y h^{2}\right)+F \frac{y^{2}}{8}$ <br> determinethe stress distribution at $0<x<l$ for $y= \pm h$, where ' $l$ ' is the span of the beam, ' $2 h$ ' the depth of the beam and $F$ the load. | Analyze \& Evaluate | CO 2 | BSTB02.07 |
| 10 | Using the stress function $\phi=\frac{3 P}{4 c}\left(x y-\frac{x y^{3}}{3 c^{2}}\right),$ <br> determine the deflection at the free end of a cantilever, with the conditions $0<x<l$ and $y= \pm c$. | Analyze \& Evaluate | CO 2 | BSTB02.07 |
| UNIT - III |  |  |  |  |
| EQUATIONS OF ELASTICITY AND TWO-DIMENSIONAL PROBLEMS OF ELASTICITY: |  |  |  |  |
| Part - A (Short Answer Questions) |  |  |  |  |
| 1 | Write the equations of equilibrium of the elemental tetrahedron, with three edges along the $\mathrm{x}, \mathrm{y}$ and z -axes. | Remember | CO 3 | BSTB02.08 |
| 2 | Write the expression for normal stress on the inclined plane of an elemental tetrahedron the direction cosines of whose normal are $l$, $m$ and $n$, and whose other faces lie in three coordinate planes. | Remember | CO 3 | BSTB02.08 |
| 3 | Give the equation of the stress ellipsoid and describe what their axes represent. | Understand | CO 3 | BSTB02.08 |
| 4 | What is stress-director surface? | Remember | CO 3 | BSTB02.09 |
| 5 | Give the cubic equation whose three roots are the principal stresses and whose coefficients are the stress-invariants? | Remember | CO 3 | BSTB02.09 |
| 6 | What do we mean by stress invariants? Explain why are they so called? | Remember | CO 3 | BSTB02.09 |
| 7 | Give the expressions for octahedral shear stress? | Remember | CO 3 | BSTB02.09 |
| 8 | Explain what is meant by homogeneous deformation and represent its conditions? | Understand | CO 3 | BSTB02.10 |
| 8 | Give the strain-displacement relations depicting both normal and shear strains. | Remember | CO 3 | BSTB02.10 |
| 9 | Write the three strain invariants, give their expressions. | Remember | CO 3 | BSTB02.10 |
| 10 | Write the equations of equilibrium of the elemental tetrahedron, with three edges along the $\mathrm{x}, \mathrm{y}$ and z -axes. | Remember | CO 3 | BSTB02.10 |
| 11 | Write the differential equations of equilibrium at a point in an elastic body. | Understand | CO 3 | BSTB02.11 |
| 12 | Give the boundary conditions associated with the differential equations of equilibrium. | Remember | CO 3 | BSTB02.11 |
| 13 | Give the differential relations of the conditions of compatibility. | Remember | CO 3 | BSTB02.11 |
| 14 | Write the stress-compatibility equations in three dimensions, also called Beltrami-Michell equations, when the body forces are constant. | Remember | CO 3 | BSTB02.12 |


| 15 | Give the equations of equilibrium in terms of displacements, also called as Navier equations for elasticity in solids. | Remember | CO 3 | BSTB02.12 |
| :---: | :---: | :---: | :---: | :---: |
| 16 | State the uniqueness theorem associated with the solution of the differential equations of equilibrium. | Remember | CO 3 | BSTB02.12 |
| 17 | Explain the Betti's Reciprocal theorem of displacements used in the theory of elasticity. | Understand | CO 3 | BSTB02.12 |
| Part - B (Long Answer Questions) |  |  |  |  |
| 1 | A rectangular bar of length $a$, breadth $b$ and height $h$ is standing under its own weight. Determine the stress distribution in the bar. | Apply | CO 3 | BSTB02.08 |
| 2 | A prismatic bar of 2a $\times 2 \mathrm{~b}$ cross-section is bent by two equal and opposite couples. Determine the equations for the bent shape of the prismatic bar. | Apply | CO 3 | BSTB02.08 |
