

# **INSTITUTE OF AERONAUTICAL ENGINEERING**

(Autonomous) Dundigal, Hyderabad-500043

## **CIVIL ENGINEERING**

## **TUTORIAL QUESTION BANK**

Course Title	THEOP	THEORY OF THIN PLATES AND SHELLS				
Course Code	BSTB03	3				
Programme	M.Tech	M.Tech				
Semester	Ι	STE				
Course Type	Elective	è				
Regulation	IARE - R18					
	Theory			Practical		
Course Structure	Lectur	res	Tutorials	Credits	Laboratory	Credits
	3		-	3	-	-
Chief Coordinator	Mr. Guo	le Ra	makrishna, Asso	ciate Professor		
Course Faculty	Mr. Gu	de Ra	amakrishna, Asso	ociate Professo	r	

#### **COURSE OBJECTIVES:**

The co	The course should enable the students to:			
Ι	Use analytical methods for the solution of thin plates and shells.			
II	Use analytical methods for the solution of shells.			
III	Apply the numerical techniques and tools for the complex problems in thin plates.			
IV	Apply the numerical techniques and tools for the complex problems in shells.			

## **COURSE OUTCOMES (COs):**

CO 1	Understand the concept of concepts of space curves, surfaces, shell co-ordinates, boundary				
	conditions.				
CO 2	Describe the governing equation for a rectangular plate, Navier solution for simply- supported				
	rectangular plate under various loadings, Levy solution for rectangular plate with other boundary				
	conditions.				
CO 3	Analyze under axi- symmetric loading, governing differential equation in polar co-ordinates.				
	Approximate methods of analysis- Rayleigh-Ritz approach for simple cases in rectangular plates.				
CO 4	Understand the membrane theory of cylindrical, conical and spherical shells.				
CO 5	Understand the cylindrical and conical shells, application to pipes and pressure vessels, thermal				
	stresses in plate/shell.				

## COURSE LEARNING OUTCOMES (CLO's):

BSTB03.01	Understand the concepts of space curves, surfaces, shell co-ordinates, boundary Conditions.
BSTB03.02	Understand the concept of displacement field approximations, stress resultants.
BSTB03.03	Determination of equation of equilibrium using principle of virtual work.
BSTB03.04	Understand the concept of bending of thin plates and assumptions.
BSTB03.05	Determination of Navier solution for simply- supported rectangular plate under various loadings.
BSTB03.06	Determination of deflection of uniformly loaded simply supported rectangular plate.
BSTB03.07	Solution of Navier and Levy type, large plate loaded at equidistant points by concentrated
	forces.
BSTB03.08	Understand basic relations in polar coordinates of circular plates.
BSTB03.09	Analyze the use of superposition for the axisymmetric analysis of circular plates.
BSTB03.10	Able to analyze the circular plates on elastic foundation, asymmetric bending of circular plates.
BSTB03.11	Analysis of Rayleigh-Ritz approach for simple cases in rectangular plates.
BSTB03.12	Analysis of membrane theory for cylindrical shells.
BSTB03.13	Understand the general theory in bending of cylindrical shell, simplified method for cylindrical shell.
BSTB03.14	Understand the simplified method for cylindrical shell.
BSTB03.15	Understand the thermal stresses in plate/shell.
BSTB03.16	Analyze shells of revolution under axisymmetric loads.
BSTB03.17	Able to analyze the axisymmetric loaded conical shells.
BSTB03.18	Able to analyze the axisymmetric deformation of toroidal shells.

