



INSTITUTE OF AERONAUTICAL ENGINEERING

Dundigal, Hyderabad - 500 043

INFORMATION TECHNOLOGY

TUTORIAL QUESTION BANK

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|--------------------|---|-----------|------------|---------|
| Course Title | DISCRETE MATHEMATICAL STRUCTURES | | | |
| Course Code | AHS013 | | | |
| Regulation | R16 | | | |
| Course Structure | Lectures | Tutorials | Practicals | Credits |
| | 3.. | 1 | - | 4 |
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OBJECTIVES

To meet the challenge of ensuring excellence in engineering education, the issue of quality needs to be addressed, debated and taken forward in a systematic manner. Accreditation is the principal means of quality assurance in higher education. The major emphasis of accreditation process is to measure the outcomes of the program that is being accredited.

In line with this, Faculty of Institute of Aeronautical Engineering, Hyderabad has taken a lead in incorporating philosophy of outcome based education in the process of problem solving and career development. So, all students of the institute should understand the depth and approach of course to be taught through this question bank, which will enhance learner's learning process.

| S. No | Question | Blooms Taxonomy Level | Course Outcome |
|--|--|-----------------------|----------------|
| UNIT – I | | | |
| Mathematical Logic and Predicates | | | |
| PART - A (Short Answer Questions) | | | |
| 1 | Define statement and atomic statement? | Knowledge | 1 |
| 2 | Explain logical equivalence with an example? | Understand | 2 |
| 3 | Describe the tautology? | Understand | 2 |
| 4 | Remember the converse, inverse and contra positive of the following propositions: $P \rightarrow (Q \rightarrow R)$ | Remember | 1 |
| 5 | Interpret that $P \vee [P \wedge (P \vee Q)]$ and P is a logically equivalent without using truth table ? | Remember | 2 |
| 6 | Explain $P \uparrow Q$ in terms of " \downarrow " ? | Understand | 1 |
| 7 | Define predicate and predicate logic? | Knowledge | 2 |
| 8 | Define contradiction and provide a proof by contradiction of the following statements for every integer 'n' ,if n^2 is odd then 'n' is odd. | Knowledge | 2 |
| 9 | Define converse, contra positive and inverse of implication? | Knowledge | 1 |
| 10 | Analyze and symbolize the following statements: a) all men are good b) no men are good | Analyze | 1 |
| 11 | Examine the disjunctive normal form of the formula: $P \leftrightarrow Q$? | Knowledge | 2 |
| 12 | Describe the value of: $P \leftrightarrow Q$ in terms of $\{\sim, \vee\}$ only ? | Understand | 1 |

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| 13 | Explain about the free and bound variables? | Understand | 2 |
| 14 | Illustrate that if 'm' is an even integer then $m+7$ is an odd integer? | Remember | 2 |
| 15 | Demonstrate the truth table for conjunction and conditional statements? | Understand | 1 |
| 16 | Construct the truth table for $p \rightarrow (q \rightarrow r)$? | Remember | 1 |
| 17 | Show that $\sim(p \rightarrow q) \rightarrow p$? | Remember | 2 |
| 18 | Construct the statements R: Mark is rich. H: Mark is happy write the following statements in symbolic form a) mark is poor but happy b) mark is poor but happy | Remember | 2 |
| 19 | Construct the following statement in symbolic form: "the crop will be destroyed if there is a flood". | Remember | 1 |
| 20 | Show that $R \rightarrow S$ can be derived from the premises $P \rightarrow (Q \rightarrow S)$, $\sim R \vee P$ and Q | Remember | 1 |

PART-B (Long Answer Questions)

| | | | |
|----|--|------------|---|
| 1 | a) Explain conditional proposition with a suitable example. b) Explain logical equivalence with an example. | Understand | 1 |
| 2 | (a) Define tautology? Show that $[(p \rightarrow q) \rightarrow r] \rightarrow [(p \rightarrow q) \rightarrow (p \rightarrow r)]$ is a tautology or not ? (b) Define the converse, inverse and contra positive of the following propositions: i. $P \rightarrow (Q \rightarrow R)$ ii. $(P \wedge (P \rightarrow Q)) \rightarrow Q$. | Knowledge | 2 |
| 3 | Show that $S \vee R$ is a tautologically implied by $(p \vee q) \wedge (p \rightarrow r) \wedge (q \rightarrow s)$ With reference to automatic theorem proving. | Remember | 2 |
| 4 | Show that RVS is valid conclusion from the premises: $CVD, (C \vee D) \rightarrow \sim H, \sim H \rightarrow (A \wedge \sim B), (A \wedge \sim B) \rightarrow RVS$ | Remember | 1 |
| 5 | Show that i) $\sim(P \uparrow Q) \leftrightarrow \sim P \downarrow \sim Q$ ii) $\sim(P \downarrow Q) \leftrightarrow \sim P \uparrow \sim Q$ without using truth table ? Express $p \rightarrow (\sim p \rightarrow q)$ i) in terms of ' \uparrow ' only ii) in terms of ' \downarrow ' | Remember | 1 |
| 6 | (a) Describe the proposition $(p \wedge q) \sim (p \vee q)$ is a contradiction. (b) Symbolize the following statements: all men are good no men are good some men are good some men are not good | Understand | 2 |
| 7 | (a) Construct the disjunctive normal form of the formula: $P \leftrightarrow Q$? (b) Construct the value of: $P \leftrightarrow Q$ in terms of $\{\sim, \vee\}$ only ? | Remember | 2 |
| 8 | Explain about the free and bound variables. With an examples? | Understand | 1 |
| 9 | Show that if 'm' is an even integer then $m+7$ is an odd integer? ii) write each of the following in symbolic form a) all monkeys have tails b) no monkey have tail c) some monkey have tails d) some monkey have no tails | Remember | 2 |
| 10 | Construct tautology? Show that $[(p \rightarrow q) \rightarrow r] \rightarrow [(p \rightarrow q) \rightarrow (p \rightarrow r)]$ is a tautology or not ? | Remember | 1 |