| 3 | Derive the vector form of the equilibrium equations | Apply | CO 3 | BSTB02.08 |
| 4 | Show that for an irrotational deformation of a body, the displacement vector is the gradient of a scalar potential function. | Apply | CO 3 | BSTB02.09 |
| 5 | Derive the expression for the Octahedral shear stress. | Apply | CO 3 | BSTB02.09 |
| 6 | Derive the differential equations of equilibrium in three dimensional cartesian coordinates using a rectangular parallelepiped element. | Understand | CO 3 | BSTB02.10 |
| 7 | Derive the conditions of compatibility in terms of strains in three dimensional cartesian coordinate system. | Understand | CO 3 | BSTB02.10 |
| 8 | Derive the conditions of compatibility in terms of stresses in three dimensional cartesian coordinate system from the strain compatibility equations. | Understand | CO 3 | BSTB02.11 |
| 9 | Derive the Navier equations in elasticity, which are the equations of equilibrium in terms of displacements. | Understand | CO 3 | BSTB02.11 |
| 10 | Explain the principle of superposition applicable for the body and surface forces in the differential equations of equilibrium. | Understand | CO 3 | BSTB02.12 |
| Part - C (Problem Solving and Critical Thinking Questions) |  |  |  |  |
| 1 | Derive the expression for normal stress on the inclined plane on an elemental tetrahedron, which has three faces along the coordinate planes. | Analyze \& Evaluate | CO 3 | BSTB02.08 |
| 2 | Derive the equation for obtaining the principal stresses for a three dimensional stress system. | Analyze \& Evaluate | CO 3 | BSTB02.08 |
| 3 | Derive the expressions for the displacements of a prismatic bar by its own self-weight considering a three dimensional stress system | Analyze \& Evaluate | CO 3 | BSTB02.09 |
| 4 | Derive the equations of equilibrium of a stressed element in cylindrical coordinates. | Analyze \& Evaluate | CO 3 | BSTB02.09 |
| 5 | Derive the expressions for the components of the rotation vector. | Analyze \& Evaluate | CO 3 | BSTB02.10 |
| 6 | The state of strain at a point within a material is given by: $\left[\begin{array}{ccc} 200 & 100 & 0 \\ 100 & 300 & 400 \\ 0 & 400 & 0 \end{array}\right] \times 10^{-6}$ <br> For $E=200 \mathrm{GPa}$ and $G=80 \mathrm{GPa}$, ascertain the components of stress tensor. | Apply | CO 3 | BSTB02.10 |
| 7 | The state of stress at a point is given by $\begin{aligned} \sigma_{x}=100, \sigma_{y}=200, \quad \sigma_{z}=-100 \\ \tau_{x y}=-200, \quad \tau_{y z}=100, \quad \tau_{z x}=-300 \mathrm{kPa} \end{aligned}$ <br> Determine the principal stresses and the direction cosines of the principal planes. | Apply | CO 3 | BSTB02.11 |
| 8 | The state of strain at a point is given by $\varepsilon_{x}=0.001, \varepsilon_{y}=-0.003, \varepsilon_{z}=0.002$ | Apply | CO 3 | BSTB02.11 |


|  | $\gamma_{x y}=0.001, \gamma_{y z}=0.0005, \gamma_{y z}=-0.002$ <br> Determine the strain invariants and the prinicipal strains. |  |  |  |
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| 9 | The given displacement components are: $u_{x}=c x(y+z)^{2}, u_{y}=$ $c y(x+z)^{2}, u_{z}=c z(x+y)^{2}$, where c is a constant. Find <br> (a) the components of linear strain. <br> (b) the components of rotation. | Apply | CO 3 | BSTB02.12 |
| 10 | The displacement field in a body is specified as: $\begin{gathered} u_{x}=\left(x^{2}+3\right) \times 10^{-3} \\ u_{y}=3 y^{2} z \times 10^{-3} \\ u_{z}=(x+3 z) \times 10^{-3} \end{gathered}$ <br> Determine the strain components at a point whose co-ordinates are $(1,2,3)$ | Apply | CO 3 | BSTB02.12 |
