



INSTITUTE OF AERONAUTICAL ENGINEERING

(Autonomous)

Dundigal, Hyderabad - 500 043

AERONAUTICAL ENGINEERING

TUTORIAL QUESTION BANK

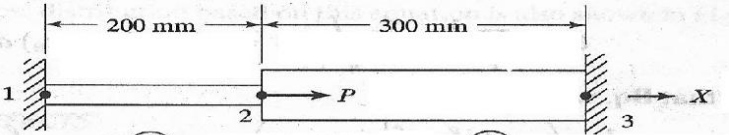
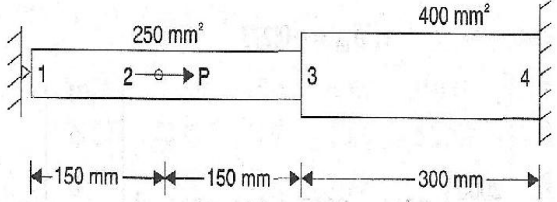
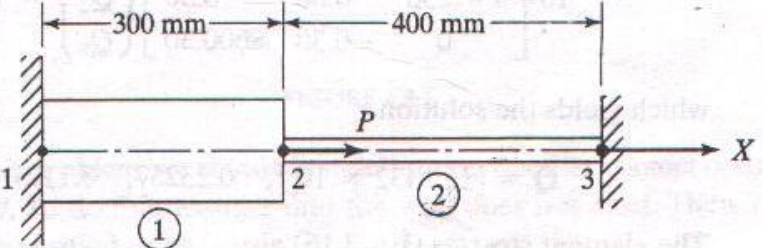
Course Name	:	FINITE ELEMENT METHODS
Course Code	:	A60330
Class	:	III - II
Branch	:	AERONAUTICAL ENGINEERING
Year	:	2017– 2018
Team of Instructors	:	Ms Y Shwetha, Asst. Professor. Department of Aeronautical Engineering Mr. G. S. D Madhav, Asst. Professor, Department of Aeronautical Engineering

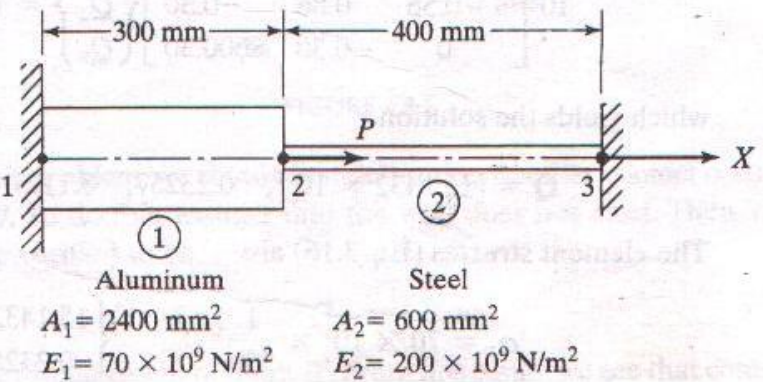
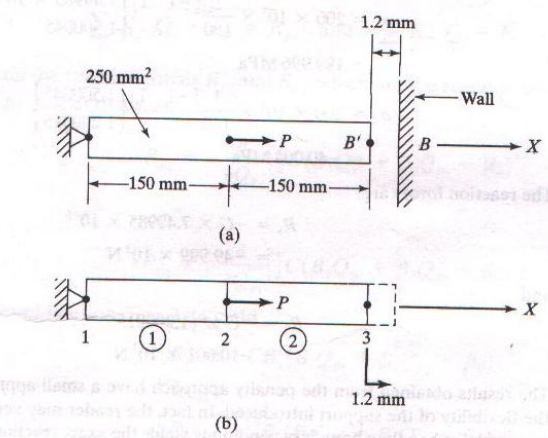
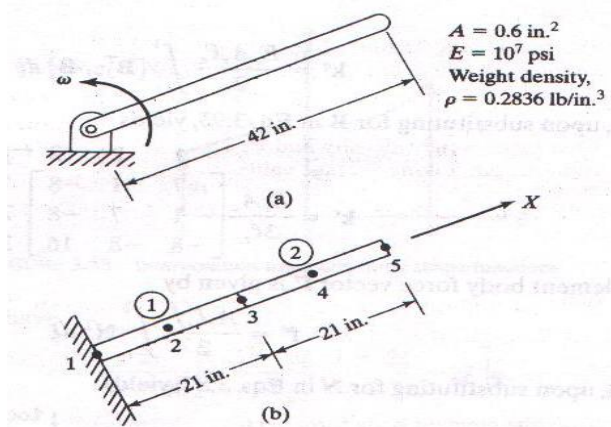
OBJECTIVES:

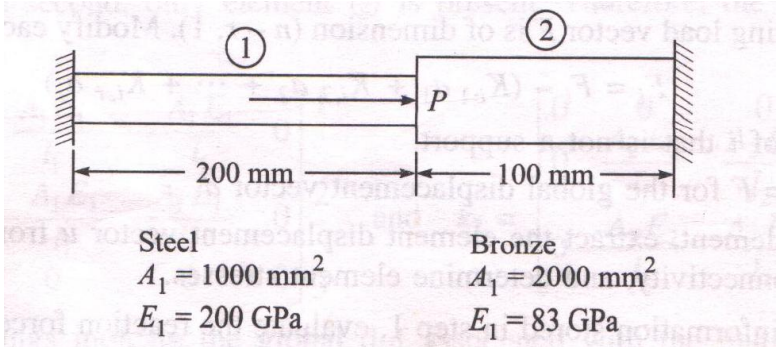
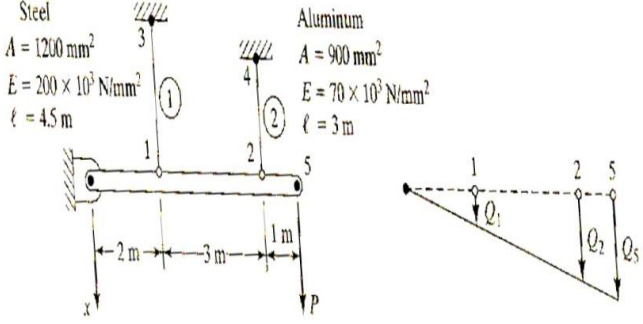
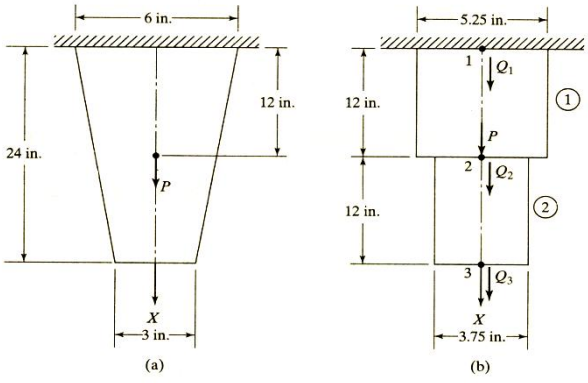
To meet the challenge of ensuring excellence in engineering education, the issue of quality needs to be addressed, debated and taken forward in a systematic manner. Accreditation is the principal means of quality assurance in higher education. The major emphasis of accreditation process is to measure the outcomes of the program that is being accredited.

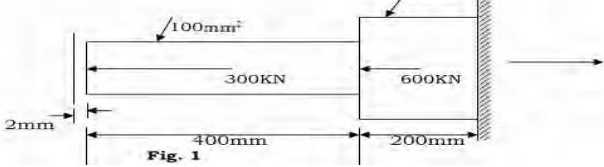
In line with this, Faculty of Institute of Aeronautical Engineering, Hyderabad has taken a lead in incorporating philosophy of outcome based education in the process of problem solving and career development. So, all students of the institute should understand the depth and approach of course to be taught through this question bank, which will enhance learner's learning process.