PART-C (Analytical Questions)

| | | | |
|---|--|----------|---|
| 1 | Construct the negations of the following statements, a) Jan will take a job in industry or go to graduate school b) James will bicycle or run tomorrow c) If the processor is fast then the printer is slow | Remember | 1 |
| 2 | Construct the pdnf of $(p \wedge q) \vee (\sim p \vee r) \vee (q \vee r)$ using truth table. | Remember | 2 |
| 3 | Show that: a) $R \wedge (P \vee Q)$ is a valid conclusion from premises $P \vee Q$, $Q \rightarrow R$, $P \rightarrow M$ and $\sim M$. b) Show that: $R \rightarrow S$ can be derived from the premises, $P \rightarrow (Q \rightarrow S)$, $\sim R \vee P$ and Q | Remember | 2 |

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| 4 | Show that the following premises are inconsistent. (a) If jack misses many classes through illness, then he fails high school (b) If jack fails high school, then he is uneducated. (c) If jack reads lot of books, then he is not uneducated.. (d) Jack misses many classes through illness and lot of books | Remember | 1 |
| 5 | Select p,q and r be the propositions P: you have the flee Q: you miss the final examination R: you pass the course. Write the following propositions into statement form. (i) $p \rightarrow q$ (ii) $\sim p \rightarrow r$ (iii) $q \rightarrow \sim r$ (iv) $p \vee q \vee r$ (v) $(p \rightarrow \sim v) \vee (q \rightarrow \sim r)$ (vi) $(p \wedge q) \vee (\sim q \wedge r)$. | Knowledge | 2 |

UNIT – II
Relations, Functions and Lattices

PART - A (Short Answer Questions)

| | | | |
|----|---|------------|---|
| 1 | Describe a relation? | Understand | 4 |
| 2 | Illustrate the operations on relations? | Remember | 5 |
| 3 | Define Reflexive relation? | Knowledge | 5 |
| 4 | Define Symmetric relation? | Knowledge | 5 |
| 5 | Define Transitive relation? | Knowledge | 5 |
| 6 | Define Indegree and Outdegree for diagraph | Knowledge | 5 |
| 7 | Define bounded lattice and distributive lattice? | Knowledge | 5 |
| 8 | Explain is a partial order relation? | Understand | 3 |
| 9 | Construct the Hasse diagram represented with positive divisors of 36? | Remember | 3 |
| 10 | Define a) onto function b) one to one function | Knowledge | 4 |
| 11 | Define bijective function? | Knowledge | 4 |
| 12 | Explain constant function? | Understand | 4 |
| 13 | Define Identity function? | Knowledge | 4 |
| 14 | Define Inverse function? | Knowledge | 4 |
| 15 | If $A = \{1,2,3\}$, $B = \{4,5\}$. Find $A \times B$ and $B \times A$? | Knowledge | 4 |
| 16 | Prove that $A - (B \cap C) = (A - B) \cup (A - C)$? | Remember | 4 |
| 17 | Define lattice ? If A is finite set and P(A) is power set then prove that $(P(A), \subseteq)$ is a lattice for i) $A = \{a\}$ | Knowledge | 4 |
| 18 | Describe the properties of lattice? | Understand | 5 |
| 19 | Show that the function $f(x) = x^3$ and $g(x) = x^{1/3}$ for $x \in \mathbb{R}$ are inverse of each other ? | Remember | 3 |
| 20 | Solve the functions $f: A \rightarrow B, g: B \rightarrow C, h: C \rightarrow D$, then prove that $h \circ (g \circ f) = (h \circ g) \circ f$? | Remember | 4 |
| 21 | Show that $(g \circ f)^{-1} = f^{-1} \circ g^{-1}$ where f and g are one to one, onto functions. | Remember | 5 |
| 22 | Design the Hasse diagram of $(P(S), \subseteq)$, where P(S) is power set of the set $S = \{a, b, c\}$? | Create | 2 |
| 23 | Let R be the Relation $R = \{(x,y) / x \text{ divides } y\}$. Design the Hasse diagram? | Create | 2 |
| 24 | Let R be the Relation $R = \{(x,y) / x \text{ is a factor of } y\}$. Design the Hasse diagram? | Create | 2 |

PART-B (Long Answer Questions)

| | | | |
|---|--|-----------|---|
| 1 | Define a relation? Explain the properties of relations and the operations on relations? | Knowledge | 3 |
| 2 | Define the transitive closure of relation $R = \{(a,a) (a,b) (a,d) (b,a) (c,b) (a,c) (d,b) (d,c) (d,d)\}$ by using warshal algorithm? | Knowledge | 4 |