| UNIT - IV |  |  |  |  |
| TORSION OF PRISMATIC BARS: |  |  |  |  |
| Part - A (Short Answer Questions) |  |  |  |  |
| 1 | Give the torsion equation for circular cross-section and explain its terms. | Remember | CO 4 | BSTB02.13 |
| 2 | Write the Poisson's equation for torsion of prismatic bars of noncircular cross-sections, explaining the various terms. | Remember | CO 4 | BSTB02.13 |
| 3 | Write the expressions for the angle of twist and the torsional rigidity for a bar of elliptical cross-section, with major and minor axes of 2 a and 2 b , respectively. | Understand | CO 4 | BSTB02.14 |
| 4 | For a bar of cross-section of an equilateral triangle of side 'a', what is the relationship between torque, $T$, and angle of twist per unit length? $G$ is the modulus of rigidity. | Remember | CO 4 | BSTB02.14 |
| 5 | State and explain the Bredt's formula for torsion of thin walled tubes. | Remember | CO 4 | BSTB02.15 |
| 6 | Write the simple bending equation for symmetrical cross-sections of a beam. | Remember | CO 4 | BSTB02.16 |
| 7 | Give the governing differential equation of bending of a cantilever by load $P$ at its free end, when the cantilever has a non-uniform cross-section. | Understand | CO 4 | BSTB02.17 |
| 8 | Give the governing differential equation of bending of a bar of circular cross-section in terms of stress functions | Remember | CO 4 | BSTB02.18 |
| 9 | Give the governing differential equation of bending of a bar of an elliptical cross-section in terms of stress functions | Remember | CO 4 | BSTB02.19 |
| 10 | Give the governing differential equation of bending of a bar of a rectangular cross-section in terms of stress functions | Understand | CO 4 | BSTB02.20 |
| Part - B (Long Answer Questions) |  |  |  |  |
| 1 | Using St. Venant's theory derive the Poisson's equation for torsion of prismatic bars of non-circular cross-sections. | Understand | CO 4 | BSTB02.13 |
| 2 | Derive the expressions for the angle of twist and the torsional rigidity for a bar of elliptical cross-section, with major and minor axes of 2 a and 2 b , respectively. | Understand | CO 4 | BSTB02.13 |
| 3 | Derive the relationship between torque, T, and angle of twist per unit length for a bar of cross-section of an equilateral triangle of side 'a'. | Remember | CO 4 | BSTB02.14 |
| 4 | Derive the torsion equation of a thin rectangular section.. | Understand | CO 4 | BSTB02.14 |
| 5 | Derive the torsion equation of a hollow cylinder. | Understand | CO 4 | BSTB02.15 |
| 6 | Derive the simple bending equation for symmetrical cross-sections | Understand | CO 4 | BSTB02.16 |


|  | of a beam. |  |  |  |
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| 7 | Derive the governing equation of bending of a cantilever, with a non-uniform cross-section, subjected to load P at its free end. | Understand | CO 4 | BSTB02.17 |
| 8 | Derive the governing differential equation of bending of a bar of circular cross-section in terms of stress functions | Understand | CO 4 | BSTB02.18 |
| 9 | Derive the governing differential equation of bending of a bar of an elliptical cross-section in terms of stress functions | Remember | CO 4 | BSTB02.19 |
| 10 | Derive the governing differential equation of bending of a bar of a rectangular cross-section in terms of stress functions | Understand | CO 4 | BSTB02.20 |
| Part - C (Problem Solving and Critical Thinking Questions) |  |  |  |  |
