



INSTITUTE OF AERONAUTICAL ENGINEERING

(Autonomous)

Dundigal, Hyderabad - 500 043

FRESHMAN ENGINEERING

TUTORIAL QUESTION BANK

| | | |
|--------------------|---|--|
| Course Name | : | Mathematics-II |
| Course Code | : | A30006 |
| Class | : | II B. Tech I Semester |
| Branch | : | CIVIL |
| Year | : | 2016 – 2017 |
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| Course Faculty | : | Ms.K.Rama Jyothi, Assistant Professor, Freshman Department |

OBJECTIVES

To meet the challenge of ensuring excellence in engineering education, the issue of quality needs to be addressed, debated and taken forward in a systematic manner. Accreditation is the principal means of quality assurance in higher education. The major emphasis of accreditation process is to measure the outcomes of the program that is being accredited.

In line with this, Faculty of Institute of Aeronautical Engineering, Hyderabad has taken a lead in incorporating philosophy of outcome based education in the process of problem solving and career development. So, all students of the institute should understand the depth and approach of course to be taught through this question bank, which will enhance learner's learning process.

1. Group - A (Short Answer Questions)

| S. No | Question | Blooms Taxonomy Level | Course Outcome |
|-----------------------------------|--|-----------------------|----------------|
| UNIT-I VECTOR CALCULUS | | | |
| 1 | Define gradient? | Remember | 1 |
| 2 | Define divergence? | Remember | 1 |
| 3 | Define curl? | Remember | 1 |
| 4 | Define laplacian operator? | Remember | 1 |
| 5 | Find $\Delta(x^2yz)$ | Apply | 1 |
| 6 | Evaluate the angle between the normal to the surface $xy = z^2$ at the points (4,1,2) and (3,3,-3)? | Understand | 1 |
| 7 | Find a unit normal vector to the given surface $x^2y + 2xz = 4$ at the point (2,-2,3)? | Apply | 1 |
| 8 | If \vec{a} is a vector then prove that $\text{grad}(\vec{a} \cdot \vec{r}) = \vec{a}$? | Understand | 1 |
| 9 | Define irrotational and solenoidal vectors? | Remember | 1 |
| 10 | Prove that $(\nabla f \times \nabla g)$ is solenoidal? | Analyze | 1 |
| 11 | Prove that $F = yzi + zxj + xyk$ is irrotational? | Analyze | 1 |
| 12 | Show that $(x+3y)i + (y-2z)j + (x-2z)k$ is solenoidal? | Understand | 1 |
| 13 | Show that $\text{curl}(r^n \vec{r}) = 0$? | Understand | 1 |
| 14 | Prove that $\text{curl}(\nabla \phi) = (\text{grad} \phi) \times \vec{a} + \nabla \text{curl} \vec{a}$? | Analyze | 1 |

