INSTITUTE OF AERONAUTICAL ENGINEERING
(Autonomous)
Dundigal, Hyderabad-500043

## INFORMATION TECHNOLOGY

## TUTORIAL QUESTION BANK

| Course Title | PROBABILITY AND STATISTICS |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Course Code | AHSB 12 |  |  |  |  |
| Programme | B.Tech |  |  |  |  |
| Semester | II CSE | CSE \| IT |  |  |  |
|  | III AE | AE \| ME |  |  |  |
|  | IV CE | CE |  |  |  |
| Course Type | Foundation |  |  |  |  |
| Regulation | IARE - R18 |  |  |  |  |
| Course Structure | Theory |  |  | Practical |  |
|  | Lectures | Tutorials | Credits | Laboratory | Credits |
|  | 3 | 1 | 4 | - | - |
| Chief Coordinator | Dr. M Anita, Professor |  |  |  |  |
| Course Faculty | Dr. J Suresh Goud, Associate Professor Ms. V Subbalaxmi, Assistant Professor Mr. Ch. Chaitanya, Assistant Professor |  |  |  |  |

## COURSE OBJECTIVES:

| The course should enable the students to: |  |
| :---: | :--- |
| I | Enrich the knowledge of probability on single random variables and probability distributions. |
| II | Apply the concept of correlation and regression to find covariance. |
| III | Determine mean and variance of given data by sampling distribution. |
| IV | Analyze the given data for appropriate test of hypothesis. |

## COURSE OUTCOMES (COs):

| CO 1 | Discuss the concepts of probability, conditional probability, Baye's theorem and random variables |
| :--- | :--- |
| CO 2 | Classify the probability distributions and study their properties |
| CO 3 | Understand the concepts of correlation and regression to the given data. |
| CO 4 | Apply testing of Hypothesis for sample means and sample proportions. |
| CO 5 | Estimate the truth value of the statistical hypotheses by using small sample tests. |

## COURSE LEARNING OUTCOMES (CLOs):

| AHSB12.01 | Describe the basic concepts of probability. |
| :---: | :--- |
| AHSB12.02 | Summarize the concept of conditional probability and estimate the probability of event using <br> Baye's theorem. |
| AHSB12.03 | Analyze the concepts of discrete and continuous random variables, probability distributions, <br> expectation and variance. <br> AHSB12.04 |
| Use the concept of random variables in real-world problem like graph theory; machine |  |
| learnin, Natural language processing. |  |$|$| AHSB12.06 | Understand binomial distribution to the phenomena of real-world problem like sick versus <br> healthy. |
| :---: | :--- |
| AHSB12.07 | Determine the poisson distribution to find mean and variance. |
| AHSB12.08 | Use poisson distribution in real-world problem to predict soccer scores. |
| AHSB12.09 | Illustrate the inferential methods relating to the means of normal distributions. |
| AHSB12.10 | Describe the mapping of normal distribution in real-world problem to analyze the stock <br> market. |
| AHSB12.11 | Explain multiple random variables and the covariance of two random variables. |
| AHSB12.12 | Understand the concept of multiple random variables in real-world problems aspects of <br> wireless communication system. |
| AHSB12.13 | Calculate the correlation coefficient to the given data. |
| AHSB12.14 | Contrast the correlation and regression to the real-world such as stock price and interest rates. |
| AHSB12.15 | Calculate the regression to the given data. |
| AHSB12.16 | Discuss the concept of sampling distribution of statistics and in particular describe the <br> behavior of the sample mean. |
| AHSB12.17 | Understand the foundation for hypothesis testing. |
| AHSB12.18 | Summarize the concept of hypothesis testing in real-world problem to selecting the best means <br> to stop smoking. |
| AHSB12.19 | Apply testing of hypothesis to predict the significance difference in the sample means. |
| AHSB12.20 | Apply testing of hypothesis to predict the significance difference in the sample proportions. |
| AHSB12.21 | Use Student t-test to predict the difference in sample means. |
| AHSB12.22 | Apply F-test to predict the difference in sample variances. |
| AHSB12.23 | Understand the characteristics between the samples using Chi-square test. |