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| 3 | Construct the hasse diagram for the divisibility relation i) $A = \{3, 6, 12, 36, 72\}$ ii) $A = \{1, 2, 3, 5, 6, 10, 15, 30\}$ | Remember | 5 |
| 4 | Define lattice ? If A is finite set and P(A) is Power set then prove that $(P(A), \leq)$ is a lattice for i) $A = \{a\}$ ii) $A = \{a, b\}$ | Knowledge | 4 |
| 5 | Define bounded lattice and distributive lattice? What is a partial order relations? | Knowledge | 5 |
| 6 | Describe the sets A & B given that $A - B = \{1, 2, 4\}$ $B - A = \{7, 8\}$ and $A \cup B = \{1, 2, 4, 5, 7, 8, 9\}$. | Knowledge | 4 |
| 7 | Solve that, Let A be a given finite set and p(θ) its power set. let \leq be the inclusion relation on the elements p(θ) draw the hasse diagram of (p(A), \leq) i) $A = \{a\}$ ii) $B = \{a, b\}$ iii) $C = \{a, b, c\}$ iv) $D = \{a, b, c, d\}$ | Remember | 5 |
| 8 | Construct the hasse diagram represented with positive divisors of 36? | Remember | 5 |
| 9 | Describe the function and find the inverse of the function i) $f(x) = 10/5\sqrt{7-3x}$ ii) $4e^{(6x+2)}$ | Understand | 5 |
| 10 | Describe a) onto function b) one to one function c) bijective function d) constant function | Understand | 4 |

PART-C (Analytical Questions)

| | | | |
|----|--|------------|---|
| 1. | Describe a bijective function. Explain with reasons whether the following functions are bijective or not. Find also the inverse of each of the functions. (i) $f(x) = 4x+2$, A = set of real numbers (ii) $f(x) = 3+1/x$, A = set of non- zero real numbers (iii) $f(x) = (2x+3) \bmod 7$, $A = \mathbb{N}_7$ | Understand | 6 |
| 2. | Consider sets $A = \{a, b, c\}$ $B = \{1, 2, 3\}$, $R = \{(a, 1), (b, 1), (c, 2), (c, 3)\}$ and $s = \{(a, 1), (a, 2), (b, 1), (b, 2)\}$ from A to B. Determine (i) \overline{R} (ii) \overline{S} (iii) $R \cup S$ (iv) $R \cap S$ (v) R^c (vi) S^c | Understand | 3 |
| 3. | Let $A = \{1, 2, 3, 4, 6, 12\}$ on set A define the relation A to B, iff A divides B.. Prove that R is partial order relation and draw the Hasse diagram form this relation. | Remember | 4 |
| 4. | a) Let the Relation R be $R = \{(2, 1), (3, 2), (3, 3)\}$ on the set $A = \{1, 2, 3\}$. What is the Transitive Closure of R? b) Explain in brief about Inversive and Recursive functions with examples? | Understand | 3 |
| 5. | How many relations are there on a set with 'n' elements? If a set A has 'm' elements and a set B has 'n' elements, how many relations are there from A to B? If a set $A = \{1, 2\}$, determine all relations from A to A. | Understand | 5 |
| 6. | a) A function $f: Z \times Z \rightarrow Z$ is defined by $f(x, y) = 4x - 5y$. Prove that f is not one-to-one, but on to? b) Let $f(x): x^2 - 3x + 2$. Find $f(x^2)$ and $f(x+3)$? | Understand | 5 |

UNIT – III

ALGEBRAIC STRUCTURES AND COMBINATORICS

PART - A (Short Answer Questions)

CIE-I

| | | | |
|----|---|------------|---|
| 1 | Define group and semi group? | Knowledge | 5 |
| 2 | Define monoid and sub group? | Knowledge | 4 |
| 3 | Define homomorphism? | Knowledge | 4 |
| 4 | Define isomorphism? | Knowledge | 5 |
| 5 | Illustrate if a, b are elements of M and $a*b=b*a$, then | Remember | 5 |
| 6 | Explain whether the given table with respect to operation * on the set | Understand | 3 |
| 7 | Solve that, Let $(G,*)$ be a group and let $a, b \in G$, then $(a^{-1})^{-1}=a$ | Remember | 4 |
| 8 | Describe sum rule and product rule? | Understand | 6 |
| 9 | Describe , the co-efficient of $a^2b^3c^3d^5$ in the expansion of $(a+2b-3c+2d+5)^{16}$? | Knowledge | 6 |
| 10 | Let G be a group. Show that $\phi : G \rightarrow G$ defined by $\phi(g) = g^{-1}$ is an isomorphism if and only if G is Abelian. | Remember | 5 |
| 11 | Let G be a group with $ G = pq$, where p, q are primes. Prove that every proper subgroup of G is cyclic. But the whole group may not be cyclic. | Evaluate | 6 |
| 12 | Let G be a group of order p^2 for a prime p. Show that G is cyclic or $g^p = e$ for all $g \in G$. | Remember | 5 |
| 13 | Can a group of order 55 have exactly 20 elements of order 11? Illustrate a reason for your answer | Remember | 5 |
| 14 | Let R_1 and R_2 be rings, and $\phi : R_1 \rightarrow R_2$ be a ring homomorphism. Show that if A is an ideal of R_1 , then $\phi(A)$ is an ideal of $\phi(R_1)$. | Remember | 6 |
| 15 | Let R_1 and R_2 be rings, and $\phi : R_1 \rightarrow R_2$ be a ring homomorphism. Give an example to show that $\phi(A)$ may not be an ideal of R_2 . | Remember | |
| 16 | Let R_1 and R_2 be rings, and $\phi : R_1 \rightarrow R_2$ be a ring homomorphism such that $\phi(R) \neq \{0\}$. Show that if R_1 has unity and R_2 has no zero-divisors, then $\phi(1)$ is a unity of R_2 . | Remember | 6 |