| 1 | A square shaft rotating at 250 rpm , transmits torque to a crane which is designed to lift maximum load of 150 kN at a speed of $10 \mathrm{~m} / \mathrm{min}$. If the efficiency of crane gearing is $65 \%$ estimate the size of the shaft for the maximum permissible shear stress of 35 MPa . Also calculate the angle of twist of the shaft for a length of 3 m . Take $\mathrm{G}=100 \mathrm{GPa}$. | Apply | CO 4 | BSTB02.14 |
| 2 | A 300 mm steel beam with flanges and web 12.5 mm thick, flange width 300 mm is subjected to a torque of 4 kN m . Find the maximum shear and angle of twist per unit length. $\mathrm{G}=100 \mathrm{GPa}$. | Apply | CO 4 | BSTB02.14 |
| 3 | An elliptical shaft of semi axes $\mathrm{a}=0.05 \mathrm{~m}, \mathrm{~b}=0.025 \mathrm{~m}$ and $\mathrm{G}=80$ GPa is subjected to a twisting moment of $1200 \pi \mathrm{Nm}$. Determine the maximum shearing stress and the angle of twist per unit length. | Apply | CO 4 | BSTB02.15 |
| 4 | A hollow aluminium section of external dimensions $100 \mathrm{~mm} \times 50$ mm and thickness 5 mm is designed for a maximum shear stress of 35 Mpa . Find the maximum permissible twisting moment for this section and the angle of twist under this moment per metre length. $\mathrm{G}=28 \mathrm{GPa}$. | Apply | CO 4 | BSTB02.15 |
| 5 | A hollow circular torsion member has an outside diameter of 22 mm and inside diameter of 18 mm , with mean diameter $\mathrm{D}=$ 20 mm and $\mathrm{t} / \mathrm{D}=0.10$. Calculate the torque and angle of twist per unit length if shearing stress at mean diameter is 70 MPa . Calculate these values if a cut is made through the wall thickness along the entire length. $\mathrm{G}=77.5 \mathrm{GPa}$. | Apply | CO 4 | BSTB02.15 |
| 6 | A prismatic bar of length 5 m and a rectangular cross-section of $80 \mathrm{~mm} \times 100 \mathrm{~mm}$ is fixed at one end as a cantilever. At the free end, 1 kN load acting in the plane of the cross-section but inclined at $30^{\circ}$ to the vertical is applied. Determine the maximum stress in the cantilever beam. | Apply | CO 4 | BSTB02.16 |
| 7 | A prismatic bar of circular cross-section of radius 25 mm is subjected to a terminal load of 5 kN . Determine the stresses in the bar at the end of the horizontal diameter. Compare the result with the elementary solution. Assume poisson's ratio $=0.3$. | Apply | CO 4 | BSTB02.17 |
| 8 | A prismatic bar of elliptical cross-section has its semi-minor axes as 40 mm and 20 mm respectively. This bar is subjected to an end loadof 2500 N . Determine the stresses in the bar at the end of major and minor axes. Assumepoisson's ratio $=0.28$. | Apply | CO 4 | BSTB02.18 |
| 9 | A prismatic bar of rectangular cross-section $50 \mathrm{~mm} \times 30 \mathrm{~mm}$ issubjected to an end load of 4500 N . Determine the stresses at thecentre of the bar and the corner. Assume $v=0.3$ | Apply | CO 4 | BSTB02.19 |
| 10 | A rectangular beam $120 \mathrm{~mm} \times 100 \mathrm{~mm}$ is 3 min length and is simplysupported at the ends. It carries a load of 5 kN at mid-span inclined at $45^{\circ}$ with the vertical axis and passing through the centroid.Determine the maximum bending stress in the beam. | Apply | CO 4 | BSTB02.20 |


| UNIT - V |  |  |  |  |
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| PLASTIC DEFORMATION: |  |  |  |  |
| Part - A (Short Answer Questions) |  |  |  |  |
| 1 | What is meant by yield criteria in the theory of plasticity? | Remember | CO 5 | BSTB02.22 |
| 2 | Give the yield conditions in the theory of plasticity? | Remember | CO 5 | BSTB02.22 |