S. No.	Question	Blooms Taxonomy Level	Course Outcomes
UNIT-I			
INTRODUCTION			
Part A -Short Answer Questions			
1	Explain finite element method.	Remember	1
2	Define degree of freedom.	Remember	1
3	Define boundary condition.	Understand	1
4	What is local and global stiffness matrix?	Remember	1
5	What is the unit of stiffness?	Understand	1
6	What is global force vector?	Understand	1
7	What is the governing equation of F.E.M?	Remember	1
8	Define potential energy.	Understand	1
9	Define strain energy.	Remember	1
10	Give the expression for total potential energy.	Remember	1
11	Give the expression for shape functions of a linear element.	Remember	1
12	Draw the shape functions of a linear element.	Remember	1
13	Write the expression for the shape functions of a quadratic element.	Understand	1
14	Draw the shape functions of a quadratic element.	Understand	1
15	What is natural boundary condition?	Remember	1
Part B - Long Answer Questions			
1	Using variational approach (potential energy), describe FE formulation for 1D bar element.	Understand	1,3

2	Using potential energy approach, describe FE formulation for plane truss Element.	Remember	1,2								
3	Define principle of virtual work. Describe the FEM formulation for 1D bar element.	Remember	1,3								
4	Explain the concept of FEM briefly and outline the steps involved in FEM along with Understands.	Understand	1,4								
5	Describe the elimination approach, with an example.	Understand	1								
6	Discuss in detail about the concepts of FEM formulation .How is that FEM emerged as a powerful tool.	Understand	2,4								
7	Discuss in detail about Understands of finite element method	Remember	3,1								
8	Derive element stiffness matrix and load vector for quadratic element using potential energy approach.	Understand	1								
9	Explain the concept of FEM briefly .outline the steps involved in FEM along with Understands.	Understand	2,3								
10	Draw the shape functions of a quadratic element.	Remember	1								
11	<p>An axial load $P=300 \times 10^3 \text{ N}$ is applied at 20° C to the rod as shown in Figure below. The temperature is raised to 60° C .</p> <p>a) Assemble the K and F matrices. b) Determine the nodal displacements and stresses.</p>  <p style="text-align: center;">FIGURE</p> <table style="width: 100%; border: none;"> <tr> <td style="text-align: center;">① Aluminum</td> <td style="text-align: center;">② Steel</td> </tr> <tr> <td style="text-align: center;">$E_1 = 70 \times 10^9 \text{ N/m}^2$</td> <td style="text-align: center;">$E_2 = 200 \times 10^9 \text{ N/m}^2$</td> </tr> <tr> <td style="text-align: center;">$A_1 = 900 \text{ mm}^2$</td> <td style="text-align: center;">$A_2 = 1200 \text{ mm}^2$</td> </tr> <tr> <td style="text-align: center;">$\alpha_1 = 23 \times 10^{-6} \text{ per } ^\circ \text{C}$</td> <td style="text-align: center;">$\alpha_2 = 11.7 \times 10^{-6} \text{ per } ^\circ \text{C}$</td> </tr> </table>	① Aluminum	② Steel	$E_1 = 70 \times 10^9 \text{ N/m}^2$	$E_2 = 200 \times 10^9 \text{ N/m}^2$	$A_1 = 900 \text{ mm}^2$	$A_2 = 1200 \text{ mm}^2$	$\alpha_1 = 23 \times 10^{-6} \text{ per } ^\circ \text{C}$	$\alpha_2 = 11.7 \times 10^{-6} \text{ per } ^\circ \text{C}$	Remember	1,4
① Aluminum	② Steel										
$E_1 = 70 \times 10^9 \text{ N/m}^2$	$E_2 = 200 \times 10^9 \text{ N/m}^2$										
$A_1 = 900 \text{ mm}^2$	$A_2 = 1200 \text{ mm}^2$										
$\alpha_1 = 23 \times 10^{-6} \text{ per } ^\circ \text{C}$	$\alpha_2 = 11.7 \times 10^{-6} \text{ per } ^\circ \text{C}$										
12	<p>Determine the nodal displacement, Element stresses for axially loaded bar as shown in the fig. below</p>  <p style="text-align: center;">Fig.</p>	Understand	1								
Part C – Problem Solving Critical Thinking Questions											
1	<p>Consider the following fig. An axial load $P=200 \text{ KN}$ is applied as shown. Using FEM approach for handling boundary conditions, do the following</p> <p>a) Determine the nodal displacements. b) Determine the stress in each material. c) Determine the reaction forces.</p>  <table style="width: 100%; border: none;"> <tr> <td style="text-align: center;">① Aluminum</td> <td style="text-align: center;">② Steel</td> </tr> <tr> <td style="text-align: center;">$A_1 = 2400 \text{ mm}^2$</td> <td style="text-align: center;">$A_2 = 600 \text{ mm}^2$</td> </tr> <tr> <td style="text-align: center;">$E_1 = 70 \times 10^9 \text{ N/m}^2$</td> <td style="text-align: center;">$E_2 = 200 \times 10^9 \text{ N/m}^2$</td> </tr> </table>	① Aluminum	② Steel	$A_1 = 2400 \text{ mm}^2$	$A_2 = 600 \text{ mm}^2$	$E_1 = 70 \times 10^9 \text{ N/m}^2$	$E_2 = 200 \times 10^9 \text{ N/m}^2$	Remember	1,2		
① Aluminum	② Steel										
$A_1 = 2400 \text{ mm}^2$	$A_2 = 600 \text{ mm}^2$										
$E_1 = 70 \times 10^9 \text{ N/m}^2$	$E_2 = 200 \times 10^9 \text{ N/m}^2$										

<p>2</p>	<p>Consider the following fig. An axial load $P=200$ KN is applied as shown. Using an FEM approach, do the following</p> <p>a) Determine the nodal displacements.</p> <p>b) Determine the stress in each material.</p>  <p>Aluminum $A_1 = 2400 \text{ mm}^2$ $E_1 = 70 \times 10^9 \text{ N/m}^2$</p> <p>Steel $A_2 = 600 \text{ mm}^2$ $E_2 = 200 \times 10^9 \text{ N/m}^2$</p>	<p>Understand</p>	<p>1,2</p>
<p>3</p>	<p>In the fig. given below, a load $P=60$ KN is applied as shown. Determine the displacement field, stress and support reactions in the body. Take E as 20 GPa.</p> 	<p>Remember</p>	<p>1,2</p>
<p>4</p>	<p>Consider the rod (a robot arm), which is rotating at constant angular velocity of 30 rad/s. Determine the axial stress distribution in the rod, using two quadratic elements. Consider only the centrifugal force. Ignore bending of the rod.</p>  <p>$A = 0.6 \text{ in.}^2$ $E = 10^7 \text{ psi}$ Weight density, $\rho = 0.2836 \text{ lb/in.}^3$</p>	<p>Remember</p>	<p>1,2</p>
<p>5</p>	<p>The structure consists of two bars. An axial load $P=200$ KN is loaded as shown in fig., determine the following:</p>	<p>Remember</p>	<p>1</p>

	<p>a) Element stiffness matrices b) Global stiffness matrix c) Nodal displacements. d) Stress in each bar.</p>  <p>Steel $A_1 = 1000 \text{ mm}^2$ $E_1 = 200 \text{ GPa}$</p> <p>Bronze $A_1 = 2000 \text{ mm}^2$ $E_1 = 83 \text{ GPa}$</p>		
6	<p>Consider the structure shown in Fig. A rigid bar of negligible mass, pinned at one end, is supported by a steel rod and an aluminum rod. A load $P = 30 \text{ kN}$. N is applied as shown</p>  <p>Steel $A = 1200 \text{ mm}^2$ $E = 200 \times 10^3 \text{ N/mm}^2$ $l = 4.5 \text{ m}$</p> <p>Aluminum $A = 900 \text{ mm}^2$ $E = 70 \times 10^3 \text{ N/mm}^2$ $l = 3 \text{ m}$</p> <p>Assemble stiffness matrix and Determine nodal displacement for above bar element</p>	Understand	1,2
7	<p>Consider the thin (steel) plate in Fig. The plate has a uniform thickness $t = 10 \text{ mm}$, Young's modulus $E = 100 \text{ GPa}$, and weight density $= 78500 \text{ N/m}^3$. In addition to its self-weight, the plate is subjected to a point load $P = 60 \text{ N}$ at its midpoint.</p> <p>a) Write down expressions for the element stiffness matrices and element body force vectors b) Understand the stresses in each element</p> <p>Determine the reaction force at the support. consider $1 \text{ in} = 1 \text{ cm}$ for SI UNITS</p> 	Remember	1,3
8	<p>Consider the bar shown in figure loaded as shown in Determine the a)nodal displacements, b)element stresses and support reactions. $E = 200 \text{ GPa}$</p>	Remember	1,4