## TUTORIAL QUESTION BANK

## MODULE- I

## PROBABILITY AND RANDOM VARIABLES

Part - A (Short Answer Questions)

| S No | QUESTIONS | Blooms Taxonomy Level | Course Outcomes | Course <br> Learning Outcomes (CLOs) |
| :---: | :---: | :---: | :---: | :---: |
| 1 | What is the definition of probability? | Remember | CO 1 | AHSB12.01 |
| 2 | What is the probability for a leap year to have 52 Mondays and 53 Sundays? | Understand | CO 1 | AHSB12.01 |
| 3 | What is conditional probability? | Remember | CO 1 | AHSB12.02 |
| 4 | State Baye's theorem. | Remember | CO 1 | AHSB12.02 |
| 5 | Define the discrete and continuous random variables with a suitable example. | Remember | CO 1 | AHSB12.03 |
| 6 | List the important Properties of probability density function. | Remember | CO 1 | AHSB12.03 |
| 7 | Obtain the probability distribution of getting number tails if we toss three coins. | Remember | CO 1 | AHSB12.03 |
| 8 | Define the term mathematical expectation of a probability distribution function | Remember | CO 1 | AHSB12.03 |
| 9 | Define the term Mean and Variance of a probability mass function. | Remember | CO 1 | AHSB12.03 |
| 10 | Define the term Mean and Variance of a probability density function. | Remember | CO 1 | AHSB12.03 |
| 11 | Find the probability distribution for sum of scores on dice if we throw two dice. | Remember | CO 1 | AHSB12.03 |
| 12 | Out of 24 mangoes, 6 mangoes are rotten. If we draw two mangoes. Obtain probability distribution of number of rotten mangoes that can be drawn. | Remember | CO 1 | AHSB12.03 |
| 13 | If X is a random variable then Prove $\mathrm{E}[\mathrm{X}+\mathrm{K}]=\mathrm{E}[\mathrm{X}]+\mathrm{K}$, where ' K ' constant. | Understand | CO 1 | AHSB12.03 |
| 14 | Prove that $\sigma^{2}=E\left(X^{2}\right)-\mu^{2}$. | Understand | CO 1 | AHSB12.03 |
| 15 | Explain probability mass function and probability density of random variables. | Remember | CO 1 | AHSB12.03 |
| 16 | If X is Discrete Random variable then Prove that Variance $(\mathrm{aX}+\mathrm{b})=\mathrm{a}^{2}$ Variance(X). | Understand | CO 1 | AHSB12.03 |
| 17 | A fair coin is tossed six times. Find the probability of getting four heads. | Understand | CO 1 | AHSB12.03 |
| 18 | Define different types of random variables with example. | Remember | CO 1 | AHSB12.03 |
| 19 | A coin is tossed 9 times. Find the probability of getting 5 heads. | Understand | CO 1 | AHSB12.03 |
| 20 | Define random variable with an example. | Remember | CO 1 | AHSB12.03 |
| Part - B (Long Answer Questions) |  |  |  |  |
| 1 | A bag A contains 2 white and 3 red balls and a bag B contains 4 white and 5 red balls. One ball is drawn at random from one of the bags and it is found to be red. Find the probability that the red ball drawn is from bag B. | Understand | CO 1 | AHSB12.02 |
| 2 | Suppose 5 men out of 100 and 25 women out of 10000 are colour blind. A colour blind person is chosen at random. What is the probability of the person being a male (Assume male and female to be in equal numbers)? | Understand | CO 1 | AHSB12.02 |
| 3 | In a bolt factory machines A, B, C manufacture $20 \%, 30 \%$ and $50 \%$ of the total of their output and $6 \%, 3 \%$ and $2 \%$ are defective. A bolt is drawn at random and found to be defective. Find the probabilities that it is manufactured from (i) Machine A (ii) Machine B (iii) Machine C. | Understand | CO 1 | AHSB12.02 |
| 4 | Bag I contains 2 white, 3 red balls and bag II contains 4 white, 5 red balls, one ball is drawn at random from one of the bag it found to be red. Find the probability that red ball is drawn from bag I. | Understand | CO 1 | AHSB12.02 |
| 5 | In a certain college $25 \%$ are boys $10 \%$ are girls are studying statistics, the girls constitute $60 \%$ of class room. <br> a) What is the probability that statistics is being studied? <br> b) If a student is selected at random and is found to be studying statistics, find the probability that the student is a girl? | Understand | CO 1 | AHSB12.02 |
| 6 | The length of time(in minutes) that a certain lady speaks on the telephone is found to be random phenomenon, with a probability function specified by the function $f(x)=\left\{\begin{array}{l}A e^{-\frac{x}{5}}, x \geq 0 \\ 0, \text { otherwise }\end{array}\right.$. (i) Find the value of A that makes $f(x)$ a probability density function. (ii) What is the probability that she will take over the phone is more than 20 minutes? | Understand | CO 1 | AHSB12.03 |