CIE-II

| | | | |
|----|---|------------|---|
| 1 | Illustrate the no of ways we can select the counting rules from the class Which having 6 boys and 5 girls | Remember | 6 |
| 2 | Solve that, if a person having 4 trousers and 3 shirts then find the no of ways of selecting a pair? | Remember | 7 |
| 3 | Solve that, the no of ways of forming three digit number from 5 elements? | Remember | 6 |
| 4 | Solve that, the no of ways of selecting 9 committees with 7 | Remember | 6 |
| 5 | Solve that, the no of ways forming a 4 letter word from the word MIXTURE in which at least one letter is repeated? | Remember | 6 |
| 6 | Explain pigeon-hole principle? | Understand | 6 |
| 7 | Prove that if there are 8 cars and 26 passengers at least one car has 4 or more passengers? | Evaluate | 6 |
| 8 | A library contains 30 books whose total number of pages is 2560. Show that one of the books must have at least 86 pages? | Remember | 7 |
| 9 | Describe how many words of three distinct letters can be formed from the letters of the word MAST? | Knowledge | 7 |
| 10 | Describe , that in how many different outcomes are possible by tossing 10 similar coins? | Knowledge | 7 |
| 11 | Describe , that in how many different 8 digit numbers can be formed by arranged digits 1, 1,1,1,2,3,3,3. | Knowledge | 6 |
| 12 | Describe , that in how many numbers can be formed using the digits 1, 3, 4,5,6,8 and 9 if no repetitions are allowed? | Knowledge | 7 |
| 13 | Describe , that in how many ways are there to seat 10 boys and 10 girls around a circular table, if boys and girls seat alternatively? | Knowledge | 6 |
| 14 | Describe , that in how many ways can the digits 0,1,2,3,4,5,6,7,8,and 9 be arranged so that 0 and 1 are adjacent and in the order of 01? | Knowledge | 7 |

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| 15 | Describe that in how many ways two slices of pizza can be chosen from a plate containing one slice each of pepperoni, sausage, mushroom, and cheese pizza? | Knowledge | 7 |
| 16 | Describe , that in how many five letter passwords can be generated using first three letters as any of the English alphabets and last two being any digit from 0 to 9 ?(repetition is allowed) | Knowledge | 6 |

PART-B (Long Answer Questions)

CIE-I

| | | | |
|---|---|------------|---|
| 1 | Explain sum rule and product rule? | Understand | 7 |
| 2 | Solve the co-efficient of x, y, z^2 in the expansion of $(2x-y-z)^4$ using multinomial theorem ? | Remember | 7 |
| 3 | Construct the co-efficient of x, y, z^2 in the expansion of $(2x-y-z)^4$ using multinomial theorem ? | Remember | 7 |
| 4 | Construct the co-efficient of $a^2b^3c^3d^5$ in the expansion of $(a+2b-3c+2d+5)^{16}$? | Remember | 6 |
| 5 | Show that inclusion-exclusion principle? I) $n(T_1 \cup T_2) = n(T_1) + n(T_2) - n(T_1 \cap T_2)$? | Remember | 7 |

CIE-II

| | | | |
|----|--|-----------|---|
| 1 | Solve that the no of ways we can select the counting rules from the class which having 6 boys and 5 girls? | Remember | 6 |
| 2 | Solve , if a person having 4 trousers and 3 shirts then find the no of ways of selecting a pair? | Remember | 7 |
| 3 | Illustrate the following a) the person has four transport modems for a travelling from(hyd to Chennai) and three transport modems travelling from(Chennai to Bangalore) then find the no of ways of the person travelling from (hyd-bangalore) via Chennai b) expand inclusion-exclusion principle ? | Remember | 7 |
| 4 | a) Solve that the no of ways of forming three digit number from 5 elements? | Remember | 6 |
| 5 | Solve that the no of ways of arranging 5 boys and 4 girls in a line and the line can start with boy and end with boy also? | Remember | 7 |
| 6 | Solve that the no of ways of forming committee of 5 persons from a group of 5 indians 4 russians such that three are at least 3 Indians | Remember | 6 |
| 7 | Solve that the no of ways forming a 4 letter word from the word MIXTURE in which at least one letter is repeated? | Remember | 6 |
| 8 | Solve that in How many ways we can distribute 12 identical pencils to 4 children such that every children get at least one pencil? | Remember | 6 |
| 9 | Define pigeon hole principle? in a group of 13 children there must be least two children who were born in the same month? | Knowledge | 6 |
| 10 | i) Describe that if 8 cars 26 passengers at least one car has 4 or more passengers? ii)A library contain 30 books whose total no of pages are 2560 show that one of the book must have at least 86 pages? | Knowledge | 7 |

PART-C (Analytical Questions)

CIE-I

| | | | |
|---|---|----------|---|
| 1 | Solve whether the following algebraic systems satisfy the properties under binary operations * and + (a) Odd integers (b) All the positive integers. | Remember | 7 |
| 2 | Solve that $(Z, *)$ is an abelian group where Z is a set of integers and the binary operations * is defined as $a*b = a+b-3$ | Remember | 7 |
| 3 | Show that in a group $(G, *)$ for every $a, b \in G$ $(a*b)^2 = a^2*b^2$ if $(G, *)$ is an abelian. | Remember | 6 |