| S. No | Question | Blooms Taxonomy Level | Course Outcome |
|--|--|-----------------------|----------------|
| 15 | Prove that $\text{div curl } \vec{f} = 0$? | Analyze | 1 |
| 16 | Define line integral? | Remember | 2 |
| 17 | Define surface integral? | Remember | 2 |
| 18 | Define volume integral? | Remember | 2 |
| 19 | State Green's theorem? | Understand | 3 |
| 20 | State Gauss divergence theorem? | Understand | 3 |
| UNIT-II | | | |
| FOURIER SERIES AND FOURIER TRANSFORMS | | | |
| 1 | Define periodic function and write examples | Remember | 5 |
| 2 | Define even and odd function | Remember | 5 |
| 3 | Express the function $f(x)$ as the sum of an even function and an odd function | Understand | 5 |
| 4 | Find the functions are even or odd (i) $x \sin x + \cos x + x^2 \cosh x$ (ii) $x \cosh x + x^3 \sinh x$ | Apply | 5 |
| 5 | If f and g are periodic functions with same period T show that $(af+bg)$ are also periodic function of period T where a and b are real numbers | Understand | 5 |
| 6 | Define Euler's formulae | Remember | 5 |
| 7 | Write Dirichlet's conditions | Understand | 4 |
| 8 | If $f(x) = x^2 - 2$ in $(-2, 2)$ then find b_2 | Apply | 5 |
| 9 | If $f(x) = x^2$ in $(-2, 2)$ then a_0 | Apply | 5 |
| 10 | If $f(x) = \sin^3 x$ in $(-\pi, \pi)$ then find a_n | Apply | 5 |
| 11 | If $f(x) = x^4$ in $(-1, 1)$ then find b_n | Apply | 5 |
| 12 | State Fourier integral theorem | Understand | 6 |
| 13 | Write about Fourier sine and cosine integral | Understand | 6 |
| 14 | Define Fourier transform and finite Fourier transform? | Remember | 6 |
| 15 | Find the Fourier sine transform of $x e^{-ax}$ | Apply | 6 |
| 16 | Find the finite Fourier cosine transform of $f(x) = 1$ in $0 < x < \pi$ | Apply | 6 |
| 17 | Find the finite Fourier sine transform of $f(x) = 2x$ in $(0, \pi)$ | Apply | 6 |
| 18 | Find the inverse finite sine transform $f(x)$ if $F_s(n) = \frac{1 - \cos n\pi}{n^2 \pi^2}$ | Apply | 6 |
| 19 | Write the properties of Fourier transform | Understand | 6 |
| 20 | If finite Fourier sine transform of f is $\frac{2\pi}{n^3}(-1)^{n-1}$ find $f(x)$ | Apply | 6 |
| UNIT-III | | | |
| INTERPOLATION AND CURVE FITTING | | | |
| 1 | Define Interpolation and extrapolation | Remember | 7 |
| 2 | Explain forward difference interpolation | Understand | 7 |
| 3 | Explain backward difference interpolation | Understand | 7 |
| 4 | Explain central difference interpolation | Understand | 7 |
| 5 | Define average operator and shift operator | Remember | 7 |
| 6 | Prove that $\Delta = E - 1$ | Analyze | 9 |
| 7 | Prove that $\nabla = 1 - E^{-1}$ | Analyze | 9 |
| 8 | Prove that $(1+\Delta)(1-\nabla) = 1$ | Analyze | 8 |
| 9 | Construct a forward difference table for $f(x) = x^3 + 5x - 7$ if $x = -1, 0, 1, 2, 3, 4, 5$ | Analyze | 9 |
| 10 | Prove that $\Delta[x(x+1)(x+2)(x+3)] = 4(x+1)(x+2)(x+3)$ | Analyze | 9 |
| 11 | Evaluate $\Delta \log f(x)$ | Understand | 9 |
| 12 | Evaluate $\Delta f(x)g(x)$ | Understand | 9 |
| 13 | Evaluate $\Delta \cos x$ | Understand | 9 |