## TUTORIAL QUESTION BANK

	UNIT-I				
	INTRODUCTION				
	Part – A (Short Answer Questio	ns)			
S.No	QUESTIONS	Blooms Taxonomy Level	Course Outcomes (CO's)	Course Learning Outcomes (CLOs)	
1	State the relations between bending moments and curvature in pure bending of plates?	Understand	CO 1	BSTB03.01	
2	Give a brief account of classifications of plates.	Remember	CO 1	BSTB03.01	
3	What are the assumptions in pure bending?	Remember	CO 1	BSTB03.01	
4	Derive the differential equations for plate subjected to ylindrical bending.	Understand	CO 1	BSTB03.01	
5	Distinguish between thin plate with small deflection and thin plate with large deflection.	Understand	CO 1	BSTB03.02	
6	What are the types of forces acting on the body explain with fig.	Remember	CO 1	BSTB03.02	
7	Give strain-displacement relation in the case of certain and cylindrical co-ordinate system?	Remember	CO 1	BSTB03.02	
8	What are the different kinds of plates, explain the boundary conditions for thin rectangular plate?	Understand	CO 1	BSTB03.02	
9	Explain any two types of rigidities in orthotropic plate with figure.	Remember	CO 1	BSTB03.02	
10	Give a formula for direction of maximum slope of bent plate.	Remember	CO 1	BSTB03.02	
	Part - B (Long Answer Questio	ns)			
1	Derive the differential equation governing the plate. Sate various assumptions involved in the derivation.	Understand	CO 1	BSTB03.02	

2	Using the Navier solution obtain general equation for a rectangular plate subjected to hydrostatic pressure	Remember	CO 1	BSTB03.02	
3	Derive the Navier solution for simply supported rectangular plates and obtain the maximum deflections.	Remember	CO 1	BSTB03.02	
4	Derive the differential equations of cylindrical bending of uniformly loaded rectangular plates will simply supported edges	Understand	CO 1	BSTB03.03	
5	Derive the differential equations of cylindrical bending of uniformly loaded rectangular plates with simply supported edges	Remember	CO 1	BSTB03.02	
6	Derive the differential equations of small deflections of laterally loaded plates (Lagrange's equations).	Understand	CO 1	BSTB03.02	
7	. Derive the differential equations of cylindrical bending of uniformly loaded rectangular plates with built in edges.	Remember	CO 1	BSTB03.02	
8	Obtain formulae for slope and curvature of a bent plate.	Remember	CO 1	BSTB03.02	
9	Obtain solution for plate problem by Ritz method in case of all round simply supported rectangular plate subjected to UDL?	Remember	CO 1	BSTB03.02	
10	Find Levy's solution for simply supported and uniformly loaded rectangular plates.	Remember	CO 1	BSTB03.03	
11	cylindrical bending of uniformly loaded rectangular plates with fixed edges.	Understand	CO 1	BSTB03.04	
12	Find displacement co-ordinates u, v in the case of Cartesian and cylindrical co-ordinate system, for strain displacement relation.	Understand	CO 1	BSTB03.04	
13	Derivation of cylindrical bending of uniformly loaded rectangular plate with fixed edges.	Understand	CO 1	BSTB03.04	
- 1	Part - C (Problem Solving and Critical Thi	nking Questions	S)	DOTED 02 01	
	A square plate with all four edges simply supported, carries a uniformly distributed load of intensity $q_0$ . Using levy's method, compute the maximum deflection & bending stress.	Remember	01	BS1B03.01	
2	Displacement co-ordinates u, v in the case of Cartesian and cylindrical co-ordinate system, for strain displacement relation	Understand	CO 1	BSTB03.02	
3	State and explain about boundary conditions for thin rectangular plate.	Remember	CO 1	BSTB03.02	
4	Deflection formulae for partially loaded simply supported rectangular plate, with fig.	Understand	CO 1	BSTB03.02	
5	Discuss briefly about Levy's solution of finding deflection of a rectangular plate.	Remember	CO 1	BSTB03.02	
6	Explain and state formulae for maximum and minimum bending stress for plates under sinusoidal load.	Understand	CO 1	BSTB03.02	
7	Find the transverse deflection w, radial moment Mr, tangential moment $M_Q$ and corresponding stresses and also find the Wmax subjected to UDL 'q'.	Remember for the simply su	CO 1 pported circu	BSTB03.02 lar plate	
8	Show that any point of the middle surface of the bent plate the sum of the curvature in two perpendicular directions is independent of the angle .	Understand	CO 1	BSTB03.02	
9	A square plate with all four edges simply supported, carries a uniformlydistributed load of intensity q0. Using levy's method, compute the maximum deflection & bending stress.	Remember	CO 1	BSTB03.02	
	UNIT – II	·		·	
	STATIC ANALYSIS OF PLA	TES			
	Part – A (Short Answer Questions)				