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| 4 | Show that If $A = \{1, -1, i, -i\}$ are the fourth roots of unity. Show that $(A, *)$ forms a group. | Remember | 7 |
| 5 | Explain The set, S , of all ordered pairs (a, b) of real numbers for which $a \neq 0$ w.r.t the operation $*$ defined by $(a, b) * (c, d) = (ac, bc + d)$ is a group. Find, The identity of (G, o) and a) Inverse of each element of G | Understand | 6 |
| 6 | Explain If $A = \{a_1, a_2, \dots, a_5\}$ $B = \{b_1, b_2, \dots, b_5\}$ find whether $(A, *)$, (B, o) for the given composition tables are groups . If, no give the | Understand | 6 |

CIE-II

| | | | |
|---|---|------------|----|
| 1 | Select the number of rows of 6 Americans, 7 Mexicans and 10 Canadians in which an American invariably stands between a Mexican and a Canadian never stand side by side. | Knowledge | 10 |
| 2 | Solve the words. (a) TALLAHASSEE (b) MISSISSIPPI How many arrangements can be made such that, (i) No two letters A of TALLAHASSEE appear together (ii) Number of 4 letter words for both the given words. | Remember | 10 |
| 3 | Select in How many integers between 1 and 10^4 contain exactly one 8 and one 9. | Knowledge | 10 |
| 4 | Select in How many integers between 10^5 and 10^6 , (i) Have no digit other than 2, 5 or 8 (ii) Have no digit other than 0, 2, 5 or 8. | Knowledge | 10 |
| 5 | Select in How many arrangements are there for the word 'MISSISSIPPI' with no two pair of consecutive same letters? | Knowledge | 10 |
| 6 | Describe , in how many ways we can distribute 12 identical pencils to 4 children such that every children get at least one pencil? | Understand | 7 |

UNIT – IV Recurrence Relation

PART - A (Short Answer Questions)

| | | | |
|----|---|----------|---|
| 1 | Solve the generating functions for the following sequences 1, 2, 3, 4 | Remember | 9 |
| 2 | Solve the generating functions for the following sequences 1, -2, 3, -4 | Remember | 8 |
| 3 | Solve the generating functions for the following sequences 0, 1, 2, 3 | Remember | 8 |
| 4 | Solve the generating functions for the following sequences 0, 1, -2, 3, -4 | Remember | 8 |
| 5 | Solve the co-efficient of x^{12} of $x^3(1-2x)^{10}$? | Remember | 7 |
| 6 | Solve the co-efficient of x^5 of $(1-2x)^{-7}$? | Remember | 8 |
| 7 | Solve the co-efficient of x^{27} of $(x^4 + x^5 + x^6 \dots \dots \dots)^5$ | Remember | 9 |
| 8 | Solve the generating functions for the following sequences $1^2, 2^2, 3^2, \dots \dots \dots$ | Remember | 8 |
| 9 | Solve the generating functions for the following sequences $0^2, 1^2, 2^2, 3^2, \dots \dots \dots$ | Remember | 9 |
| 10 | Solve the co-efficient of x^{27} of $(x^4 + 2x^5 + 3x^6 \dots \dots \dots)^5$ | Remember | 9 |
| 11 | Solve the generating functions for the following sequences $1^3, 2^3, 3^3, \dots \dots \dots$ | Remember | 8 |
| 12 | Solve the recurrence relation $a_n = a_{n-1} + n^3, n \geq 1$ where $a_0 = 5$ by using substitution method ? | Remember | 8 |
| 13 | Solve the recurrence relation $a_n = a_{n-1} + 3n^2 + 3n + 1, n \geq 1$ where $a_0 = 5$ by using substitution method ? | Remember | 9 |
| 14 | Solve the generating functions for the following sequences $0^2, 1^3, 2^3, 3^3, \dots \dots \dots$ | Remember | 8 |
| 15 | Solve the recurrence relation $a_{n+1} = 8a_n, n \geq 0$ where $a_0 = 4$ | Remember | 9 |
| 16 | Solve the recurrence relation $a_{n+1} = 8a_n, n \geq 0$ where $a_0 = 6$ | Remember | 9 |

| | | | |
|----|--|----------|---|
| 17 | Solve the generating functions for the following sequences 1,1,0,1,1,1 | Remember | 9 |
| 18 | Solve the co-efficient of x^{27} of $(x^4+x^5+x^6+\dots)^5$ | Remember | 8 |
| 19 | Solve recurrence relation $a_n=a_{n-1}+n^3$, $n \geq 1$ where $a_0=5$ by using substitution method ? | Remember | 9 |
| 20 | Solve recurrence relation $a_n=a_{n-1}+n$, $n \geq 1$ where $a_0=2$ by using substitution method ? | Remember | 9 |

PART-B (Long Answer Questions)

