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Question Paper Code No: AHSB06



INSTITUTE OF AERONAUTICAL ENGINEERING

(Autonomous)

Dundigal, Hyderabad - 500 043

MODEL QUESTION PAPER-II

B. Tech IV Semester End Examinations (Regular), May-2020

Regulation: IARE-R18

COMPLEX ANALYSIS AND PROBABILITY DISTRIBUTIONS

(EEE)

Time: 3 hours

Max. Marks: 70

Answer ONE Question from each Module

All Questions Carry Equal Marks

All parts of the question must be answered in one place only

MODULE-1

- Define the term Analyticity of a complex variable function $f(z)$. Examine the complex variable function $f(z) = z^3$ to analyticity for all values of z in Cartesian form [7M]
 - Show that real part $u = x^3 - 3xy^2$ of an analytic function $f(z)$ is harmonic. Hence find the conjugate harmonic function and the analytic function. [7M]
- Define the term Analyticity and Differentiability of a complex function $f(z)$. Prove that an analytic function with constant imaginary part is always constant. [7M]
 - Examine the complex variable function $f(z) = \frac{x-iy}{x^2+y^2}$ for analyticity in Cartesian form. [7M]

MODULE-2

- State Cauchy's integral theorem for multiple connected region. Examine the value of $\int_c e^{-z} dz$ with $C: |z-1| = 1$ by Cauchy integral formulae [7M]
 - Verify Cauchy's theorem for the function $f(z) = 5 \sin 2z$ if c is the square with vertices at $1 \pm i$ and $-1 \pm i$. [7M]
- Define the term Line integral. Estimate the value of line integral to $\int_{z=0}^{z=1+i} [x^2 + 2xy + i(y^2 - z)] dz$ along the curve $y = x^2$. [7M]
 - Determine the value of line integral to $\int_c \frac{e^{2z}}{(z-1)(z-2)} dz$ where c is the circle $|z|=3$ using Cauchy's integral formula. [7M]

MODULE-3

5. (a) State Laurent's theorem of complex power series. Define the residue of a function by Laurent series expansion [7M]
- (b) Estimate the Residues of the function $f(z) = \frac{1}{(z - \sin z)}$ about $z = 0$ by Laurent's expansion. [7M]
6. (a) State Residue formulae for simple pole and pole of nth order. [7M]
- (b) Expand $f(z) = \frac{1}{z^2}$ in powers of $z+1$ as a Taylor's series. [7M]

MODULE-4

- 7 (a) Define continuous probability distributions and mass function, density function of a probability distribution. [7M]
- (b) The probability density function of a random variable x is $f(x) = e^{-x/2}$, $x > 0$. Estimate the value of the probability of $1 < x < 2$. [7M]
8. (a) Define Central moments, Moment generating function of probability distribution. [7M]
- (b) Let X be the random variable of the following values $x=1,2,3$ if $f(x) = x/6$. Then find mean and variance. [7M]

MODULE-5

9. (a) Describe about the Poisson distributions and their properties [7M]
- (b) Out of 20 tape recorders 5 are defective. Find the standard deviation of defective in the sample of 10 randomly chosen tape recorders. Find (i) $P(X=0)$ (ii) $P(X=3)$ (iii) $P(X=5)$ (iv) $P(2 < X < 4)$. [7M]
- 10 (a) Describe about properties of Normal distribution [7M]
- (b) The marks obtained in Statistics in a certain examination found to be normally distributed. If 15% of the students greater than or equal to 60 marks, 40% less than 30 marks. Find the mean and standard deviation. [7M]



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COURSE OBJECTIVES:

The course should enable the students to:

I	Understand the basic theory of complex functions to express the power series.
II	Evaluate the contour integration using Cauchy residue theorem.
III	Enrich the knowledge of probability on single random variables and probability distributions.

COURSE OUTCOMES (COs):

CO 1	Discuss about continuity/differentiability/analyticity of a Complex function using Cauchy-Riemann Equations. Estimate complex conjugate using Milne Thomson method and understand the concept of Bilinear transformation.
CO 2	Recognize and apply the Cauchy's integral formula and the generalized Cauchy's integral formula. Evaluate complex functions as power series and radius of convergence of power series
CO 3	Establish the contour integral with an integrand which has singularities lying inside or outside the simple closed contour. Expand complex function as power series using Taylor's and Laurent series..
CO 4	Enrich the knowledge of Probability to discrete and continuous random variables.
CO 5	Analyze probability distributions for Binomial, Poisson and normal distributions and study its properties.