1	State the relations between bending moments and curvature in	Remember	CO 2	BSTB03.01
	pure bending of plates?		<u> </u>	DOTDOGOS
2	Give a brief account of classifications of plates.	Remember	<u>CO 2</u>	BSTB03.05
3	What are the assumptions in pure bending?	Remember	<u>CO 2</u>	BSTB03.05
4	Derive the differential equations for plate subjected to	Understand	CO 2	BSTB03.05
5	Distinguish between this plate with small deflection and this	Understand	CO 2	DSTD02.06
5	plate with large deflecti	Understand	02	<b>DS1D</b> 05.00
6	What are the types of forces acting on the body explain with	Remember	CO 2	BSTB03.06
Ũ	fig?	itemenioer	002	251203.00
7	Give strain-displacement relation in the case of certain and	Understand	CO 2	BSTB03.05
	cylindrical co-ordinate system?			
8	What are the different kinds of plates, explain the boundary	Remember	CO 2	BSTB03.05
	conditions for thin rectangular plate.			
9	Explain any two types of rigidities in orthotropic plate with	Remember	CO 2	BSTB03.05
	figure.			
	Part - B (Long Answer Quest	ions)		
1	Derive the differential equation governing the plate. Sate	Understand	CO 2	BSTB03.05
	various assumptions involved in the derivation.			
2	Using the Navier solution obtain general equation for a	Understand	CO 2	BSTB03.05
	rectangular plate subjected to hydrostatic pressure			
3	Derive the Navier solution for simply supported rectangular	Understand	CO 2	BSTB03.06
	plates and obtain the maximum deflections.			
4	Derive the differential equations of cylindrical bending of	Remember	CO 2	BSTB03.05
	uniformly loaded rectangular plates will simply supported			
	edges			
5	Derive the differential equations of cylindrical bending of	Remember	CO 2	BSTB03.05
	uniformly loaded rectangular plates with simply supported			
6	Derive the differential equations of small deflections of	Understand	<u> </u>	DCTD02.05
0	laterally loaded plates (Lagrange's equations)	Understand	02	<b>DS1D</b> 05.05
7	Derive the differential equations of cylindrical hending of	Remember	CO 2	BSTR03.06
,	uniformly loaded rectangular plates with built in edges	Remember	002	<b>D</b> 51 <b>D</b> 05.00
8	Obtain formulae for slope and curvature of a bent plate	Remember	CO 2	BSTB03.06
9	Obtain solution for plate problem by Ritz method in case of all	Remember	$CO^2$	BSTB03.06
	round simply supported rectangular plate subjected to UDL?	Remember	002	<b>D</b> 51 <b>D</b> 05.00
10	Find Levy's solution for simply supported and uniformly		CO 2	BSTB03.06
10	loaded rectangular plates		002	201200100
11	cylindrical bending of uniformly loaded rectangular plates	Remember	CO 2	BSTB0306
	with fixed edges	Remember	002	DBTD0500
12	Find displacement co-ordinates u. v in the case of Cartesian	Remember	CO 2	BSTB03.06
	and cylindrical co-ordinate system, for strain displacement			
	relation.			
13	Derivation of cylindrical bending of uniformly loaded	Remember	CO 2	BSTB03.06
	rectangular plate with fixed edges.			
	Part - C (Problem Solving and Critical Thi	nking Questions	s)	
1	A square plate with all four edges simply supported, carries a	Analyze	CO 2	BSTB03.07
	uniformly distributed load of intensity $q_0$ . Using levy's method,			
	compute the maximum deflection & bending stress.			
2	Displacement co-ordinates u, v in the case of Cartesian and	Remember	CO 2	BSTB03.07
	cylindrical co-ordinate system, for strain displacement relation			
3	State and explain about boundary conditions for thin	Remember	CO 2	BSTB03.07
	rectangular plate.	-		
4	Deflection formulae for partially loaded simply supported	Evaluate	CO 2	BSTB03.08