			
9	<p>A bar is subjected to an axial force is divided into a number of quadratic elements. For a particular element the nodes 1, 3, 2 are located at 15mm, 18mm and 21mm respectively from origin. If the axial displacements of the three nodes are given by $u_1=0.00015\text{mm}$, $u_3=0.0033$ and $u_2=0.00024\text{mm}$. Determine the following</p> <p>i) shape function ii) variation of the displacement $u(x)$ in the element iii) axial strain in the element</p> <p>Derive the thermally induced stress in the two noded Bar element.</p>	Understand	1
10	Derive element stiffness and load vector Using, Galerkin Approach.	Understand	1,4

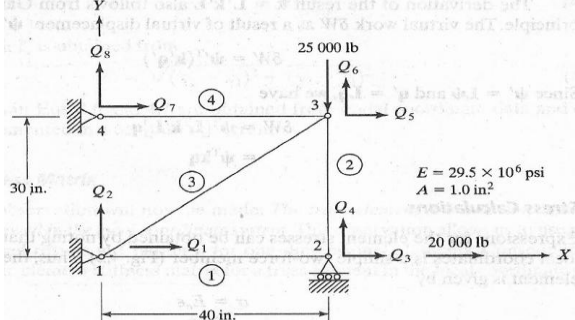
UNIT – II

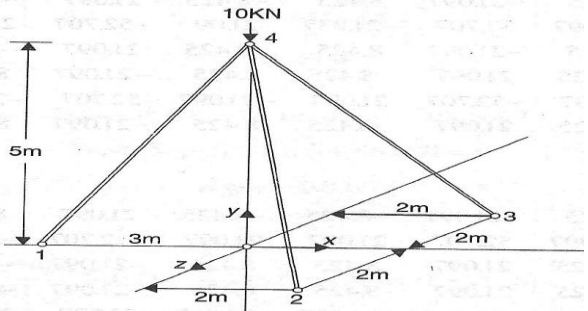
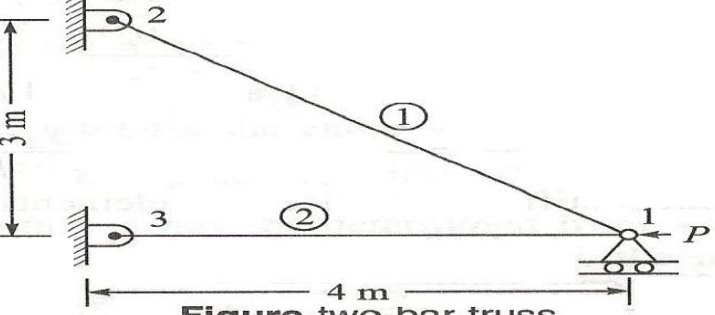
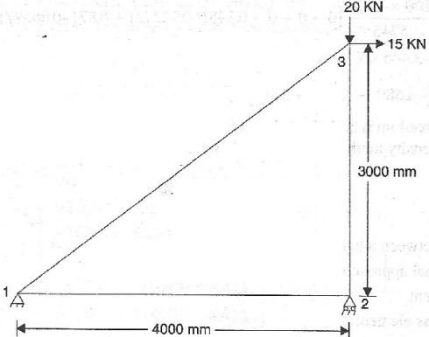
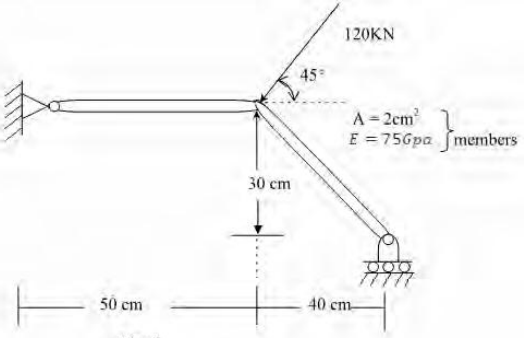
Analysis of trusses and Beams

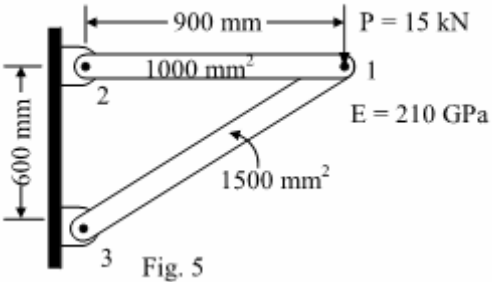
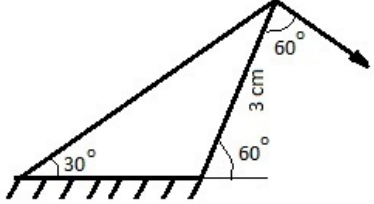
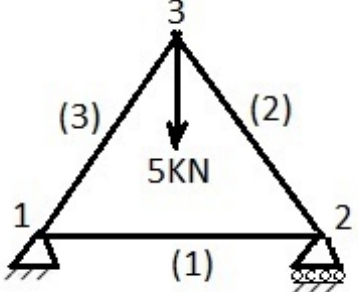
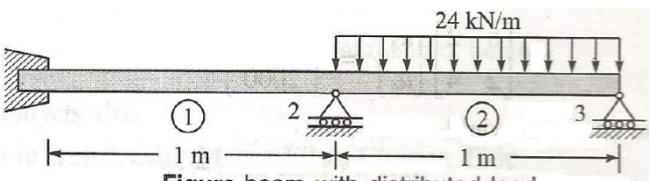
Part A -Short Answer Questions

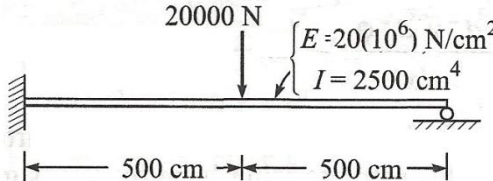
S. No.	Question	Blooms Taxonomy Level	Course Outcomes
1	Represent the truss in local coordinate system.	Understand	1
2	Represent the truss in global coordinate system.	Remember	1
3	What are the characteristics of a truss?	Remember	1
4	Draw a plane truss structure.	Understand	1
5	What is a member and joint?	Understand	1, 3
6	Give the transformation matrix of a truss.	Remember	1
7	What is the expression for element length of a truss?	Understand	1, 3
8	What is the expression for an element stiffness matrix of a truss in local coordinate system?	Understand	1, 3
9	What is the expression for strain energy in a truss element?	Remember	1
10	What is the expression for an element stiffness matrix of a truss in global coordinate system?	Understand	1, 3
11	Give the expression for the stress in a truss element in a local coordinates.	Remember	1
12	Define a beam with examples.	Understand	1, 3
13	Give the various Understands of a beam.	Remember	1
14	Draw the stress distribution diagram for a beam section.	Understand	1, 3
15	Give the expression for the potential energy of a beam.	Remember	1, 3

Part B - Long Answer Questions

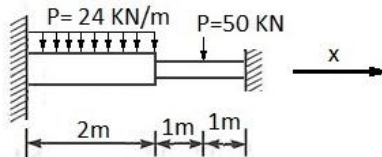
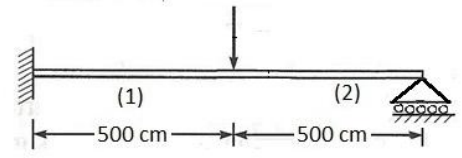
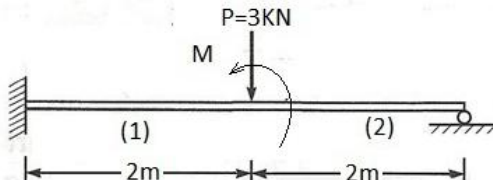
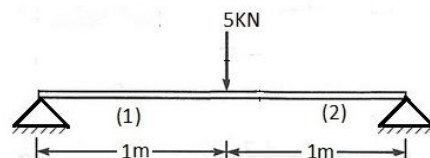
1	<p>Assemble the global stiffness matrix and nodal displacement-for the fig. shown below Understand the problem by using SI units only. Take $1\text{lb} = 4.44\text{N}$ $1\text{in}^2 = 645.16\text{mm}^2$ $1\text{psi} = 6.89\text{KP}$ $1\text{in} = 25.4\text{mm}$</p> 	Remember	1,2
---	---	----------	-----