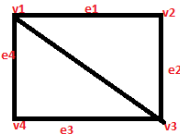
| | | | |
|----|--|-----------|----|
| 1 | Identify the generating functions for the following sequences i)1,2,3,4 ii)1,-2,3,-4 iii)0,1,2,3 iv)0,1,-2,3,-4 | Knowledge | 8 |
| 2 | Identify the generating function for the following sequence i)1 ² ,2 ² ,3 ² ,----- ii)0 ² ,1 ² ,2 ² ,3 ² ,----- | Knowledge | 9 |
| 3 | Identify the generating function for the following sequence i)1 ³ ,2 ³ ,3 ³ ,-----ii)0 ² ,1 ³ ,2 ³ ,3 ³ ,----- | Knowledge | 9 |
| 4 | Identify the generating function for the following sequence 1,1,0,1,1,1 | Knowledge | 8 |
| 5 | Identify the co-efficient of x^{12} of $x^3(1-2x)^{10}$? | Knowledge | 8 |
| 6 | Identify the co-efficient of x^5 of $(1-2x)^{-7}$? | Knowledge | 9 |
| 7 | Identify the co-efficient of x^{27} of i) $(x^4+x^5+x^6+\dots)^5$ ii) $(x^4+2x^5+3x^6+\dots)^5$ | Knowledge | 8 |
| 8 | Solve the recurrence relation $a_n=a_{n-1}+n^3$, $n \geq 1$ where $a_0=5$ by using substitution method ? | Remember | 9 |
| 9 | Solve the recurrence relation $a_n=a_{n-1}+3n^2+3n+1$, $n \geq 1$ where $a_0=5$ by using substitution method ? | Remember | 8 |
| 10 | Solve the recurrence relation $a_{n+1}=8a_n$, $n \geq 0$ where $a_0=4$ | Remember | 9 |
| 11 | Solve the recurrence relation $a_n-7a_{n-1}+10a_{n-2}=0$, $n \geq 2$, $a_0=10$, $a_1=41$ | Remember | 8 |
| 12 | Solve the recurrence relation $a_n-9a_{n-1}+26a_{n-2}+24a_{n-3}=0$, $n \geq 3$, $a_0=0$, $a_1=1$, $a_2=10$ | Remember | 9 |
| 13 | Solve the recurrence relation $a_n=3a_{n-1}+2n$, $a_1=3$ | Remember | 8 |
| 14 | Solve the recurrence relation $a_n-3a_{n-1}=n$, $n \geq 1$, $a_0=1$ by using generating function ? | Remember | 9 |
| 15 | Solve the recurrence relation $a_{n+1}-a_n=3^n$, $n \geq 0$, $a_0=1$ by using generating function ? | Remember | 11 |

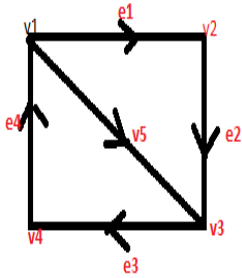
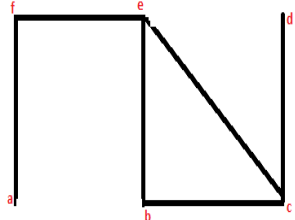
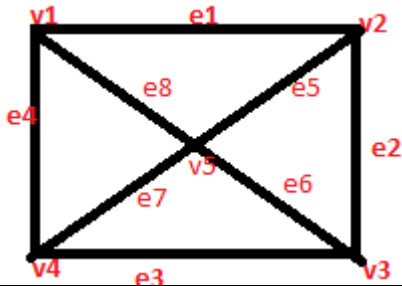
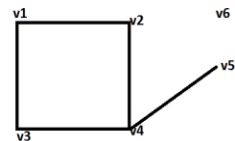
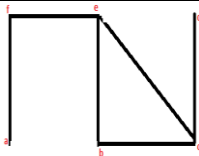
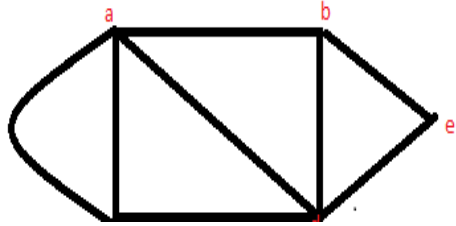
PART-C (Analytical Questions)

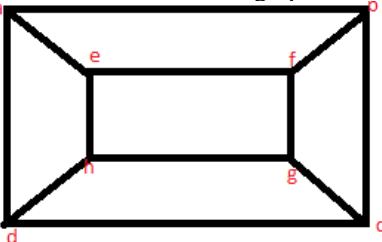
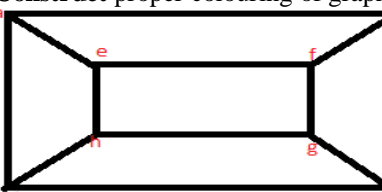
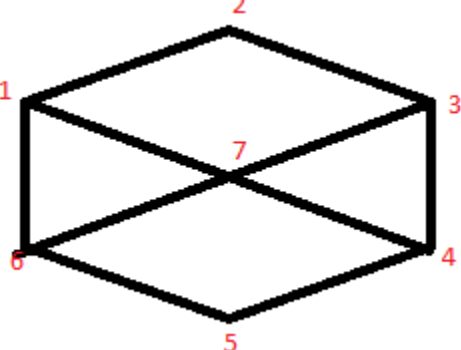
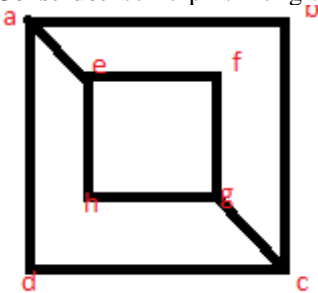
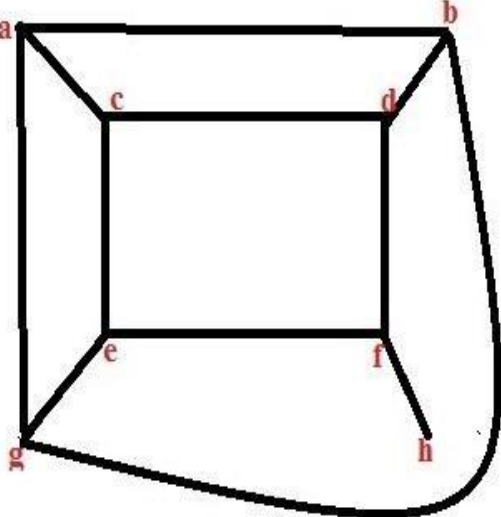
| | | | |
|---|--|----------|----|
| 1 | Solve the recurrence relation $a_n-3a_{n-1}=n$, $n \geq 1$, $a_0=1$ by using generating function ? | Remember | 12 |
| 2 | Solve the recurrence relation $a_{n+1}-a_n=3^n$, $n \geq 0$, $a_0=1$ by using generating function ? | Remember | 12 |
| 3 | Solve the recurrence relation $a_{n+2}-2a_{n+1}+a_n=2^n$, $n \geq 0$, $a_0=1$, $a_1=2$ using generating function ? | Remember | 11 |
| 4 | Solve the co-efficient of x^{27} of i) $(x^4+x^5+x^6+\dots)^5$ ii) $(x^4+2x^5+3x^6+\dots)^5$ | Remember | 11 |