| 3 | Give the assumptions in plastic analysis. | Understand | CO 5 | BSTB02.21 |
| 4 | What are residual stresses in plastic bending? | Remember | CO 5 | BSTB02.21 |
| 5 | Define shape factor and load factor? | Remember | CO 5 | BSTB02.21 |
| 6 | What is a plastic hinge? | Understand | CO 5 | BSTB02.21 |
| 7 | Give the Tresca's yield criteria in the theory of plasticity | Remember | CO 5 | BSTB02.21 |
| 8 | Give the Von-Mises yield criteria. | Understand | CO 5 | BSTB02.22 |
| 9 | What are the tangent and plastic moduli? | Remember | CO 5 | BSTB02.22 |
| 10 | Define the Plastic hinge and Plastic Moment Capacity in plastic analysis of beams | Remember | CO 5 | BSTB02.21 |
| Part - B (Long Answer Questions) |  |  |  |  |
| 1 | Explain the Tresca's yield criteria giving the diagram of the yield envelop. | Understand | CO 5 | BSTB02.22 |
| 2 | Explain the Mises's yield criteria giving the diagram of the yield envelop. | Understand | CO 5 | BSTB02.22 |
| 3 | Explain the various flow models of plasticity: perfectly plastic, elastoplastic and strain hardening. | Remember | CO 5 | BSTB02.21 |
| 4 | State and explain the Bauschinger effect. | Understand | CO 5 | BSTB02.21 |
| 5 | Derive the expression for shape factor for a rectangular beam cross-section. | Understand | CO 5 | BSTB02.21 |
| 6 | Derive the expression for shape factor for a circular beam crosssection. | Remember | CO 5 | BSTB02.21 |
| 7 | Derive the expression for shape factor for a triangular beam crosssection. | Understand | CO 5 | BSTB02.21 |
| 8 | Derive the expression for shape factor for a symmetric I -section. | Understand | CO 5 | BSTB02.22 |
| 9 | Draw and comparatively explain the conventional or engineering stress-strain diagram and true stress - true strain diagram. | Remember | CO 5 | BSTB02.22 |
| 10 | Derive the relationship between true strain and the conventional linear strain. | Understand | CO 5 | BSTB02.22 |
|  | Part - C (Problem Solving and Critical Thinking Questions) |  |  |  |
| 1 | A tensile specimen with a 12 mm initial diameter and 50 mm gauge length reaches maximum load at 90 kN and fractures at 70 kN . The maximum diameter at fracture is 10 mm . Determine engineering stress at maximum load (the ultimate tensile strength), true fracture stress, true strain at fracture and engineering strain at fracture. | Apply | CO 5 | BSTB02.21 |
| 2 | Stress analysis of a structural member gives the state of stress shown below. If the part is made from aluminium alloy whose yield stress, $\sigma=500 \mathrm{MPa}$, will it exhibit yielding as per Von Mises criteria? If not, what is the safety factor? | Apply | CO 5 | BSTB02.21 |


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| 3 | Use the maximum-shear-stress criterion to establish whether yielding will occur for the stress state shown in the figure. $\sigma_{z}=50 \mathrm{MPa}$ | Apply | CO 5 | BSTB02.21 |
| 4 | Calculate the shape factor of the T-section as shown in the figure. The yield stress, $\mathrm{f}_{\mathrm{y}}=250 \mathrm{~N} / \mathrm{mm}^{2}$. | Apply | CO 5 | BSTB02.22 |
| 5 | Calculate the shape factor of the T-section as shown in the figure. The yield stress, $\mathrm{f}_{\mathrm{y}}=300 \mathrm{~N} / \mathrm{mm}^{2}$. | Apply | CO 5 | BSTB02.22 |


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| Calculate the shape factor of the T-section as shown in the figure. <br> The yield stress, $\mathrm{f}_{\mathrm{y}}=275 \mathrm{~N} / \mathrm{mm}^{2}$. | Apply | CO 5 | BSTB02.22 |



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