| S. No | Question | Blooms Taxonomy Level | Course Outcome | | | | | | | | | | | | |
|--|--|-----------------------|----------------|-------|----|---|---|---|---|---|---|-------|----|-------|---|
| 14 | Find the missing term in the following table <table><tr><td>X</td><td>0</td><td>1</td><td>2</td><td>3</td><td>4</td></tr><tr><td>Y</td><td>1</td><td>3</td><td>9</td><td>-----</td><td>81</td></tr></table> | X | 0 | 1 | 2 | 3 | 4 | Y | 1 | 3 | 9 | ----- | 81 | Apply | 8 |
| X | 0 | 1 | 2 | 3 | 4 | | | | | | | | | | |
| Y | 1 | 3 | 9 | ----- | 81 | | | | | | | | | | |
| 15 | What is the principle of method of least square | Understand | 9 | | | | | | | | | | | | |
| 16 | Solve the difference equation $y_{n+2}+5y_{n+1}+6y_n=0$ | Understand | 8 | | | | | | | | | | | | |
| 17 | Derive the normal equations for straight line | Understand | 8 | | | | | | | | | | | | |
| 18 | Derive the normal equations for second degree parabola | Understand | 8 | | | | | | | | | | | | |
| 19 | Explain errors in interpolation | Understand | 9 | | | | | | | | | | | | |
| 20 | Write the normal equations to fit the curve $y = ae^{bx}$ | Understand | 8 | | | | | | | | | | | | |
| UNIT-IV | | | | | | | | | | | | | | | |
| Numerical Techniques | | | | | | | | | | | | | | | |
| 1 | Define algebraic and transcendental equation and give example | Remember | 10 | | | | | | | | | | | | |
| 2 | Explain graphically the root of an equation | Understand | 10 | | | | | | | | | | | | |
| 3 | Write about bisection method | Understand | 10 | | | | | | | | | | | | |
| 4 | Write about false position method | Understand | 10 | | | | | | | | | | | | |
| 5 | Write a short note on iterative method | Understand | 10 | | | | | | | | | | | | |
| 6 | Explain iterative method approach in solving the problems | Understand | 10 | | | | | | | | | | | | |
| 7 | State the condition for convergence of the root by iterative method | Understand | 10 | | | | | | | | | | | | |
| 8 | Derive Newton's Raphson formula | Understand | 10 | | | | | | | | | | | | |
| 9 | Show that Newton's Raphson method is quadratic convergence | Understand | 10 | | | | | | | | | | | | |
| 10 | Establish the formula to find the square root of a number N by Newton's Raphson method | Analyze | 10 | | | | | | | | | | | | |
| 11 | Find the square root of a number 16 by using Newton's Raphson | Apply | 10 | | | | | | | | | | | | |
| 12 | Derive the formula to find the reciprocal of a number | Understand | 10 | | | | | | | | | | | | |
| 13 | Explain solving system of non-homogeneous equations | Understand | 10 | | | | | | | | | | | | |
| 14 | Explain LU decomposition method | Apply | 11 | | | | | | | | | | | | |
| 15 | Define Crout's and Doolittle's method | Remember | 11 | | | | | | | | | | | | |
| 16 | If $A=LU$ and $A = \begin{bmatrix} 1 & 5 \\ 2 & 3 \end{bmatrix}$ then find L | Apply | 11 | | | | | | | | | | | | |
| 17 | Explain the procedure to find the inverse of the matrix by using LU decomposition method | Understand | 11 | | | | | | | | | | | | |
| 18 | Write a short note on Jacobi's method | Understand | 11 | | | | | | | | | | | | |
| 19 | Write a short note on Gauss Seidel iterative method | Understand | 11 | | | | | | | | | | | | |
| 20 | Write the difference between Jacobi's and Gauss Seidel iterative method | Understand | 11 | | | | | | | | | | | | |
| UNIT-V | | | | | | | | | | | | | | | |
| Numerical Integration and Numerical solutions of differential equations | | | | | | | | | | | | | | | |
| 1 | Derive the Newton-cote's quadrature formula | Understand | 12 | | | | | | | | | | | | |
| 2 | Explain Trapezoidal rule | Understand | 12 | | | | | | | | | | | | |
| 3 | Explain Simpson's 1/3 and 3/8 rule | Understand | 12 | | | | | | | | | | | | |
| 4 | Estimate $\int_0^{\pi/2} e^{\sin x} dx$ taking $h=\pi/6$ correct o four decimal places | Understand | 12 | | | | | | | | | | | | |
| 5 | Explain two point and three point Gaussian quadrature | Understand | 12 | | | | | | | | | | | | |
| 6 | Compute using Gauss integral $\int_{-1}^1 \sqrt{1-x^2} dx, n = 3$ | Apply | 12 | | | | | | | | | | | | |
| 7 | Compute using Gauss integral $\int_0^1 x dx, n = 3$ | Apply | 12 | | | | | | | | | | | | |
| 8 | Define initial value problem | Remember | 13 | | | | | | | | | | | | |
| 9 | Define boundary value problem | Remember | 13 | | | | | | | | | | | | |

| S. No | Question | Blooms Taxonomy Level | Course Outcome |
|-------|---|-----------------------|----------------|
| 10 | Explain single step method and step by step method | Understand | 13 |
| 11 | Explain Taylor's series method and limitations | Understand | 13 |
| 12 | Explain Picard's method of successive approximation Write the second approximation for $y' = x^2 + y^2, y(0)=1$ | Understand | 13 |
| 13 | Explain Euler's method | Understand | 13 |
| 14 | Explain Euler's modified method | Understand | 13 |
| 15 | Give the difference between Euler's method and Euler's modified method | Analyze | 13 |
| 16 | Find $y(0.1)$ given $y' = x^2 - y, y(0)=1$ by Euler's method | Apply | 13 |
| 17 | Explain Runge-Kutta second and classical fourth order | Understand | 13 |
| 18 | Write any three properties of Eigen value problems | Understand | 14 |
| 19 | Explain power method to find the largest Eigen value of a matrix | Understand | 14 |
| 20 | Write the finite difference formula for $y'(x), y''(x)$ | Understand | 14 |