	rectangular plate, with fig.			
5	Discuss briefly about Levy's solution of finding deflection of a	Remember	CO 2	BSTB03.08
	rectangular plate			
6	Explain and state formulae for maximum and minimum	Analyze	CO 2	BSTB03.08
	bending stress for plates under sinusoidal load			
7	Find the transverse deflection w, radial moment Mr, tangential	Remember	CO 2	BSTB03.08
	moment M <sub>Q</sub> and corresponding stresses and also find the			
	Wmax for the circular plates of the following type.			
	• A simply supported plate subjected to UDL 'q'.			
8	Show that any point of the middle surface of the bent plate	Evaluate	CO 2	BSTB03.08
	the sum of the curvature in two perpendicular directions is			
	independent of the angle.			
9	A square plate with all four edges simply supported, carries	Analyze	CO 2	BSTB03.08
	a uniformly distributed load of intensity q0. Using levy's			
	method, compute the maximum deflection & bending stress.			
	UNIT – III			
	CIRCULAR PLATES			
1	Part - A (Short Answer Question	ons)	<u> </u>	
	I ne maximum deflection at the center of the plate with	Remember	CO 3	BS1B03.09
2	uniformly loaded circular plate.	D	<u> </u>	DCTD02.00
2	Deflection of circular plate with supported edges	Remember	CO 3	BS1B03.09
3	Determine the deflection and internal moments of simply	Understand	CO 3	BS1B03.09
4	Supported rectangular support plate of size a x b.	Domomhon	<u> </u>	DSTD02.00
4	briefly explain an expression for maximum deflection at the	Remember	003	DS1D03.09
	centre of a simply supported plate concreted toad at the center.			
5	Write down slope and deflection of circular plate with clamped	Understand	CO 3	BSTB03.09
5	edge when $r=0$ and $r=a$	Onderstand	005	DS1D03.09
	cuge, when 1–0 and 1–a.			
6	Find maximum deflection at the center of the plate for	Remember	CO 3	BSTB03.09
Ŭ	uniformly loaded circular plate.	remember	605	<b>DD1D03</b> .0 <b>9</b>
7	Find maximum deflection at the center of the plate for	Understand	CO 3	BSTB03.09
	uniformly loaded circular plate.			
8	Find deflection and bending moments for circular plate loaded	Remember	CO 3	BSTB03.09
	at center.			
9	Deflection produced by the moment in case of circular plate	Remember	CO 3	BSTB03.09
	concentrically loaded.			
	Part – B (Long Answer Quest	tions)		
1	Derive expressions for deflection, shear force and bending	Remember	CO 3	BSTB03.10
	moment for a circular plate with simply supported boundary			
	conditions subjected to uniformly distributed loading.			
2	Derive the moment curvature relationship in the case of pure	Understand	CO 3	BSTB03.10
	bending of plates.			
3	A simply supported rectangular plate of dimension a x b x h is	Understand	CO 3	BSTB03.10
	subjected to load 'P' acting over an area. Derive the			
<u> </u>	expression for deflection. Adopt Navier's approach.			Dampacit
4	Derive the equations of equilibrium for small deflections of	Understand	CO 3	BSTB03.10
	Interally loaded plates.	TT. 1. · ·	00.1	
5	Find Levy's solution for simply supported rectangular plates.	Understand	03	B21B0310
				1
6	Obtain the expression for deflection in case of uniformly	Remember	CO 3	BSTB03.10
	loaded circular plates with clamped edges.			
/	Expression for slope and deflection for circular plate with a	Understand	CO 3	BSTB03.10