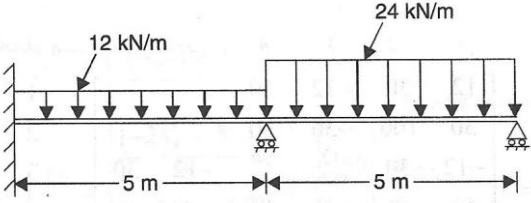
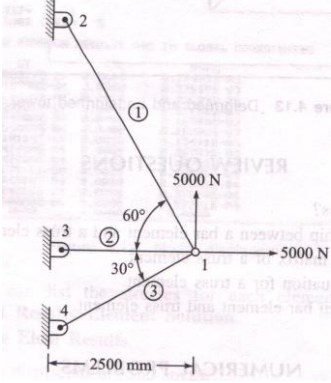
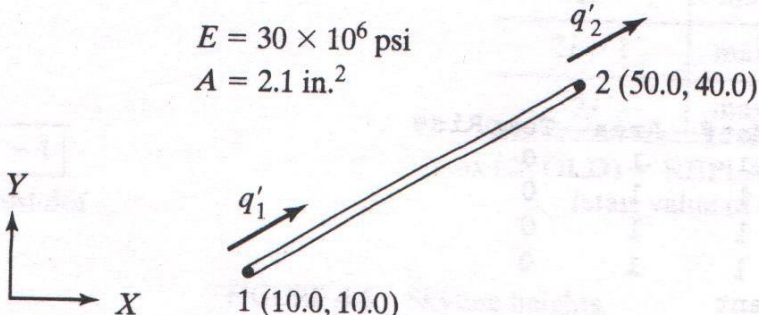
2	<p>The tripod shown in figure below carries a vertically downward load of 10kN at joint 4. If Young's modulus of the material of tripod stand is 200kN/mm², determine the forces developed in the legs of the tripod.</p> 	Remember	1,3
3	<p>For the two-bar truss shown in Figure below, determine the nodal displacements, element stresses and support reactions. A force of P=1000kN is applied at node-1. Assume E=210GPa and A=600mm² for each element.</p>  <p style="text-align: center;">Figure two-bar truss.</p>	Understand	1,4
4	<p>Obtain the forces in the plane Truss shown in Figure below and determine the support reactions also. Take E=200GPa and A= 2000mm²</p>  <p style="text-align: center;">Fig.</p>	Remember	3,1
5	<p>For the truss shown in fig.2 determine the a) displacements and b) stresses in the bars .</p>  <p style="text-align: center;">Fig. 2</p>	Understand	1, 3
6	<p>a) Distinguish between local, natural and global coordinates. b) For the pin jointed configuration shown in Fig.5, determine; i) displacement ii) element stress given $\alpha = 10 \times 10^{-6}$ per $^{\circ}\text{C}$ $\Delta T = 50^{\circ}$</p>	Remember	2,3

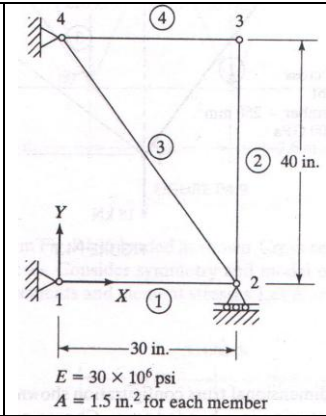
	 <p>Fig. 5</p>														
7	<p>Calculate nodal displacements and element stresses for the members shown in fig. $E=200\text{GPa}$, $A=500\text{mm}^2$, and $P=25\text{KN}$.</p> 	Understand	2,3												
8	<p>Determine Nodal displacements and Element stresses in the truss shown in fig. $E=80\text{GPa}$.</p> <table border="1" data-bbox="319 985 1085 1153"> <thead> <tr> <th>Element</th> <th>Area mm^2</th> <th>Length mm</th> </tr> </thead> <tbody> <tr> <td>1</td> <td>600</td> <td>500</td> </tr> <tr> <td>2</td> <td>600</td> <td>600</td> </tr> <tr> <td>3</td> <td>600</td> <td>500</td> </tr> </tbody> </table> 	Element	Area mm^2	Length mm	1	600	500	2	600	600	3	600	500	Remember	1
Element	Area mm^2	Length mm													
1	600	500													
2	600	600													
3	600	500													
9	Derive the stiffness matrix for a_1^1 2D truss Element.	Remember	1,3												
10	Derive the Stiffness matrix for a 3D truss Element.	Understand	1,2												
11	<p>For the beam shown in Figure below, determine the following: a) Slopes at nodes 2 and 3. b) Vertical deflection at the mid-point of the distributed load. Consider all the elements have $E=200\text{GPa}$, $I=5 \times 10^6 \text{ mm}^4$.</p>  <p>Figure beam with distributed load</p>	Remember	1,4												
12	A beam fixed at one end and supported by a roller at the other end, has a 20kN concentrated load applied at the centre of the span (Figure below). Calculate the deflection under the load and construct the shear force and	Understand	1												

	bending moment diagrams for the beam.  Figure beam with a point load		
13	Derive the Hermite shape functions for a beam element.	Remember	1,2
14	Draw beam element in global and intrinsic co ordinate system.	Understand	1,2
15	Derive element stiffness matrix for a beam element.	Understand	1,2

Part C – Problem Solving Critical Thinking Questions

1	Determine the deflection and slope under the point load for the beam shown in fig given. $E=200 \text{ GP}_a, I=4 \times 10^{-6} \text{ m}^4, I_2=2 \times 10^{-6} \text{ m}^4$. 	Remember	1,2
2	A beam fixed at one end and supported by a roller at the end, has a 20kN concentrated load applied at the centre of the span, as shown in fig. calculate the deflection under the load and construct shear force and bending moment diagram for the beam. Take $E = 20 \times 10^6 \text{ N/c}^2, I=2500 \text{ cm}^4$. 	Understand	1,3
3	Determine the nodal displacements and slopes for the beam shown in fig. find the moment at the mid point of element. Take $E=200 \text{ GP}_a, I=5 \times 10^4 \text{ mm}^4, M=6 \text{ kNm}$. 	Remember	2,3
4	Determine the nodal displacements and slopes at the position of one-fourth distance from the support of shaft: Take $E=200 \text{ GP}_a, I=6 \times 10^4 \text{ mm}^4$. The shaft is simply supported at A and B. 	Remember	1
5	Understand the beam shown in Figure below by finite element method and determine the end reactions. Also determine the deflections at mid spans given $E=2 \times 10^5 \text{ N/mm}^2$, and $I=5 \times 10^6 \text{ mm}^4$.	Understand	3,1

			
6	Derive element stiffness matrix for a truss element in global coordinate system.	Understand	1
7	For the truss shown in fig, Understand for the horizontal and vertical components of displacement at node 1 and determine the stress in each element. All elements have $A = 500 \text{ mm}^2$ and $E = 70 \text{ GPa}$. 	Remember	1,2
8	Derive stiffness matrix and stress equation for a truss element.	Understand	1,2
9	For the truss element shown below, if $q = [1.5, 1.0, 2.1, 4.3]^T \times 10^{-2} \text{ in.}$, determine the following: <ol style="list-style-type: none"> The vector q' The stress in the element The K matrix. $E = 30 \times 10^6 \text{ psi}$ $A = 2.1 \text{ in.}^2$ 	Remember	1,2
10	For the truss given below, a horizontal load of $P = 4000 \text{ lb}$ is applied in the x-direction at node 2. <ol style="list-style-type: none"> Write down the element stiffness matrix k for each element. Assemble the K matrix Using elimination approach, Understand for Q 	Remember	1,2



UNIT – III
Stress analysis with CST elemets

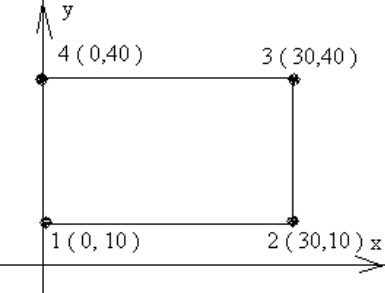
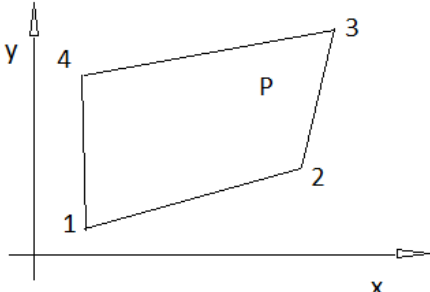
Part A -Short Answer Questions