1. Group - B (Long Answer Questions)

| S. No | Question | Blooms Taxonomy Level | Course Outcome |
|-----------------------------------|---|-----------------------|----------------|
| UNIT-I VECTOR CALCULUS | | | |
| 1 | Find the constants a and b so that the Surface $ax^2 - byz = (a+z)x$ will be orthogonal to the Surface $4x^2y + z^3 = 4$ at the point $(-1,1,2)$. | Apply | 1 |
| 2 | Prove that $\nabla f(r) = \frac{\bar{r}}{r} \cdot f'(r)$ | Analyze | 1 |
| 3 | Prove that if \bar{r} is the position vector of any point in the space then $r^n \cdot \bar{r}$ is irrotational and is solenoidal if $n = -3$. | Analyze | 1 |
| 4 | Prove that $\text{div}(r^n \cdot \bar{r}) = (n+3)r^n$. Hence Show that $\frac{\bar{r}}{r^3}$ is solenoidal Vector | Analyze | 1 |
| 5 | If $\bar{F} = (5xy - 6x^2)\bar{i} + (2y - 4x)\bar{j}$ evaluate $\int_C \bar{F} \cdot d\bar{r}$ along the curve C in xy plane $y=x^3$ from $(1,1)$ to $(2,8)$. | Understand | 2 |
| 6 | Evaluate the line integral $\int_c (x^2 + xy)dx + (x^2 + y^2)dy$ where c is the square formed by the lines $y = \pm 1$ and $x = \pm 1$ | Understand | 2 |
| 7 | Evaluate $\iint_S \bar{A} \cdot \bar{n} ds$ where $\bar{A} = Z\bar{i} + x\bar{j} - 3y^2z\bar{k}$ and S is the surface of the cylinder $x^2 + y^2 = 16$ included in the first octant between $Z=0$ and $Z=5$ | Understand | 2 |
| 8 | If $\bar{F} = (x^2 - 27)\bar{i} - 6yz\bar{j} + 8xz^2\bar{k}$ evaluate $\int_C \bar{F} \cdot d\bar{r}$ from the point $(0,0,0)$ to the point $(1,1,1)$ along the straight line from $(0,0,0)$ to $(1,0,0)$ then from $(1,0,0)$ to $(1,1,0)$ and then finally from $(1,1,0)$ to $(1,1,1)$ | Understand | 2 |
| 9 | Evaluate $\int_C \bar{f} \cdot d\bar{r}$ where $f = 3xy\bar{i} - y^2\bar{j}$ and C is the parabola $y=2x^2$ from $(0,0)$ to $(1,2)$. | Understand | 2 |
| 10 | Evaluate $\iint_S \bar{F} \cdot \bar{d}\bar{s}$ if $f = yz\bar{i} + 2y^2\bar{j} + xz^2\bar{k}$ and S is the Surface of the Cylinder $x^2 + y^2 = 9$ contained in the first Octant between the planes $z=0$ | Understand | 2 |