| 11 | Explain about Normal distribution. |  |  |  |  |  |  |  |  | Remember | CO 2 | AHSB12.09 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 12 | What is the recurrence relation for binomial distribution? |  |  |  |  |  |  |  |  | Remember | CO 2 | AHSB12.05 |
| 13 | The mean and variance of a binomial distribution are 4 and $4 / 3$ respectively. Then find $\mathrm{P}(\mathrm{x}=1)$. |  |  |  |  |  |  |  |  | Understand | CO 2 | AHSB12.05 |
| 14 | In eight throws of a die 5 or 6 is considered a success. Find the mean number of success |  |  |  |  |  |  |  |  | Understand | CO 2 | AHSB12.05 |
| 15 | If a bank received on the average 6 bad cheques per day, find the probability that it will receive 4 bad cheques on any given day. |  |  |  |  |  |  |  |  | Understand | CO 2 | AHSB12.05 |
| 16 | Define Normal curve. |  |  |  |  |  |  |  |  | Remember | CO 2 | AHSB12.09 |
| 17 | Define the terms Mean, Variance of Poisson distribution |  |  |  |  |  |  |  |  | Remember | CO 2 | AHSB12.07 |
| 18 | Define the term mode of a Binomial distribution. |  |  |  |  |  |  |  |  | Remember | CO 2 | AHSB12.05 |
| 19 | Define the terms mean, variance of Binomial distribution. |  |  |  |  |  |  |  |  | Remember | CO 2 | AHSB12.05 |
| 20 | Draft the recurrence relation for the Binomial distribution. |  |  |  |  |  |  |  |  | Remember | CO 2 | AHSB12.05 |
| Part - B (Long Answer Questions) |  |  |  |  |  |  |  |  |  |  |  |  |
| 1 | Out of 20 tape recorders 5 are defective. Find the standard deviation of defective in the sample of 10 randomly chosen tape recorders. Find (i) $P(X=0)$ (ii) $P(X=1)$ (iii) $\mathrm{P}(\mathrm{X}=2)$ (iv) $\mathrm{P}(1<\mathrm{X}<4)$. |  |  |  |  |  |  |  |  | Understand | CO 2 | AHSB12.05 |
| 2 | A car-hire firm has two cars which it hires out day by day. The number of demands for a car o $n$ each day is distributed as a Poisson distribution with mean 1.5. Calculate the proportion of days (i) on which there is no demand (ii) on which demand is refused. |  |  |  |  |  |  |  |  | Understand | CO 2 | AHSB12.07 |
| 3 | The average number of phone calls per minute coming into a switch board between 2 P.M. and 4 P.M. is 2.5 . Determine the probability that during one particular minute (i) 4 or fewer calls (ii) more than 6 calls. |  |  |  |  |  |  |  |  | Understand | CO 2 | AHSB12.07 |
| 4 | In 1000 sets of trials per an event of small probability the frequencies $f$ of the number of $x$ of successes are |  |  |  |  |  |  |  |  | Understand | CO 2 | AHSB12.07 |
|  | X | 1 | 2 | 3 | 4 | 5 | 6 | 7 | Tot |  |  |  |
|  | f | 365 | 210 | 80 | 28 | 9 | 2 | 1 | 100 |  |  |  |
|  | Fit the expected frequencies Using Poisson. |  |  |  |  |  |  |  |  |  |  |  |
| 5 | For a normally distributed variate with mean 1 and standard deviation 3 . <br> Find <br> i) $\mathrm{P}(3.43 \leq \mathrm{X} \leq 6.19)$ <br> ii) $\mathrm{P}(-1.43 \leq \mathrm{X} \leq 6.19)$. |  |  |  |  |  |  |  |  | Understand | CO 2 | AHSB12.09 |
| 6 | If X is a normal variate with mean 30 and standard deviation 5 . Find the probabilities that i) P $(26 \leq \mathrm{X} \leq 40)$ <br> ii) $\mathrm{P}(\mathrm{X} \geq 45)$. |  |  |  |  |  |  |  |  | Understand | CO 2 | AHSB12.09 |
| 7 | 4 coins are tossed 160 times. Fit the Binomial distribution of getting number of heads. |  |  |  |  |  |  |  |  | Understand | CO 2 | AHSB12.05 |
| 8 | The mean weight of 500 male students at a certain college is 75 kg and the standard deviation is 7 kg . Assuming that the weights are normally distributed find how many students weight (i) Between 60 and 78 kg (ii) more than 92 kg . |  |  |  |  |  |  |  |  | Understand | CO 2 | AHSB12.09 |
| 9 | The mean and standard deviation of the box obtained by 1000 students in an examination are respectively 34.5 and 16.5 . Assuming the normality of the distribution. Find the approximate number of students expected to obtain marks between 30 and 60 . |  |  |  |  |  |  |  |  | Understand | CO 2 | AHSB12.09 |
| 10 | If the masses of 300 students are normally distributed with mean 68 kgs and standard deviation 3 kgs. How many students have masses (i) greater than 72 kg (ii) less than or equal to 64 kg (iii) between 65 and 71 kg inclusive. |  |  |  |  |  |  |  |  | Understand | CO 2 | AHSB12.09 |
| 11 | Out of 800 families with 5 children each, how many would you expect to have (i) 3 boys (ii) 5 girls (iii)either 2 or 3 boys? Assume equal probabilities for boys and girls. |  |  |  |  |  |  |  |  | Understand | CO 2 | AHSB12.05 |
| 12 | If a Poisson distribution is such that $P(X=1)=\frac{3}{2} P(X=3)$ then find (i) $P(X \geq 1)$ <br> (ii) $P(X \leq 3)$ <br> (iii) $P(2 \leq X \leq 5)$. |  |  |  |  |  |  |  |  | Understand | CO 2 | AHSB12.07 |
| 13 | Average number of accidents on any day on a national highway is 1.8. Determine the probability that the number of accidents is (i) at least one (ii) at most one. |  |  |  |  |  |  |  |  | Understand | CO 2 | AHSB12.07 |
| 14 | In a Normal distribution, $7 \%$ of the item are under 35 and $89 \%$ are under 63. Find the mean and standard deviation of the distribution. |  |  |  |  |  |  |  |  | Understand | CO 2 | AHSB12.09 |
| 15 | A shipment of 20 tape recorders contains 5 defectives find the standard deviation of the probability distribution of the number of defectives in a sample of 10 |  |  |  |  |  |  |  |  | Understand | CO 2 | AHSB12.07 |