8	Obtain differential equation for symmetrical bending of	Understand	CO 3	BSTB03.10		
	laterally loaded circular plate.					
9	Derive an expression for deflection of simply supported solid circular plate subjected to an end moments	Understand	CO 3	BSTB03.10		
	Part - C (Problem Solving and Critical Thi	nking Question	18)			
1	Briefly explain an expression for maximum deflection at the	Understand	CO 3	BSTB03.11		
	centre of a simply supported plate concreted load at the cente	Charlound	000	201200111		
2	Explain correction to the elementary theory of symmetrical	Understand	CO 3	BSTB03.11		
	bending of circular plates					
3	Obtain the expression for deflection in case of uniformly	Understand	CO 3	BSTB03.11		
	loaded circular plates with clamped edges.					
4	Obtain the expression for deflection in case of uniformly	Remember	CO 3	BSTB03.11		
	loaded circular plates with clamped edges.					
5	Determine the deflection and internal moments of simply	Remember	CO 3	BSTB03.11		
	supported rectangular support plate of size a x b.					
	A material la solution of the first second state the solution	Denverter	CO 1	DCTD02 11		
0	A rectangular plate a x b simply supported at the edges is	Remember	CO 3	B\$1B03.11		
	subjected to sinusoidal loading. Using the Navier solution,					
	moment					
7	Find the deflection equation for a plate subjected to hydro.	Remember	CO 3	BSTB03 11		
/	static pressure use Levy's basic equation for calculating	Remember	005	<b>D</b> 51D05.11		
	deflection					
8	Determine the deflection and internal moments of simply	Remember	CO 3	BSTB03.11		
0	supported rectangular support plate of size a x b.	1.0	000	201200111		
9	A uniform loaded solid circular plate with radius 'a ' has its	Remember	CO 3	BSTB03.12		
-	edges simply supported obtain the expressions for the					
	maximum deflection and obtain bending moment.					
	UNIT - IV					
	STATIC ANALYSIS OF SHELLS: MEMBRAN	E THEORY O	FSHELLS			
	Part – A (Short Answer Ques	tions				
1	Differentiate between long shells and short shells.	Remember	CO 4	BSTB03.12		
2	Explain the bending and membrane theories for analysis of shells.	Remember	CO 4	BSTB03.12		
3	Briefly explain about the classification of shells.	Remember	CO 4	BSTB03.12		
4	Explain about the various types of shells with neat sketches.	Remember	CO 4	BSTB03.12		
5	Explain about the advantages and disadvantages of the shells.	Remember	CO 4	BSTB03.13		
6	Explain about beam analysis.	Remember	CO 4	BSTB03.13		
7	Explain the bending and membrane theories for analysis of	Remember	CO 4	BSTB03.13		
	shells					
8	Derive the membrane equation for shells.	Remember	CO 4	BSTB03.13		
9	Explain about the bending theory of shells	Remember	CO 4	BSTB03.13		
10	Explain about the advantages and disadvantages of the shells.	Remember	CO 4	BSTB03.13		
	Part - B (Long Answer Quest	ions)	<b>GO</b> 4	DOTE: 00 10		
1	Derive Shorer's differential equation	Understand	<u>CO 4</u>	BSTB03.13		
2	Write boundary conditions for simply supported cylindrical	Understand	CO 4	BSTB03.13		
	snells with the edge					
	i) single shell with edge beam					
2	If single shell will cuge use in a market of the market of	Understand	CO 4	BSTR03 12		
3	analysis of shells of double curvature	Understand	0.04	0.10		
1	Derive the membrane stress resultants for rectangular	Understand	CO 4	BSTB03 13		
-	hyperbolic paraboloid on straight line generators.	Chaoistand	00 1	251205.15		
5	Derive the equilibrium equation of rectangular shell.	Understand	CO 4	BSTB03.13		