| S. No | Question | Blooms Taxonomy Level | Course Outcome |
|--|---|-----------------------|----------------|
| | and $z=2$. | | |
| 11 | Evaluate $\oint_c (yz \, dx + xz \, dy + xy \, dz)$ over arc of a helix $x = a \cos t, y = a \sin t, z = kt$ as t varies from 0 to 2π . | Understand | 2 |
| 12 | Find the circulation of \vec{f} around the curve c Where $\vec{f} = (e^x \sin y)\mathbf{i} + (e^x \cos y)\mathbf{j}$ and c is the rectangle whose vertices are $(0,0), (1,0), (1, \frac{\pi}{2}), (0, \frac{\pi}{2})$ | Apply | 2 |
| 13 | Verify gauss divergence theorem for the vector point function $F = (x^3 - yz)\mathbf{i} - 2yx\mathbf{j} + 2zk$ over the cube bounded by $x=y=z=0$ and $x=y=z=a$ | Apply | 3 |
| 14 | Verify divergence theorem for $2x^2y\mathbf{i} - y^2\mathbf{j} + 4xz^2\mathbf{k}$ taken over the region of first octant of the cylinder $y^2 + z^2 = 9$ and $x = 2$ | Apply | 3 |
| 15 | Verify Green's theorem in the plane for $\int_C (x^2 - xy^3)dx + (y^2 - 2xy)dy$ where C is a square with vertices $(0,0), (2,0), (2,2), (0,2)$. | Apply | 3 |
| 16 | Applying Green's theorem evaluate $\int (y - \sin x)dx + \cos x \, dy$ where C is the plane Δ^e enclosed by $y = 0, y = \frac{2x}{\pi}$, and $x = \frac{\pi}{2}$ | Apply | 3 |
| 17 | Verify Green's Theorem in the plane for $\int_C (x^2 - xy^3)dx + (y^2 - 2xy)dy$ where C is a square with vertices $(0,0), (2,0), (2,2), (0,2)$ | Apply | 3 |
| 18 | Verify Stokes theorem for $f = (2x - y)\mathbf{i} - yz^2\mathbf{j} - y^2z\mathbf{k}$ where S is the upper half surface $x^2 + y^2 + z^2 = 1$ of the sphere and C is its boundary | Apply | 3 |
| 19 | Verify Stokes theorem for $f = (x^2 - y^2)\mathbf{i} + 2xy\mathbf{j}$ over the box bounded by the planes $x=0, x=a, y=0, y=b, z=c$ | Apply | 3 |
| 20 | Evaluate by Stroke's Theorem $\iint_S \text{Curl} \vec{F} \cdot \vec{n} \, ds$ where $\vec{F} = y^2\vec{i} + x^2\vec{j} - (x+Z)\vec{k}$ and S comprising the planes $x=0, y=0, y=4; z=-1$ | Apply | 3 |
| UNIT-II FOURIER SERIES AND FOURIER TRANSFORMS | | | |
| 1 | Obtain the Fourier series expansion of $f(x)$ given that $f(x) = (\pi - x)^2$ in $0 < x < 2\pi$ and deduce the value of $\frac{1}{1^2} + \frac{1}{2^2} + \frac{1}{3^2} + \dots = \frac{\pi^2}{6}$. | Understand | 5 |
| 2 | Obtain Fourier cosine series for $f(x) = x \sin x$ $0 < x < \pi$ and show that $\frac{1}{1.3} - \frac{1}{3.5} + \frac{1}{5.7} - \frac{1}{7.9} + \dots = \frac{\pi - 2}{4}$. | Understand | 5 |
| 3 | Find the Fourier Series to represent the function $f(x) = \sin x $ in $-\pi < x < \pi$. | Apply | 5 |
| 4 | Find the Fourier series to represent $f(x) = x^2$ in $(0, 2\pi)$. | Apply | 5 |
| 5 | Express $f(x) = x$ as a Fourier series in $(-\pi, \pi)$. | Understand | 5 |