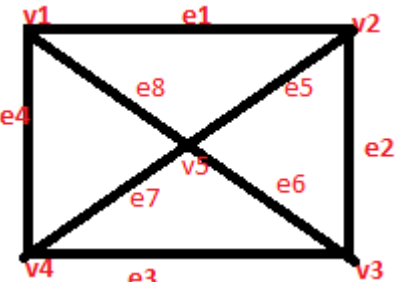
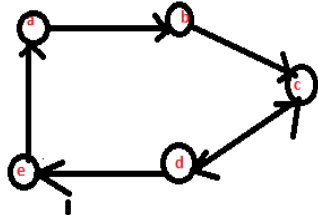
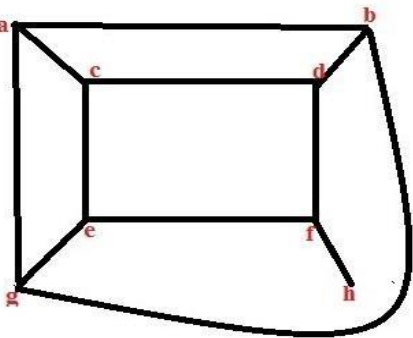
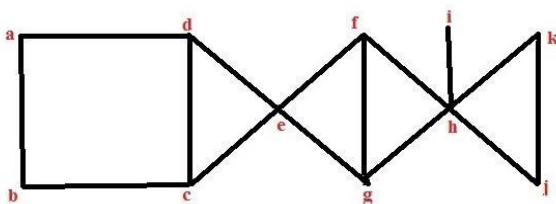
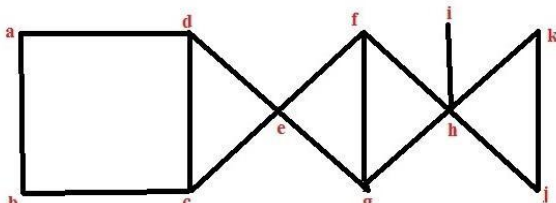
UNIT – V Graphs and Trees

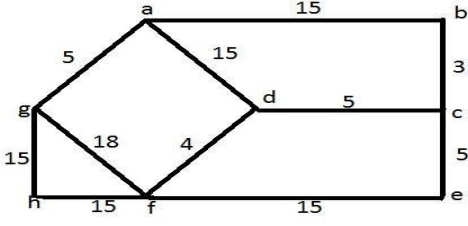
PART - A (Short Answer Questions)

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| 1 |  <p>Define graph? Write the matrix representation of the above graph.</p> | Knowledge | 11 |
|---|---|-----------|----|

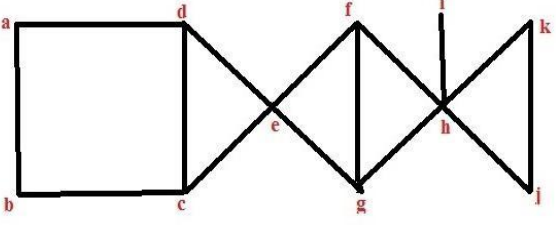
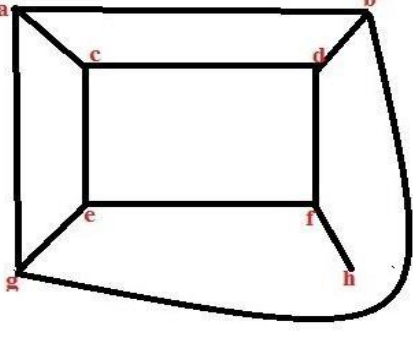
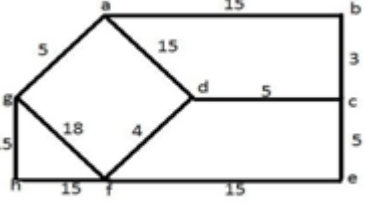
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| 2 | Define tree and spanning tree? | Knowledge | 10 |
| 3 | Illustrate the adjacency matrix of directed graph?  | Remember | 10 |
| 4 | Describe the spanning trees of graph?  | Understand | 11 |
| 5 | Describe simple graph AND degree of each vertex?  | Understand | 10 |
| 6 | Define i. Null graph? ii. Isolated vertex? | Knowledge | 11 |
| 7 | Define i) pendent vertex ii) self-loop  What are the pendent vertexes in the above graph? | Knowledge | 10 |
| 8 |  Define order, size AND regular graph? | Knowledge | 1 1 |
| 9 | Define complete graph? | Knowledge | 1 |
| 10 | Construct eulerian graph? And write eulerian path  | Remember | 1 1 |