| 9 | From the following data calculate (i) correlation c coefficient (ii) standard deviation of $y$.$\text { bxy }=0.85, \text { byx }=0.89, \sigma_{x}=3 .$ |  |  |  |  |  |  |  |  |  |  | Understand | CO 3 | AHSB12.14 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 10 | If $\mathrm{N}=8, \sum X=544, \sum Y=552, \sum X Y=37560$ then find $\operatorname{COV}(\mathrm{X}, \mathrm{Y})$. |  |  |  |  |  |  |  |  |  |  | Understand | CO 3 | AHSB12.12 |
| 11 | The equations of two regression lines are $7 x-16 y+9=0,5 y-4 x-3=0$. Find the coefficient of correlation. |  |  |  |  |  |  |  |  |  |  | Understand | CO 3 | AHSB12.14 |
| 12 | What are normal equations for regression lines? |  |  |  |  |  |  |  |  |  |  | Remember | CO 3 | AHSB12.14 |
| 13 | Explain about multiple correlation. |  |  |  |  |  |  |  |  |  |  | Remember | CO 3 | AHSB12.14 |
| 14 | If $\mathrm{r}_{12}=0.5, \mathrm{r}_{13}=0.3, \mathrm{r}_{23}=0.45$ then find multiple correlation coefficient $\mathrm{R}_{1.23}$. |  |  |  |  |  |  |  |  |  |  | Understand | CO 3 | AHSB12.14 |
| 15 | What is the regression equation of $\mathrm{X}_{1}$ on $\mathrm{X}_{2}$ and $\mathrm{X}_{3}$ ? |  |  |  |  |  |  |  |  |  |  | Remember | CO 3 | AHSB12.14 |
| 16 | Define multiple regressions. |  |  |  |  |  |  |  |  |  |  | Remember | CO 3 | AHSB12.14 |
| 17 | If $r_{12}=0.77, r_{13}=0.72, r_{23}=0.52$ Find the multiple correlation coefficient $\mathrm{R}_{1.23}$. |  |  |  |  |  |  |  |  |  |  | Understand | CO 3 | AHSB12.14 |
| 18 | Write the properties of regression lines. |  |  |  |  |  |  |  |  |  |  | Remember | CO 3 | AHSB12.14 |
| 19 | Write the difference between correlation and regression. |  |  |  |  |  |  |  |  |  |  | Remember | CO 3 | AHSB12.14 |
| 20 | If $\mathrm{r}_{12}=0.8, \mathrm{r}_{13}=0.5$ and $\mathrm{r}_{23}=0.3$ then find multiple correlation coefficient $\mathrm{R}_{1.23}$. |  |  |  |  |  |  |  |  |  |  | Understand | CO 3 | AHSB12.14 |
|  | Part - B (Long Answer Questions) |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 1 | A random sample of 5 college students is selected and their grades in mathematics and statistics are found to be |  |  |  |  |  |  |  |  |  |  | Understand | CO 3 | AHSB12.13 |
|  | $\square$ |  | 1 | 2 | 3 |  |  | 4 |  | 5 |  |  |  |  |
|  | Mathematics |  | 85 | 60 | 73 |  |  | 40 |  | 90 |  |  |  |  |
|  | Statistics |  | 93 | 75 | 65 |  |  | 50 |  | 80 |  |  |  |  |