| S. No | Question | Blooms Taxonomy Level | Course Outcome |
|-------|--|-----------------------|----------------|
| 6 | If $f(x)=\cosh x$ expand $f(x)$ as a Fourier Series in $(-\pi, \pi)$. | Understand | 5 |
| 7 | Expand the function $f(x) = x^2$ as a Fourier series in $(-\pi, \pi)$. | Understand | 5 |
| 8 | <p>If $f(x) = \begin{cases} x & \text{for } 0 < x < \frac{\pi}{2} \\ \pi - x & \text{for } \frac{\pi}{2} < x < \pi \end{cases}$. Then</p> <p>prove $f(x) = \frac{4}{\pi} \left[\sin x - \frac{1}{3^2} \sin 3x + \frac{1}{5^2} \sin 5x - \dots \right]$.</p> | Apply | 5 |
| 9 | <p>Find the Fourier series to represent the function $f(x)$ given by:</p> $f(x) = \begin{cases} 0 & \text{for } -\pi \leq x \leq 0 \\ x^2 & \text{for } 0 \leq x < \pi \end{cases}$ | Apply | 5 |
| 10 | Find cosine and sine series for $f(x) = \pi - x$ in $[0, \pi]$ | Apply | 5 |
| 11 | Expand $f(x)=\cos x$ for $0 < x < \pi$ in half range sine series | Understand | 5 |
| 12 | Using Fourier integral show that $e^{-x} \cos x = \frac{2}{\pi} \int_0^{\infty} \frac{\lambda^2 + 2}{\lambda^4 + 4} \cos \lambda x dx$ | Understand | 6 |
| 13 | <p>Find the Fourier transform of $f(x)$ defined by</p> $f(x) = \begin{cases} 1 - x^2 & \text{if } x \leq 1 \\ 0 & \text{if } x > 1 \end{cases}$ | Apply | 6 |
| 14 | <p>Find the Fourier transform of $f(x) = \begin{cases} a^2 - x^2 & \text{if } x < a \\ 0 & \text{if } x > a \end{cases}$ Hence</p> <p>show that</p> $\int_0^{\infty} \frac{\sin x - x \cos x}{x^3} dx = \frac{\pi}{4}$ | Apply | 6 |
| 15 | <p>Find the Fourier sine transform for the function $f(x)$ given by</p> $f(x) = \begin{cases} \sin x, & 0 < x < a \\ 0 & x \geq a \end{cases}$ | Apply | 6 |
| 16 | Find the finite Fourier sine and cosine transforms of $f(x) = \sin ax$ in $(0, \pi)$. | Apply | 6 |
| 17 | Find the finite Fourier sine and cosine transforms of $f(x) = \frac{e^{-ax} - e^{-bx}}{x}$ | Apply | 6 |
| 18 | Find the inverse Fourier cosine transform $f(x)$ of $F_c(p) = p^n e^{-ap}$ and inverse Fourier sine transform $f(x)$ of $F_s(p) = \frac{p}{1+p^2}$ | Apply | 6 |
| 19 | Find the inverse Fourier transform $f(x)$ of $F(p) = e^{- p y}$ | Apply | 6 |
| 20 | Evaluate using Parseval's identity $\int_0^{\infty} \frac{x^2}{(a^2 + x^2)^2} dx \ (a > 0)$ | Understand | 6 |