1	What is a two dimensional element.	Understand	4,5
2	List any four two dimensional elements with neat sketches.	Understand	4,5
3	Enumerate some of the Understands of 2-D elements.	Remember	4,5
4	What do you mean by discretizing of 2-D elements.	Remember	4,5
5	Define shape function.	Remember	4,5
6	What is the condition for number of unknown polynomial coefficients of a 2-D element?	Understand	4,5
7	Express the 2-D element in polynomial series.	Remember	4,5
8	What is a CST element?	Understand	4,5
9	What is LST element?	Understand	4,5
10	Represent the node numbering of Constant strain triangle element.	Remember	4,5
11	Represent the node numbering of Linear strain triangle element.	Understand	4,5
12	Define Quadratic triangle.	Remember	4,5
13	Write the expression for displacements developed in the X-direction of CST element.	Understand	4,5
14	Write the expression for displacements developed in the X-direction of LST element.	Remember	4,5
15	Write the expression for displacements developed in the Y-direction of CST element.	Remember	4,5
16	Write the expression for displacements developed in the Y-direction of LST element.	Understand	4,5
17	What is a linear element?	Remember	4,5
18	What is a nonlinear element?	Understand	4,5
19	Differentiate between linear and non linear elements.	Remember	4,5
20	What type of nodes of considered for Linear elements?	Understand	4,5
21	What type of nodes of considered for non-Linear elements?	Remember	4,5

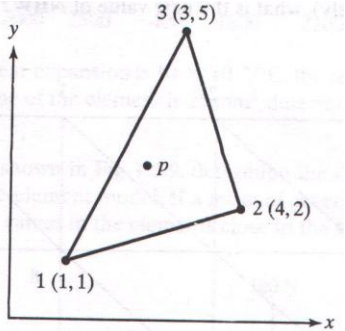
Part B - Long Answer Questions

1	<p>a) formulate the finite element equations for constant strain triangle as shown in fig 1.1. Assume plane stress, $E=200\text{Gpa}$, $\nu=0.25$, thickness=5mm, nodal co-ordinates</p> <table border="1" style="margin-left: auto; margin-right: auto;"> <tr> <td style="padding: 2px;">X1=1</td> <td style="padding: 2px;">X2=5</td> <td style="padding: 2px;">X3=3</td> </tr> <tr> <td style="padding: 2px;">Y1=2</td> <td style="padding: 2px;">Y2=4</td> <td style="padding: 2px;">Y3=6</td> </tr> </table> <p>Pressure on 1-2 edge is 5N/mm^2</p> <p>b) calculate the element stress for the element shown in fig1.2 for the plain strain condition. Displacement vector given as $[q]=[0 \ 0 \ 0.001 \ 0.002 \ -0.003 \ 0.002]$ mm, $E=200\text{Gpa}$, $\nu=0.25$, thickness=20mm $\alpha=2 \times 10^{-6}$ per 0c $\Delta T=50$ deg c</p> <table border="1" style="margin-left: auto; margin-right: auto;"> <tr> <td style="padding: 2px;">X1=0</td> <td style="padding: 2px;">X2=25</td> <td style="padding: 2px;">X3=25</td> </tr> <tr> <td style="padding: 2px;">Y1=0</td> <td style="padding: 2px;">Y2=0</td> <td style="padding: 2px;">Y3=25</td> </tr> <tr> <td></td> <td></td> <td style="padding: 2px;">0</td> </tr> </table>	X1=1	X2=5	X3=3	Y1=2	Y2=4	Y3=6	X1=0	X2=25	X3=25	Y1=0	Y2=0	Y3=25			0	Remember	4,5
X1=1	X2=5	X3=3																
Y1=2	Y2=4	Y3=6																
X1=0	X2=25	X3=25																
Y1=0	Y2=0	Y3=25																
		0																
2	<p>Formulate the finite element equations for the element shown in fig2.1 $E=200\text{Gpa}$, $\nu=0.3$, thickness=5mm, $p_1=5\text{N/mm}^2$ acting on side jk and along x -direction $P_2=2\text{N/mm}^2$ acting along on the side and perpendicular to the side ik. use plane stress condition.</p> <table border="1" style="margin-left: auto; margin-right: auto;"> <tr> <td style="padding: 2px;">$X_i=1$</td> <td style="padding: 2px;">$X_j=6$</td> <td style="padding: 2px;">$X_k=3$</td> </tr> <tr> <td style="padding: 2px;">$Y_i=1$</td> <td style="padding: 2px;">$Y_j=4$</td> <td style="padding: 2px;">$Y_k=5$</td> </tr> </table> <div style="text-align: center; margin-top: 10px;"> </div>	$X_i=1$	$X_j=6$	$X_k=3$	$Y_i=1$	$Y_j=4$	$Y_k=5$	Remember	4,5									
$X_i=1$	$X_j=6$	$X_k=3$																
$Y_i=1$	$Y_j=4$	$Y_k=5$																
3	<p>a). Explain Iso-parametric, sub-parametric and super-parametric elements b) Advantages of iso-parametric elements c) Write short notes on Gaussian quadrature integration technique</p>	Understand	4,5															
4	Derive the strain displacement matrix for triangular element.	Understand	4,5															
5	<p>For the configuration shown in figure, determine the deflection at the point load Understand Using a one element model. $T = 10 \text{ mm}$, $E = 70 \text{ G Pa}$, $\nu = .3$</p> <div style="text-align: center; margin-top: 10px;"> </div>	Remember	4,5															
6	<p>a) Explain Convergence requirements. b) The Nodal Coordinates of the triangular elements is shown in fig: At the interior point P, the x-coordinate is 3.3 and $N_1 = 0.3$. Determine N_1N_2 and the y-coordinate of point P.</p>	Remember	4,5															

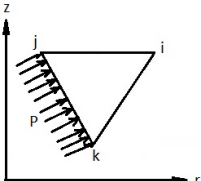
7	<p>a) Understand the integral $I = \int \int (2x^2 + 3xy + 4y^2) dx dy$ in the limits of -1 to +1 using gauss quadrature numerical integration</p> <p>b) Verify with exact solution.</p>	Understand	4,5
8	<p>Understand the element stiffness matrix for the triangular element shown in fig. under plane strain condition. Assume the following values. $E=200 \text{ GPa}$, $\mu=0.25$, $t=1 \text{ mm}$.</p>	Remember	4,5
9	<p>For the plane stress element shown in fig. the nodal displacements are $u_1=2.0\text{mm}$; $V_1=1.0$; $u_2=1.0\text{mm}$; $V_2=1.5\text{mm}$; $u_3=2.5\text{mm}$; $V_3=0.5\text{mm}$. Determine the element stresses. Assume $E=200 \text{ GN/m}^2$; $\mu=0.3$; $t=10$</p> <p style="text-align: center;">mm.</p>	Understand	4,5
10	<p>Determine the nodal displacements and element stresses for the two dimensional loaded plate as shown in fig. Assume plane stress conditions. Body force may be neglected in comparison to the external forces. Take $E=210 \text{ GPa}$, $\mu=0.25$; thickness = 10mm.</p>	Understand	4,5

11	<p>a) A four node quadrilateral element is shown in fig 1.3. The coordinates of each node are given in cm. The element displacement vector is given as $[q] = [0 \ 0 \ 0.2 \ 0 \ 0.15 \ 0.10 \ 0 \ 0.05]$ cm. Determine (i) the x, y coordinates of a point P whose location at $\xi = 0.5, \eta = 0.5$ (ii) the displacement of point P (u,v) (iii) the jacobian at P</p> <p>b) Understand the Integral $I = \int_{-1}^1 (3\xi^2 + \xi^3) d\xi$ using Gaussian quadrature method.</p>	Remember	6,7															
12	Determine the shape functions for a 8 node quadratic quadrilateral element (boundary noded).	Understand	6,7															
13	<p>For the element shown in the figure, assemble Jacobian matrix and strain displacement matrix</p> 	Understand	6,7															
14	Derive the a) shape function and b) strain displacement matrices for triangular element of revolving body.	Remember	6,7															
15	<p>For the Isoparametric quadrilateral element shown in fig, determine the local co-ordinates of the point P whose Cartesian co-ordinates are (6,4)</p>  <table border="1" data-bbox="497 1344 865 1505"> <thead> <tr> <th>node</th> <th>x</th> <th>y</th> </tr> </thead> <tbody> <tr> <td>1</td> <td>2</td> <td>1</td> </tr> <tr> <td>2</td> <td>5</td> <td>2</td> </tr> <tr> <td>3</td> <td>7</td> <td>6</td> </tr> <tr> <td>4</td> <td>1</td> <td>5</td> </tr> </tbody> </table>	node	x	y	1	2	1	2	5	2	3	7	6	4	1	5	Understand	6,7
node	x	y																
1	2	1																
2	5	2																
3	7	6																
4	1	5																