|  | Calculate Spearman's rank correlation coefficient. |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 2 | Calculate the coefficient of correlation from the following data |  |  |  |  |  |  |  |  |  |  | Understand | CO 3 | AHSB12.12 |
|  | 12 | 9 | 8 | 10 | 11 |  | 13 | 7 |  |  |  |  |  |  |
|  | y 14 | 8 | 6 | 9 | 11 |  | 12 | 13 |  |  |  |  |  |  |
| 3 | The following data gives the marks in obtained by 10 students in accountancy and statistics. |  |  |  |  |  |  |  |  |  |  | Understand | CO 3 | AHSB12.13 |
|  | R. No. | 1 | 2 | 3 | 4 - 5 | 6 | 7 | 8 | 9 | 10 |  |  |  |  |
|  | Accountancy <br> Statistics | y 45 | 70 | 65 | $30 \quad 90$ | 40 | 50 | 75 | 85 | 60 |  |  |  |  |
|  |  | 35 | 90 | 70 | $40 \quad 95$ | 40 | 80 | 80 | 80 | 50 |  |  |  |  |
|  | Find the coefficient of correlation. |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 4 | Calculate the Karl Pearson's coefficient of correlation from the following data. |  |  |  |  |  |  |  |  |  |  | Understand | CO 3 | AHSB12.12 |
|  | Wages | 100 | 101 | 102 | 102 | 100 | 99 | 97 | 98 | 96 | 95 |  |  |  |
|  | $\begin{array}{\|c} \hline \begin{array}{c} \text { Cost of } \\ \text { living } \end{array} \\ \hline \end{array}$ | 98 | 99 | 99 | 97 | 95 | 92 | 95 | 94 | 90 | 91 |  |  |  |
| 5 | Find a suitable coefficient of correlation for the following data: |  |  |  |  |  |  |  |  |  |  | Understand | CO 3 | AHSB12.12 |
|  | Fertilizer used(tones) | 15 | -18 | 20 | 24 | 30 | 3 |  | 40 | 50 |  |  |  |  |
|  | Productivity (tones) | $85$ | 93 | 95 | 105 | 120 | 13 |  | 150 | 160 |  |  |  |  |
| 6 | The following table give the distribution of the total population and those who are totally partially blind among them. Find out if there is any relation between age and blindness. |  |  |  |  |  |  |  |  |  |  | Understand | CO 3 | AHSB12.12 |
|  | Age | 0-10 | 10-20 | 20-30 | 30-40 |  | 40-50 | 50-60 |  | 60-70 | 70- |  |  |  |
|  | No. of Persons (000) | 100 | 60 | 40 | 36 |  | 24 | 11 |  | 6 | 3 |  |  |  |
|  | Blind | 55 | 40 | 40 |  | 0 | 36 |  | 22 | 18 | 1.5 |  |  |  |
| 7 | Following are the ranks obtained by 10 students in two subjects, Statistics and Mathematics. To what extent the knowledge of the students in two subjects is related? |  |  |  |  |  |  |  |  |  |  | Understand | CO 3 | AHSB12.13 |
|  | Statistics | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | $9 \mathrm{l}{ }^{9} 10$ |  |  |  |  |
|  | Mathematics | - 2 | 4 | 1 | 5 | 3 | 9 | 7 | 10 | 6 6 |  |  |  |  |