6	Derive the membrane differential equation for the elliptic paraboloid	Understand	CO 4	BSTB03.13
7	Derive the membrane differential equation for the rotational paraboloid	Understand	CO 4	BSTB03.13
8	Explain about membrane theory of anticlastic shells	Understand	CO 4	BSTB03.14
	Part - C (Problem Solving and Critical Thi	nking Question	ns)	
1	Derive the equilibrium equation of rectangular shell.	Remember	CO 4	BSTB03.14
2	Derive the general equations for axisymmetric shells of	Remember	CO 4	BSTB03.14
_	revolution.			
3	Define the membrane state of stress in shells. Derive equations of equilibrium, using membrane theory for cylindrical shell and obtain Mx, Mq&Mxq.	Remember	CO 4	BSTB03.14
4	Explain the following a) Membrane behavior b) Membrane equation	Remember	CO 4	BSTB03.14
5	Explain about membrane theory of anticlastic shells	Remember	CO 4	BSTB03 1/
5	Find the equations of equilibrium in case of shells in the form	Understand	CO 4	BSTB03.14
0	of a surface of revolution and loaded symmetrically with respect to their axis.	Understand	0.4	D51D03.14
7	<ul><li>(a) Differentiate between long shells and short shells.</li><li>(b) Explain about the advantages and disadvantages of the shells.</li></ul>	Understand	CO 4	BSTB03.15
8	Write a short note on	Understand	CO 4	BSTB03.15
Ť	a) Anti-symmetric shells			
	b) Singly curved shells			
	c) ISI classification of shells			
9	a) How do you classify shells into long and short shells as per	Understand	CO 4	BSTB03.15
	various theories			
	b) Write boundary conditions for simply supported cylindrical			
	shells with the edge conditions.			
	i) Single shell without edge beam			
	ii) single shell with edge beam			
10	Define the membrane state of stress in shells. Derive equations	Understand	CO 4	BSTB03.15
	of equilibrium, using membrane theory for cylindrical shell.			
		DIG DEGIGE	NCE	
	SHELLS OF REVOLUTION: WITH BEND	ING RESISTA	ANCE	
1	Part - A (Short Answer Quest	lons)	<u> </u>	DGTD02.15
1	Derive geometrical relations for shells of double curvature.	Remember	<u> </u>	BS1B03.15
2	Explain about Anti-symmetric shells	Remember Democratier		DS1BU3.13
5	Derive the equilibrium equation of rectangular shell.	Remember	CO 5	BS1B03.10
4	Briefly explain about the types of shells.	Remember		BS1B03.16
5	Drieny explain about the classification of shells.	Remember	CO 5	BS1B03.10
6	Explain about the bending theory of shells	Remember	CO 5	BS1B03.16
7	Differentiate between long shells and short shells.	Remember		BS1B03.16
8	Explain about membrane theory of anticlastic shells	Remember	05	BSTB03.16
	Part - B (Long Answer Quest	ions)	<u> </u>	DCCD20.16
1	a) Anti-symmetric shells b) Singly curved shells	Understand	0.5	BCSB28.16
2	Explain about the bending theory of shells.	Understand	CO 5	BSTB03.16
3	Derive the general equations for axisymmetric shells of revolution.	Understand	CO 5	BSTB03.16
4	Derive the membrane stress resultants for rectangular	Understand	CO 5	BSTB03.17
	hyperbolic paraboloid on straight line generators.			
5	Explain about membrane theory of anticlastic shells	Understand	CO 5	BSTB03.17

6	Derive the general equations for axisymmetric shells of revolution.	Understand	CO 5	BSTB03.17
7	Explain about membrane theory of anticlastic shells	Understand	CO 5	BSTB03.17
8	Explain about cylindrical bending of uniformly loaded rectangular plates with fixed edges	Understand	CO 5	BSTB03.17
9	Write assumptions made in general theory of thin elastic shells.	Understand	CO 5	BSTB03.17
	Part - C (Problem Solving and Critical Thi	nking Questio	ns)	
1	Derive the membrane differential equation for the rotational paraboloid	Understand	CO 5	BSTB03.17
2	Derive geometrical relations for shells of double curvature	Understand	CO 5	BSTB03.18
3	Derive the governing differential equation for the membrane analysis of shells of double curvature.	Understand	CO 5	BSTB03.18
4	Derive the membrane stress resultants for rectangular hyperbolic paraboloid on straight line generators.	Understand	CO 5	BSTB03.18
5	Derive the membrane differential equation for the rotational paraboloid.	Remember	CO 5	BSTB03.18
6	Write a short note on a) Anti-symmetric shells b) Singly curved shells c) ISI classification of shells	Remember	CO 5	BSTB03.18
7	Derive the moment curvature in the case of pure bending of plates	Remember	CO 5	BSTB03.18
8	State the assumptions in shorer's theory of cylindrical shells and drive the shorer's differential equation.	Remember	CO 5	BSTB03.18
9	Classify thin shell into various types based on shell geometry & curvature.	Remember	CO 5	BSTB03.18

Prepared by:

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