Part C – Problem Solving Critical Thinking Questions

1	<p>For the point P located inside the triangle, the shape functions N_1 and N_2 are 0.15 and 0.25, respectively. Determine the x and y coordinate of P.</p> 	Remember	5,6
2	<p>For the triangular element shown in fig, obtain strain-displacement relation matrix B and determine the strains ϵ_x, ϵ_y and γ_{xy}.</p>	Remember	5,6

3	<p>Formulate the element equations for axisymmetric element shown in fig</p> <table border="1"> <thead> <tr> <th>node</th> <th>R</th> <th>z</th> </tr> </thead> <tbody> <tr> <td>i</td> <td>5</td> <td>5</td> </tr> <tr> <td>j</td> <td>1</td> <td>5</td> </tr> <tr> <td>k</td> <td>3</td> <td>2</td> </tr> </tbody> </table> <p>$E=100\text{Gpa}$, $\nu=0.3 \text{ \AA } 5 \times 10^{-6}$ per deg C $\Delta T=60$ deg $p=8\text{N/mm}^2$ acting perpendicular to jk side</p>	node	R	z	i	5	5	j	1	5	k	3	2	Remember	5,6
node	R	z													
i	5	5													
j	1	5													
k	3	2													
4	<p>Determine the strain displacement matrix for the TETRAHEDRAL element as shown in fig</p>	Understand	5,6												
5	<p>A triangular membrane element of thickness=0.1cm with the x,yco ordinates of the nodes indicated node numbers as shown in the figure. If the material of the element is steel with young's modulus $E=207$ Gpa and poisons ratio=0.3.Determine the following.</p> <ol style="list-style-type: none"> shape functions of the element N_1, N_2 & N_3 strain displacement matrix ,B Elasticity matrix D for plane stress condition element stiffness matrix <p>$x_1=1$ $y_1=3$ $x_2=5$ $y_2=4$ $x_3=4$ $y_3=7$</p>	Understand	5,6												
6	<p>Explain the concept of numerical integration and its utility in generating Isoperimetric finite element matrices.</p>	Understand	5,6												
7	<p>Explain the concept of numerical integration and its utility in generating Isoperimetric finite element matrices.</p>	Remember	5,6												
8	<p>Understand the integral $I=\int \int (3x^3 + 2xy + 7y^3) dx dy$ in the limits of -1 to +1 using gauss quadrature numerical integration and verify with exact solution.</p>	Understand	6,7												

9	<p>Formulate element equations for the Axisymmetric element shown in fig.</p> <p>$E=100 \text{ GPa}$, $\mu=0.3$ $\alpha=5 \times 10^{-6} \text{ Pic}^{\circ}\text{C}$.</p> <p>$\square T = 60^{\circ}\text{C}$</p> <p>$P=8\text{N/mm}^2$ acting perpendicular to side jk</p> <p>Nodal co-ordinates</p> <p>$r_i = 5, \quad r_j = 1, \quad r_k = 3,$ $z_i = 5, \quad z_j = 5, \quad z_k = 2,$</p> 	Remember	5,6
---	--	----------	-----

UNIT – IV

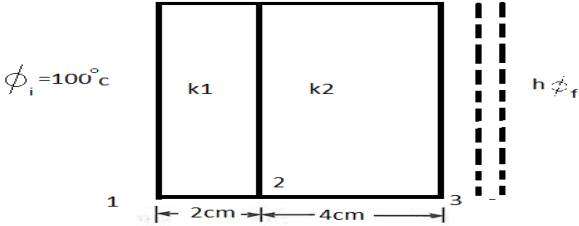
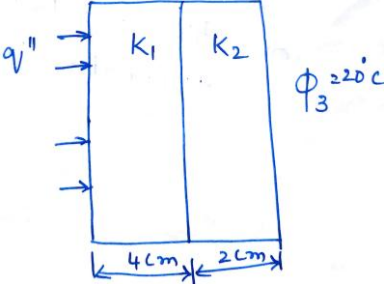
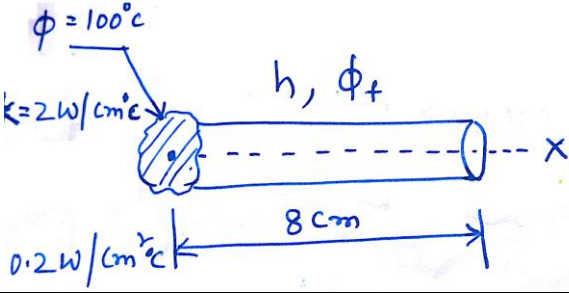
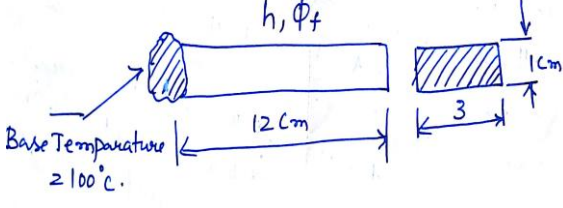
Steady state Heat transfer analysis

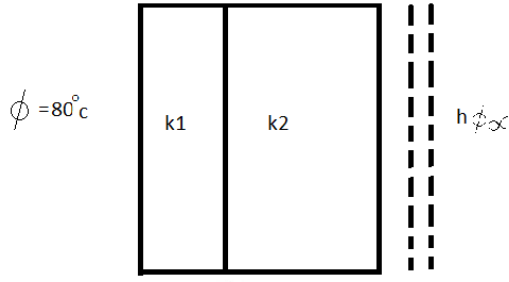
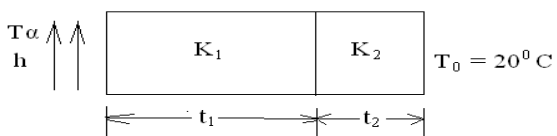
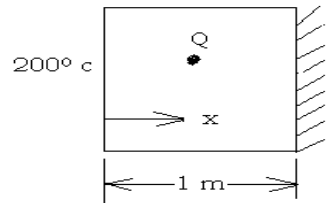
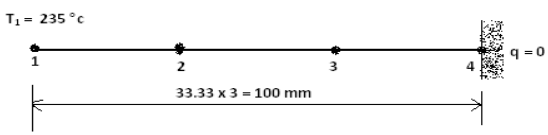
Part A -Short Answer Questions

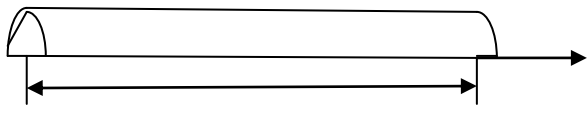
1	What is conduction?	Remember	9,10
2	Define fins or extended surfaces	Remember	9,10
3	State the Understands of fins.	Remember	9,10
4	Discuss the types of heat transfer	Remember	9,10
5	What is Convection?	Understand	9,10
6	What is radiation?	Understand	9,10
7	What is Fourier's law?	Understand	9,10
8	What is Newton's law of cooling?	Remember	9,10
9	What is Stefan-Boltzmann law?	Understand	9,10
10	Write the basic equation of heat transfer.	Understand	9,10