| 9 | If the population consists of four members $1,5,6,8$. How many samples of size three can be drawn with replacement? | Understand | CO 4 | AHSB12.16 |
| :---: | :---: | :---: | :---: | :---: |
| 10 | The mean weekly wages of workers are with standard deviation of rupees 4. A sample of 625 is selected. Find the standard error of the mean. | Understand | CO 4 | AHSB12.16 |
| 11 | Distinguish between large and small samples with example. | Remember | CO 4 | AHSB12.16 |
| 12 | In a manufacturing company out of 100 goods 25 are top quality. Find sample proportion. | Understand | CO 4 | AHSB12.20 |
| 13 | Construct the confidence interval for single mean if mean of sample size of 400 is 40 , standard deviation is 10 . | Understand | CO 4 | AHSB12.19 |
| 14 | Construct the confidence interval for single proportion if 18 goods are defective from a sample of 200 goods. | Understand | CO 4 | AHSB12.20 |
| 15 | Define sample proportion. | Remember | CO 4 | AHSB12.20 |
| 16 | In a manufacturing company out of 200 goods 80 were faulty. Find sample proportion. | Understand | CO 4 | AHSB12.20 |
| 17 | Find the sample proportion in one day production of 400 articles only 50 are top quality. | Understand | CO 4 | AHSB12.20 |
| 18 | Write the test statistic for difference of means in large samples. | Remember | CO 4 | AHSB12.19 |
| 19 | Write the test statistic for difference of proportions in large samples. | Remember | CO 4 | AHSB12.20 |
| 20 | Find the confidence interval for mean if mean of sample size of 144 is 150 , standard deviation is 2 . | Understand | CO 4 | AHSB12.19 |
| Part - B (Long Answer Questions) |  |  |  |  |
| 1 | A population consists of five numbers 2,3,6,8 and 11. Consider all possible samples of size two which can be drawn with replacement from this population. Find <br> i) The mean of the population. <br> ii) The standard deviation of the population. <br> iii) The mean of the sampling distribution of means. <br> iv) The standard deviation of the sampling distribution of means. | Understand | CO 4 | AHSB12.16 |
| 2 | A population consists of $5,10,14,18,13,24$. Consider all possible samples of size two which can be drawn without replacement from this population. Find <br> i) The mean of the population. <br> ii) The standard deviation of the population. <br> iii) The mean of the sampling distribution of means. <br> iv) The standard deviation of the sampling distribution of means. | Understand | CO 4 | AHSB12.16 |
| 3 | A population consists of five numbers $4,8,12,16,20,24$. Consider all possible samples of size two which can be drawn without replacement from this population. Find <br> i) The mean of the population. <br> ii) The standard deviation of the population. <br> iii) The mean of the sampling distribution of means. <br> iv) he standard deviation of the sampling distribution of means. | Understand | CO 4 | AHSB12.16 |
| 4 | Samples of size 2 are taken from the population 1, 2, 3, 4, 5, 6. Which can be drawn with replacement? Find <br> i) The mean of the population. <br> ii) The standard deviation of the population. <br> iii) The mean of the sampling distribution of means. <br> iv) T he standard deviation of the sampling distribution of means. | Understand | CO 4 | AHSB12.16 |
| 5 | Samples of size 2 are taken from the population 3, 6, 9, 15 27. Which can be drawn with replacement? Find <br> i) The mean of the population <br> ii) The standard deviation of the population iii) The mean of the sampling distribution of means <br> iv) The standard deviation of the sampling distribution of means. | Understand | CO 4 | AHSB12.16 |
| 6 | If the population is $3,6,9,15,27$ <br> i) List all possible samples of size 3 that can be taken without replacement from the finite population. <br> ii) Calculate the mean of each of the sampling distribution of means. <br> iii) Find the standard deviation of sampling distribution of means. | Understand | CO 4 | AHSB12.16 |
| 7 | The mean height of students in a college is 155 cms and standard deviation is 15 . What is the probability that the mean height of 36 students is less than 157 cms . | Understand | CO 4 | AHSB12.16 |