COURSE LEARNING OUTCOMES (CLOs):

AHSB06.01	Recall continuity, differentiability, analyticity of a function using limits.
AHSB06.02	Interpret the conditions for a complex variable to be analytic and/or entire function.
AHSB06.03	Interpret the concepts of Cauchy-Riemann relations and harmonic functions.
AHSB06.04	Analyze the Bilinear transformation by cross ratio property.
AHSB06.05	Identify the conditions of fixed and critical point of Bilinear Transformation.
AHSB06.06	Demonstrate the area under a curve using the concepts of indefinite integration.
AHSB06.07	Interpret the concepts of the Cauchy's integral formula and the generalized Cauchy's integral formula.
AHSB06.08	Demonstrate complex functions as power series and radius of convergence of power series.
AHSB06.09	Interpret the concept of complex integration to the real-world problems of flow with circulation around a cylinder.
AHSB06.10	Asses the Taylor's and Laurent series expansion of complex functions.
AHSB06.11	Interpret the concept of different types of singularities for analytic function.
AHSB06.12	Identify the poles, residues and solve integrals using Cauchy's residue theorem.
AHSB06.13	Interpret the concept of Cauchy's residue theorem to the real-world problems of Quantum Mechanical scattering and Quantum theory of atomic collisions.

AHSB06.14	Demonstrate an understanding of the basic concepts of probability and random variables.
AHSB06.15	Classify the types of random variables and calculate mean, variance.
AHSB06.16	Estimate moment about origin, central moments, moment generating function of probability distribution.
AHSB06.17	Recognize where the Binomial distribution could be appropriate model of the distributions.
AHSB06.18	Recognize where the Poisson distribution could be appropriate model of the distributions.
AHSB06.19	Recognize where the Binomial distribution and Poisson distribution could be appropriate to find mean, variance of the distributions.
AHSB06.20	Apply the inferential methods relating to the means of normal distributions.
AHSB06.21	Interpret Binomial distribution to the phenomena of real-world problem like sick versus healthy.
AHSB06.22	Identify the mapping of Normal distribution in real-world problem to analyze the stock market.
AHSB06.23	Use Poisson distribution in real-world problem to predict soccer scores.
AHSB06.24	Possess the knowledge and skills for employability and to succeed in national and international level competitive examinations.

MAPPING OF SEMESTER END EXAMINATIONS TO COURSE LEARNING OUTCOMES:

SEE Question No.	CLO Code	Course learning Outcomes	CO	Blooms Taxonomy Level
1	a	AHSB06.01 Recall continuity, differentiability, analyticity of a function using limits.	CO 1	Remember
	b	AHSB06.02 Interpret the conditions for a complex variable to be analytic and/or entire function.	CO 1	Understand
2	a	AHSB06.01 Recall continuity, differentiability, analyticity of a function using limits.	CO 1	Remember
	b	AHSB06.03 Interpret the concepts of Cauchy-Riemann relations and harmonic functions.	CO 1	Understand
3	a	AHSB06.07 Interpret the concepts of the Cauchy's ntegral formula and the generalized Cauchy's integral formula.	CO 2	Remember
	b	AHSB06.06 Demonstrate the area under a curve using the concepts of indefinite integration.	CO 2	Understand
4	a	AHSB06.06 Demonstrate the area under a curve using the concepts of indefinite integration.	CO 2	Remember
	b	AHSB06.07 Interpret the concepts of the Cauchy's ntegral formula and the generalized Cauchy's integral formula.	CO 2	Understand
5	a	AHSB06.10 Asses the Taylor's and Laurent series expansion of complex functions.	CO 3	Remember
	b	AHSB06.10 Asses the Taylor's and Laurent series expansion of complex functions.	CO 3	Understand
6	a	AHSB06.11 Interpret the concept of different types of singularities for analytic function.	CO 3	Remember
	b	AHSB06.12 Identify the poles, residues and solve integrals using Cauchy's residue theorem.	CO 3	Understand

SEE Question No.	CLO Code	Course learning Outcomes	CO	Blooms Taxonomy Level	
7	a	AHSB06.14	Demonstrate an understanding of the basic concepts of probability and random variables.	CO 4	Remember
	b	AHSB06.15	Classify the types of random variables and calculate mean, variance.	CO 4	Understand
8	a	AHSB06.16	Estimate moment about origin, central moments, moment generating function of probability distribution.	CO 4	Remember
	b	AHSB06.16	Classify the types of random variables and calculate mean, variance.	CO 4	Understand
9	a	AHSB06.17	Recognize where the binomial distribution and Poisson distribution could be appropriate model and find mean, variance of the distributions.	CO 5	Remember
	b	AHSB06.17	Recognize where the binomial distribution and Poisson distribution could be appropriate model and find mean, variance of the distributions.	CO 5	Understand
10	a	AHSB06.20	Apply the inferential methods relating to the means of normal distributions.	CO 5	Remember
	b	AHSB06.20	Apply the inferential methods relating to the means of normal distributions.	CO 5	Understand

Signature of Course Coordinator

HOD, EEE