Part B - Long Answer Questions

1	Derive thermal stiffness matrix for one dimensional heat conduction with lateral surface convection and with internal heat generation.	Remember	8,9
2	Describe heat transfer analysis for composite wall.	Remember	8,9
3	Describe heat transfer analysis for straight fin	Understand	8,9
4	Derive the Strain displacement Matrix for 2D-Thin plate. Consider the temperature field with in the triangular element is given by $T= N_1T_1 + N_2T_2 + N_3T_3$.	Remember	8,9
5	Describe heat transfer analysis for tapered fin.	Understand	8,9
6	Determine the nodal temperatures in a composite wall shown in fig. the wall in maintained at 100°C at the left face and convection mode of heat transfer occurs between the right fare and the existing fluwd. Thermal conduction $K_1=0.06\text{W/cm}^{\circ}\text{C}$, $K_2=0.2 \text{ W/Cm}^{\circ}\text{C}$, Convection co-efficient of heat transfer between walls and fluid $h=0.1\text{W/cm}^2 \text{ }^{\circ}\text{C}$ and $\varnothing_f=25^{\circ}\text{C}$. Consider unit area $A=1\text{cm}^2$ perpendicular to the direction of heat flow.	Understand	8,9

			
7	<p>Determine the temperature at the nodal interfaces for the two layered wall shown in fig. the left face is supplied with heat flux of $q''=5\text{w/cm}^2$ and right face in main fained at 20°C.</p> <p>$Q''=5\text{w/cm}^2$ $K_1=0.2\text{W/cm}^0\text{C}$ $K_2=0.06\text{W/cm}^0\text{C}$ $A=1\text{cm}^2$.</p> 	Remember	8, 9
8	<p>Determine the temperature distribution in a fig of circular goss-section shown in fig. Base of the fin in maintained at 100°C and tip of the fin is insulated. Thermal conductivity $K=2\text{w/cm}^0\text{C}$, Convective heat transfer co-efficient $h=0.2\text{w/cm}^2$, $\phi_f=20^\circ\text{C}$ (fluid temperature) and Diameter of the fin=1cm.</p> 	Remember	8, 9
9	<p>Calculate the nodal temperature using one dimensional analysis of a fin as shown in fig. The fin has rectangular cross-section. Assume that the tip of the fin in insulated. Understand the problem</p> <ol style="list-style-type: none"> 2 Linear elements 3 Linear elements 4 Linear elements and compare nodal temperatures. <p>Thermal conductivity $K=4\text{w/cm}^0\text{C}$, Convective heat transfer co-efficient $h=0.1\text{w/cm}^2\text{ }^\circ\text{C}$ and Adjacent fluid temperature $\phi_f=25^\circ\text{C}$.</p> 	Understand	8, 9
10	<p>Determine the nodal temperatures and rate of heat transfer through a composite wall shown in fig. Thermal conductivities $K_1=45\text{w/m}^0\text{C}$ and $K_2=0.5\text{w/m}^0\text{C}$. Convective heat transfer co-efficient $h=20\text{w/m}^2\text{ }^\circ\text{C}$, Temperature of left face of wall $=80^\circ\text{C}$ and Ambient temperature $\phi_a=25^\circ\text{C}$. Assume the area normal to the direction of heat flow $=1\text{cm}^2$. Use linear elements.</p>	Understand	8, 9

			
11	Write down the differential equations of 1D steady state heat conduction problem.	Remember	8, 9
12	What are different types of boundary conditions for 1D heat conduction problems?	Understand	8, 9
13	Obtain the functional approach of finite element equations for a one dimensional heat conduction problem.	Remember	8, 9
14	Derive one dimensional steady state heat conduction equation.	Understand	8, 9
15	Compare the finite element formulations of structural problems with heat transfer problems.	Remember	8, 9
Part C – Problem Solving Critical Thinking Questions			
1	<p>Determine the temperature distribution through the composite wall shown in figure, when convection heat loss occurs on the left surface. Assume unit area. Assume wall thickness $t_1 = 4\text{cm}$, $t_2 = 2\text{cm}$, $k_1 = 0.5\text{W/cm}^0\text{c}$, $k_2 = 0.05\text{W/cm}^0\text{c}$, $h = 0.1\text{W/cm}^2\text{ }^0\text{c}$ and $T_a = -5^0\text{c}$.</p> 	Remember	8, 9
2	<p>The plane wall shown in fig. The thermal conductivity $K = 25\text{W/m}^0\text{c}$ and there is a uniform generation of heat in the wall of $Q = 400\text{W/m}^3$. Determine the temperature distribution at five nodes (include two sides of the walls) in equal distances through the wall thickness.</p> 	Remember	8, 9
3	<p>A metallic fin with thermal conductivity $K=360\text{W/m}^0\text{c}$, 1mm thick and 100mm long extends from a plane wall whose temperature is 235^0c. Determine the distribution and amount of heat transferred from the fin to air at 20^0c with $h= 9\text{W/m}^2\text{ }^0\text{c}$ take width of the fin is 1000 mm. Assume tip is insulated.</p> 	Understand	8, 9
4	<p>Determine the temperature distribution in a fin of circular cross section shown in fig1.5. considering two elements, base of the fin is maintained at 100 deg c and tip of the fin is insulated. Thermal conductivity $k=2\text{w/cm deg c}$. Convective heat transfer co-efficient is $h=0.2\text{w/cm}^2\text{deg c}$. Fluid temperature $T_\infty=20\text{ DEG C}$, DIAMETRE OF THE FIN=1cm.</p>	Remember	8, 9

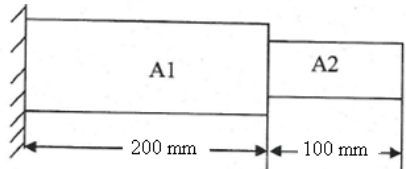
	length=8cm 		
5	Derive one dimensional steady state heat conduction equation and Understand to one dimensional fin problem	Understand	8, 9
6	Explain the methodology for the treatment of all three boundary conditions in a 1-D heat transfer element?	Understand	8, 9
7	Derive element equations for a one dimensional heat conduction element by considering the weak form.	Remember	8, 9
8	Derive the conductivity matrix and thermal load vector for the one dimensional finite element for the three boundary conditions.	Remember	8, 9
9	Give a brief description of steady state problems.	Understand	8, 9

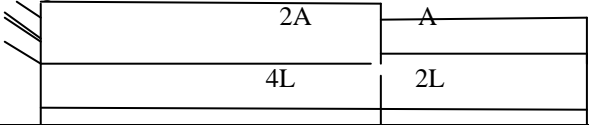
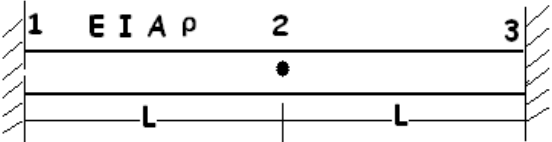
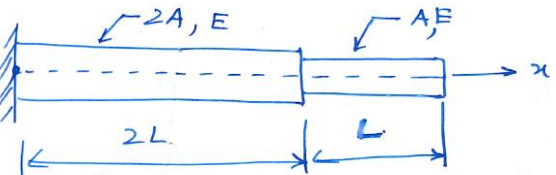
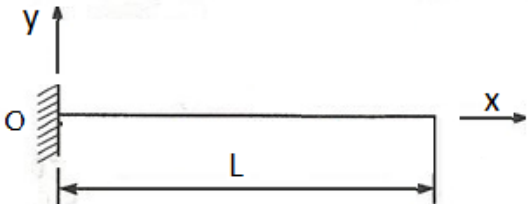
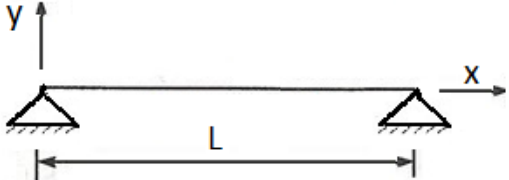
UNIT – V
Dynamic analysis