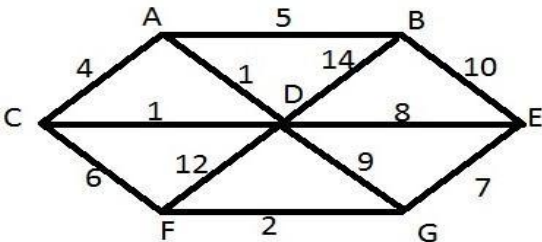
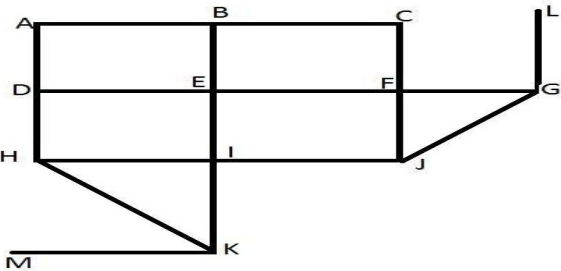
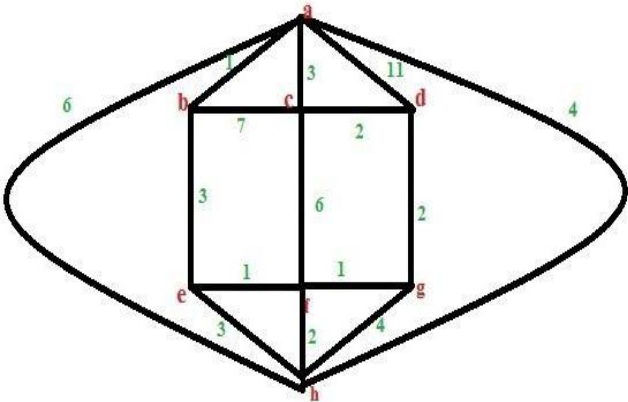
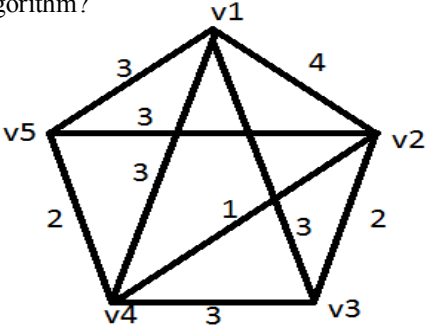
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|--------|--|----------|--------|
| 1 1 | Construct Hamiltonian graph?  | Remember | 1 0 |
| 1 2 | Construct proper colouring of graph?  Assign the proper coloring in the above graph? | Remember | 1 2 |
| 1 3 | Construct chromatic number of graph?  | Remember | 1 2 |
| 1 4 | Construct isomorphism of graph?  | Remember | 1 2 |
| 1 | Construct multigraph? | Remember | 1 |
| 1 6 | Construct an algorithm of breadth first search?  | Remember | 12 |

| | | | |
|---------------------------------------|---|------------|--------|
| 1 7 | Construct planar graph? Count the orders and sizes of that graph?  | Remember | 11 |
| 1 | Illustrate the matrix representation of graph? | Remember | 12 |
| 1 | Illustrate the incidence matrix of graph? | Remember | 11 |
| 2 0 | Describe the linked list representation of graph?  | Knowledge | 12 |
| 2 | Construct depth first search algorithm? | Remember | 13 |
| PART-B (Long Answer Questions) | | | |
| 1. | Examine graph? explain i) matrix representation ii) incidence matrix iii) linked list representation of graph? | Knowledge | 12 |
| 2. | Examine tree and spanning tree, find all spanning trees of  | Knowledge | 1 2 |
| 3. | Discuss Breadth first search algorithm with an example?  | Understand | 1 2 |
| 4. | Discuss depth first search algorithm? Explain with an example?  | Understand | 1 2 |
| 5. | Discuss prim's algorithm with an example? | Understand | 1 |

| | | | |
|-----|---|------------|----|
| 6. | Discuss krushkal's algorithm with an example?  | Understand | 12 |
| 7. | Name graph and explain eulerian graph? Name graph and explain Euler path and Euler circuit? | Knowledge | 12 |
| 8. | Enumerate Hamiltonian graph? Define proper colouring and define chromatic number? | Knowledge | 12 |
| 9. | Enumerate isomorphism and explain with an example? Define multigraph? | Knowledge | 12 |
| 10. | Enumerate a)graph b)simple graph c)degree of vertex d)null graph | | |

PART-C (Analytical Questions)

| | | | |
|---|---|----------|----|
| 1 |  Construct the spanning tree of graph G by using i) BFS ii)DFS | Remember | 10 |
| 2 | Construct the spanning tree of graph G by using BFS  | Remember | 12 |
| 3 | Construct the minimal cost spanning tree for the cities shown in above graph using Kruskal's algorithm?  | Remember | 12 |

| | | | |
|---|---|----------|----|
| 4 |  <p>Construct the minimal cost spanning tree for the cities shown in above graph using Prim's algorithm?</p> | Remember | 12 |
| 5 |  <p>Construct the spanning tree of the graph G by using DFS with vertex in the ordering "abcfjihdegl"?</p> | Remember | 12 |
| 6 |  <p>Construct the minimal cost spanning tree for the cities shown in above graph using Kruskal's algorithm?</p> | Remember | 12 |
| | <p>Construct the minimal spanning tree of weighted graph G by using Prim's algorithm?</p>  | Remember | 12 |

Prepared by : Mrs B.Pravallika, Assistant Professor

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