| 8 | A random sample of size 100 is taken from an infinite population having the mean 76 and the variance 256 . What is the probability that $\bar{x}$ will be between 75 and 78. |  |  |  | Understand | CO 4 | AHSB12.16 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 9 | The mean of certain normal population is equal to the standard error of the mean of the samples of 64 from that distribution. Find the probability that the mean of the sample size 36 will be negative. |  |  |  | Understand | CO 4 | AHSB12.16 |
| 10 | A random sample of size 64 is taken from a normal population with $\mu=51.4$ and $\sigma=68$. What is the probability that the mean of the sample will <br> i) exceed 52.9 <br> ii) fall between 50.5 and 52.3 <br> iii) be less than 50.6. |  |  |  | Understand | CO 4 | AHSB12.16 |
| 11 | A sample of 400 items is taken from a population whose standard deviation is 10.The mean of sample is 40 .Test whether the sample has come from a population with mean 38 also calculate $95 \%$ confidence interval for the population. |  |  |  | Understand | CO 4 | AHSB12.19 |
| 12 | The means of two large samples of sizes 1000 and 2000 members are 67.5 inches and 68.0 inches respectively. Can the samples be regarded as drawn from the same population of S.D 2.5 inches. |  |  |  | Understand | CO 4 | AHSB12.19 |
| 13 | An ambulance service claims that it takes on the average 8.9 minutes to reach its destination In emergency calls. To check on this claim the agency which issues license to Ambulance service has then timed on fifty emergency calls getting a mean of 9.2 minutes with 1.6 minutes. What can they conclude at $5 \%$ level of significance? |  |  |  | Understand | CO 4 | AHSB12.19 |
| 14 | According to norms established for a mechanical aptitude test persons who are 18 years have an average weight of 73.2 with S.D 8.6 if 40 randomly selected persons have average 76.7 test the hypothesis $H_{0}: \mu=73.2$ againist alternative hypothesis : $\mu>73.2$. |  |  |  | Understand | CO 4 | AHSB12.19 |
| 15 | A sample of 100 electric bulbs produced by manufacturer 'A' showed a mean life time of 1190 hrs and $\mathrm{s} . \mathrm{d}$. of 90 hrs A sample of 75 bulbs produced by manufacturer 'B' Showed a mean life time of 1230 hrs with s.d. of 120 hrs . Is there difference between the mean life times of the two brands at a significance level of 0.05 . |  |  |  | Understand | CO 4 | AHSB12.19 |
| 16 | On the basis of their total scores, 200 candidates of a civil service examination are divided into two groups; the first group is $30 \%$ and the remaining $70 \%$. Consider the first question of the examination among the first group, 40 had the correct answer. Whereas among the second group, 80 had the correct answer. On the basis of these results, can one conclude that the first question is not good at discriminating ability of the type being examined here. |  |  |  | Understand | CO 4 | AHSB12.20 |
| 17 | A cigarette manufacturing firm claims that brand A line of cigarettes outsells its brand B by $8 \%$.if it is found that 42 out of a sample of 200 smokers prefer brand A and 18 out of another sample of 100 smokers prefer brand B. Test whether $8 \%$ difference is a valid claim. |  |  |  | Understand | CO 4 | AHSB12.20 |
| 18 | If 48 out of 400 persons in rural area possessed 'cell' phones while 120 out of 500 in urban area. Can it be accepted that the proportion of 'cell' phones in the rural area and Urban area is same or not. Use 5\% of level of significance. |  |  |  | Understand | CO 4 | AHSB12.20 |
| 19 | Samples of student kilograms mean and test to the significan | drawn fr <br> differenc <br> Mean <br> 55 <br> 57 | universities and shown bel een means. | rom their weights in ake a large sample | Understand | CO 4 | AHSB12.19 |
| 20 | In a big city 325 men out of 600 men were found to be smokers. Does this information support the conclusion that the majority of men in this city are smokers? |  |  |  | Understand | CO 4 | AHSB12.20 |
| Part - C (Problem Solving and Critical Thinking) |  |  |  |  |  |  |  |
| 1 | Let $S=\{1,5,6,8\}$, find the probability distribution of the sample mean for random sample of size 2 drawn without replacement. Find <br> i) The mean of the population. <br> ii) The standard deviation of the population. <br> iii) The mean of the sampling distribution of means. |  |  |  | Understand | CO 4 | AHSB12.16 |