Part A -Short Answer Questions

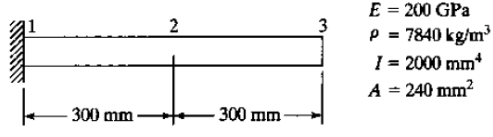
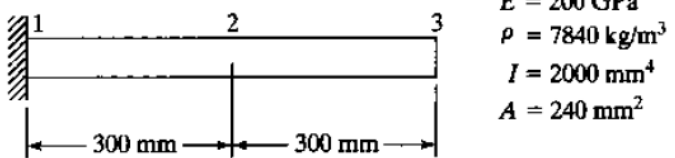
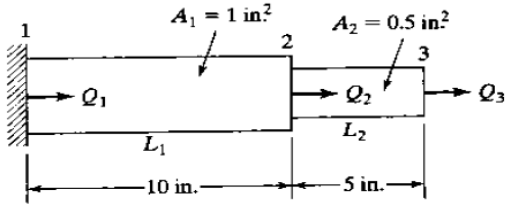
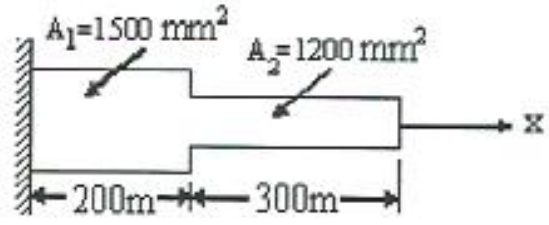
1	What is lumped mass matrix?	Understand	12
2	What is consistent mass matrix?	Remember	12
3	Define Eigen values?	Understand	12
4	What is meant Eigen Vectors?	Understand	12
5	Write the expression for element mass matrix for a bar element?	Remember	12, 13
6	Write the expression for element mass matrix for a truss element?	Remember	12
7	Write the expression for element mass matrix for a CST element?	Understand	12, 13
8	Write the mass matrix for truss element with an example.	Remember	12, 13
9	Write the expression for modal analysis of bar and beam elements.	Remember	12
10	What are the convergence requirements in finite element modeling?	Remember	12, 13
11	List some software packages of FEA.	Remember	12
12	What are the important steps in ANSYS.	Understand	12, 13,14
13	Give some practical problems associated with finite element modelling.	Remember	12
14	What is the difference between h-method and p-method.	Remember	12, 13
15	Write the importance of element selection in fem.	Understand	12, 13
16	Write the importance of boundary conditions in finite element modelling.	Remember	12
17	List out factors influencing the accuracy of the results	Understand	12, 13
18	Define free meshing.	Understand	12,14
19	Define mapped meshing.	Remember	12, 13,14
20	What is meant by pre processing?	Understand	13,14

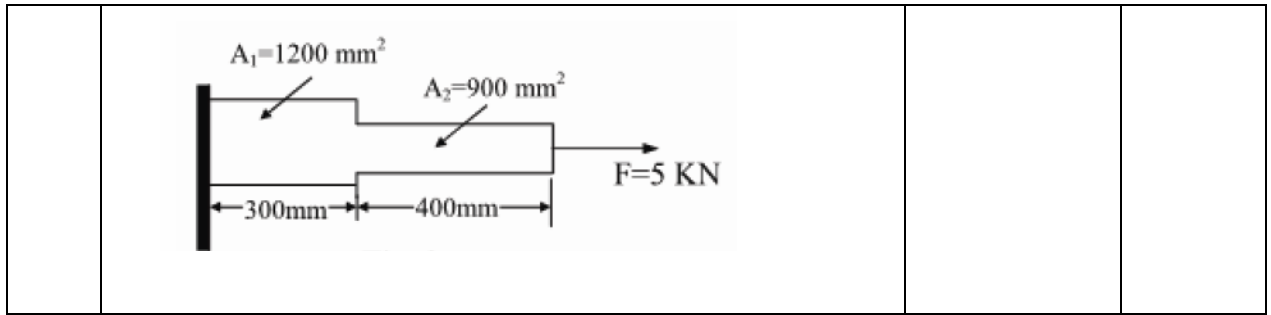
Part B - Long Answer Questions

1	Understand natural frequencies for the stepped bar shown fig. in axial vibration take $E=200$ GPa and DENSITY= 7850 Kg/m ³ .b)Draw mode shapes and determine Eigen vector .Take $A_1=400$ mm ² and $A_2=200$ mm ² using characteristic polynomial method. 	Remember	12, 13
2	Explain the following with examples: a) Lumped parameter model. b) Continuous system model.	Understand	12, 13

3	Understand natural frequencies for the cantilever beam using one element.	Understand	12, 13
4	<p>a) Understand natural frequencies for the stepped bar shown in fig</p> <p>b) corresponding eigenvectors and mode shapes. take $E=200\text{Gpa}$ and density 7500 Kg/m^3. Take $A=600\text{mm}^2$ and LENGTH $L=300\text{mm}$</p> 	Remember	12, 13
5	<p>a) Determine the eigen values and the associated Eigen vectors of the matrix [A] given by</p> $A = \begin{bmatrix} 3 & 4 \\ 4 & -3 \end{bmatrix}$ <p>b) State the properties of Eigen Values.</p>	Remember	12, 13
6	<p>Determine the Natural frequency of the beam shown in the figure.</p> 	Remember	12, 13
7	<p>Derive the eigen value eigen vector and mode shapes of the given stepped bar element. When L=length; A=Area of cross-section E=Modules of electivity and P=Density of the material.</p> 	Remember	12, 13
8	<p>Derive Approximate the first two natural frequencies of a cantilever beam using one element model. EI=Flexural rigidity.</p> 	Remember	12, 13
9	<p>Determine the approximate first two natural frequeneves of a simply supported beam using on a element. Flexural Rigidity =EI; Density = P Cross-sectional area=A</p> 	Remember	12, 13
10	<p>Determine the mass matrix for truss element with an example.</p> <p>Consider axial vibration of the Aluminium bar shown in Figure below,</p> <ol style="list-style-type: none"> Develop the global stiffness and Determine the nodal displacements and stresses using elimination approach and with help of linear and quadratic shape function concept. Assume Young's Modulus $E = 70\text{Gpa}$. 	Remember	12, 13

11	Differentiate between Consistent Mass matrix and Lumped Mass matrix	Understand	12, 13
12	<p>Consider axial vibration of the steel bar shown in Figure below,</p> <p>a. Develop the global stiffness and mass matrix and</p> <p>b. Determine the natural frequencies and mode shapes using the characteristic polynomial technique.</p>	Remember	12, 13
13	Derive the elemental mass matrix for 1-D bar element and 1-D plane truss element.	Understand	12, 13
Part C – Problem Solving Critical Thinking Questions			
1	<p>Consider axial vibration of the steel bar shown in Figure below develop the global stiffness and mass matrix and determine the natural frequencies and mode shapes using the characteristic polynomial technique</p>	Remember	12, 13
2	Determine the Eigenvalues and Eigenvectors for the stepped bar shown in Figure below.	Remember	12, 13
	<p style="text-align: center;">$E = 30 \times 10^6 \text{ psi}$ Specific weight $f = 0.283 \text{ lb/in}^3$</p>		
3	Understand the lowest Eigenvalue and the corresponding Eigenmode for the beam shown in Figure below	Remember	12, 13

	 <p> $E = 200 \text{ GPa}$ $\rho = 7840 \text{ kg/m}^3$ $I = 2000 \text{ mm}^4$ $A = 240 \text{ mm}^2$ </p>		
4	<p>Understand the lowest Eigenvalue and the corresponding Eigenmode for the beam shown in Figure below.</p>  <p> $E = 200 \text{ GPa}$ $\rho = 7840 \text{ kg/m}^3$ $I = 2000 \text{ mm}^4$ $A = 240 \text{ mm}^2$ </p>	Understand	12, 13
5	<p>Determine the Eigenvalues and Eigenvectors for the stepped bar shown in Figure below.</p>  <p> $E = 30 \times 10^6 \text{ psi}$ Specific weight $f = 0.283 \text{ lb/in}^3$ </p>	Understand	12, 13
6	From first principles, derive the general equation for elemental mass matrix?	Understand	12, 13
7	Determine the natural frequencies and mode shapes of a stepped bar shown in figure below using the characteristic polynomial technique. Assume $E=300\text{GPa}$ and density is 7800 Kg/m^3 .	Understand	12, 13
8	State the method used for obtaining natural frequencies and corresponding eigen vectors.	Remember	12, 13
9	Determine the natural frequencies and mode shapes of a stepped bar shown in figure below using the characteristic polynomial technique. Assume $E=300\text{GPa}$ and density is 7800 Kg/m^3 .	Remember	12, 13
			
10	<p>Consider axial vibration of the Aluminium bar shown in Figure below,</p> <ol style="list-style-type: none"> Develop the global stiffness and Determine the nodal displacements and stresses using elimination approach and with help of linear and quadratic shape function concept. Assume Young's Modulus $E = 70\text{Gpa}$. 	Understand	12, 13



Prepared by:

Ms Y Shwetha, Asst. Professor . Department of AE

Mr. G. S. D Madhav, Asst. Professor, Department of AE

HOD, AE