|  | iv) The standard deviation of the sampling distribution of means. |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| 2 | Samples of size 2 are taken from the population 1, 2, 3, 4, 5, 6. Which can be drawn without replacement? Find <br> i) The mean of the population. <br> ii) The standard deviation of the population. <br> iii) The mean of the sampling distribution of means. <br> iv) The standard deviation of the sampling distribution of means. | Understand | CO 4 | AHSB12.16 |
| 3 | A normal population has a mean of 0.1 and standard deviation of 2.1. Find the probability that mean of a sample of size 900 will be negative. | Understand | CO 4 | AHSB12.16 |
| 4 | A random sample of size 64 is taken from an infinite population having the mean 45 and the standard deviation 8 . What is the probability that x will be between 46 and 47.5. | Understand | CO 4 | AHSB12.16 |
| 5 | If a 1-gallon can of paint covers on an average 513 square feet with a standard deviation of 31.5 square feet, what is the probability that the mean area covered by a sample of 40 of these 1 -gallon cans will be anywhere from 510 to 520 square feet? | Understand | CO 4 | AHSB12.16 |
| 6 | A sample of 900 members has mean of 3.4 and S.D of 2.61 is this sample has been taken from a large population mean 3.25 and S.D 2.61. Also calculate $95 \%$ confidence interval. | Understand | CO 4 | AHSB12.19 |
| 7 | It is claimed that a random sample of 49 tyres has a mean life of 15200 kms this sample was taken from population whose mean is 15150 kms and S.D is 1200 km test 0.05 level of significant. | Understand | CO 4 | AHSB12.19 |
| 8 | A manufacturer claims that at least $95 \%$ of the equipment which he supplied to a factory conformed to specifications. An examination of sample of 200 pieces of equipments received 18 were faulty test the claim at 0.05 level. | Understand | CO 4 | AHSB12.20 |
| 9 | Among the items produced by a factory out of 500,15 were defective. In another sample of 400,20 were defective test the significant difference between two proportions at 5\% level. | Understand | CO 4 | AHSB12.20 |
| 10 | A manufacturer produced 20 defective articles in a batch of 400 . After overhauled it produced 10 defective in a batch of 300 has a machine being improved after over hauling. | Understand | CO 4 | AHSB12.20 |
| MODULE -V |  |  |  |  |
| TEST OF HYPOTHESIS - II |  |  |  |  |
| Part - A (Short Answer Questions) |  |  |  |  |
| 1 | If $\bar{x}=47.5, \mu=42.1, s=8.4, n=24$ then find t . | Understand | CO 5 | AHSB12.21 |
| 2 | Write a short note on Distinguish between t test for difference of means and F test. | Remember | CO 5 | AHSB12.22 |
| 3 | If $\bar{x}=40, \mu=25, s=8.4, n=24$ then find t . | Understand | CO 5 | AHSB 12.21 |
| 4 | What is the test statistic for t test for single mean? | Remember | CO 5 | AHSB12.21 |
| 5 | Define degree of freedom. | Remember | CO 5 | AHSB12.21 |
| 6 | What is the degree of freedom for F test? | Remember | CO 5 | AHSB12.22 |
| 7 | Find $\mathrm{F}_{0.05}$ with $(7,8)$ degrees of freedom. | Understand | CO 5 | AHSB12.22 |
| 8 | Find $\mathrm{t}_{0.05}$ when 16 degrees of freedom. | Understand | CO 5 | AHSB12.21 |
| 9 | A random sample of size 16 from a normal population. The mean of sample is 53 and sum of square of deviations from mean is 150 .can this sample is regarded as taken from the population having mean 56 at 0.05 level of significance. | Understand | CO 5 | AHSB12.21 |
| 10 | Find $\mathrm{F}_{0.95}$ with $(19,24)$ degrees of freedom. | Understand | CO 5 | AHSB12.22 |
| 11 | What is the test statistic for t test for difference of means? | Remember | CO 5 | AHSB12.21 |
| 12 | Find $\mathrm{t}_{0.99}$ when 7 degrees of freedom. | Understand | CO 5 | AHSB12.21 |
| 13 | What is the degree of freedom for $t$ test for difference of means? | Remember | CO 5 | AHSB12.21 |
| 14 | Find $\mathrm{t}_{0.95}$ when 9 degrees of freedom. | Understand | CO 5 | AHSB12.21 |
| 15 | What is the test statistic for F test? | Remember | CO 5 | AHSB12.22 |
| 16 | Find $\mathrm{F}_{0.99}$ with $(28,12)$ degrees of freedom. | Understand | CO 5 | AHSB12.22 |
| 17 | Write the formulae for sample variance and sample standard deviation. | Remember | CO 5 | AHSB12.21 |
| 18 | What is the degree of freedom for chi square test in case of contingency table of order $4 \times 3$ ? | Understand | CO 5 | AHSB12.23 |
| 19 | What is the test statistic for chi square test? | Remember | CO 5 | AHSB12.23 |
| 20 | Find $\chi_{0.05}^{2}$ at 9 degrees of freedom. | Understand | CO 5 | AHSB12.23 |





## Prepared by:

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