| S. No | Question | Blooms Taxonomy Level | Course Outcome | | | | | | | | | | | | | | |
|---------------------------------|--|-----------------------|----------------|----------|----------|------|------|----------------|------|----------|----------|----------|----------|------------|-----|-------|---|
| UNIT-III | | | | | | | | | | | | | | | | | |
| INTERPOLATION AND CURVE FITTING | | | | | | | | | | | | | | | | | |
| 1 | Find the interpolation polynomial for the following data using Newton's forward interpolation formula. <table><tr><td>x</td><td>2.4</td><td>3.2</td><td>4.0</td><td>4.8</td><td>5.6</td></tr><tr><td>f(x)</td><td>22</td><td>17. 8</td><td>14. 2</td><td>38. 3</td><td>51. 7</td></tr></table> | x | 2.4 | 3.2 | 4.0 | 4.8 | 5.6 | f(x) | 22 | 17. 8 | 14. 2 | 38. 3 | 51. 7 | Apply | 8 | | |
| x | 2.4 | 3.2 | 4.0 | 4.8 | 5.6 | | | | | | | | | | | | |
| f(x) | 22 | 17. 8 | 14. 2 | 38. 3 | 51. 7 | | | | | | | | | | | | |
| 2 | Use Newton's forward difference formula to find the polynomial satisfied by (0,5), (1,12),(2,37) and (3,86). | Apply | 8 | | | | | | | | | | | | | | |
| 3 | <table><tr><td>x</td><td>20</td><td>25</td><td>30</td><td>35</td><td>40</td><td>45</td></tr><tr><td>y</td><td>354</td><td>332</td><td>291</td><td>260</td><td>231</td><td>204</td></tr></table> Find f(22), from the following data using Newton's Backward formula. | x | 20 | 25 | 30 | 35 | 40 | 45 | y | 354 | 332 | 291 | 260 | 231 | 204 | Apply | 8 |
| x | 20 | 25 | 30 | 35 | 40 | 45 | | | | | | | | | | | |
| y | 354 | 332 | 291 | 260 | 231 | 204 | | | | | | | | | | | |
| 4 | Given sin 45=0.7071,sin 50=0.7660,sin 55=0.8192 and sin 60=0.8660 find sin 52 using newton's formula | Apply | 8 | | | | | | | | | | | | | | |
| 5 | The population of a town in the decimal census was given below. Estimate the population for the year 1895 <table><tr><td>Year (x)</td><td>1891</td><td>1901</td><td>1911</td><td>1921</td><td>1931</td></tr><tr><td>Population (y)</td><td>46</td><td>66</td><td>81</td><td>93</td><td>101</td></tr></table> | Year (x) | 1891 | 1901 | 1911 | 1921 | 1931 | Population (y) | 46 | 66 | 81 | 93 | 101 | Understand | 8 | | |
| Year (x) | 1891 | 1901 | 1911 | 1921 | 1931 | | | | | | | | | | | | |
| Population (y) | 46 | 66 | 81 | 93 | 101 | | | | | | | | | | | | |
| 6 | Find y(25) given that y(20)=24, y(24)=32, y(28)=35, y(32)=40, using Gauss forward difference formula. | Apply | 8 | | | | | | | | | | | | | | |
| 7 | Find by Gauss's backward interpolating formula the value of y at x = 1936 using the following table <table><tr><td>X</td><td>1901</td><td>1911</td><td>1921</td><td>1931</td><td>1941</td><td>1951</td></tr><tr><td>Y</td><td>12</td><td>15</td><td>20</td><td>27</td><td>39</td><td>52</td></tr></table> | X | 1901 | 1911 | 1921 | 1931 | 1941 | 1951 | Y | 12 | 15 | 20 | 27 | 39 | 52 | Apply | 8 |
| X | 1901 | 1911 | 1921 | 1931 | 1941 | 1951 | | | | | | | | | | | |
| Y | 12 | 15 | 20 | 27 | 39 | 52 | | | | | | | | | | | |
| 8 | Find by Gauss's backward interpolating formula the value of y at x = 8 using the following table <table><tr><td>X</td><td>0</td><td>5</td><td>10</td><td>15</td><td>20</td><td>25</td></tr><tr><td>y</td><td>7</td><td>11</td><td>14</td><td>18</td><td>24</td><td>32</td></tr></table> | X | 0 | 5 | 10 | 15 | 20 | 25 | y | 7 | 11 | 14 | 18 | 24 | 32 | Apply | 8 |
| X | 0 | 5 | 10 | 15 | 20 | 25 | | | | | | | | | | | |
| y | 7 | 11 | 14 | 18 | 24 | 32 | | | | | | | | | | | |
| 9 | Using Lagrange's formula find y(6) given <table><tr><td>x</td><td>3</td><td>5</td><td>7</td><td>9</td><td>11</td></tr><tr><td>y</td><td>6</td><td>24</td><td>58</td><td>108</td><td>74</td></tr></table> | x | 3 | 5 | 7 | 9 | 11 | y | 6 | 24 | 58 | 108 | 74 | Apply | 8 | | |
| x | 3 | 5 | 7 | 9 | 11 | | | | | | | | | | | | |
| y | 6 | 24 | 58 | 108 | 74 | | | | | | | | | | | | |
| 10 | Find f (1.6) using Lagrange's formula from the following table. <table><tr><td>x</td><td>1.2</td><td>2.0</td><td>2.5</td><td>3.0</td></tr><tr><td>f(x)</td><td>1.36</td><td>0.58</td><td>0.34</td><td>0.20</td></tr></table> | x | 1.2 | 2.0 | 2.5 | 3.0 | f(x) | 1.36 | 0.58 | 0.34 | 0.20 | Apply | 8 | | | | |
| x | 1.2 | 2.0 | 2.5 | 3.0 | | | | | | | | | | | | | |
| f(x) | 1.36 | 0.58 | 0.34 | 0.20 | | | | | | | | | | | | | |
| 11 | Find y(5) given that y(0)=1, y(1)=3, y(3)=13 and y(8) =123 using Lagrange's formula | Apply | 8 | | | | | | | | | | | | | | |
| 12 | Find y(10), given that y(5)=12, y(6)=13, y(9)=14, y(11)=16 using Lagrange's formula | Apply | 8 | | | | | | | | | | | | | | |
| 13 | A curve passes through the points (0, 18),(1,10), (3,-18) and (6,90). Find the slope of the curve at x = 2. | Apply | 7 | | | | | | | | | | | | | | |
| 14 | By the method of least square, find the straight line that best fits the following data: <table><tr><td>x</td><td>1</td><td>2</td><td>3</td><td>4</td><td>5</td></tr><tr><td>y</td><td>14</td><td>27</td><td>40</td><td>55</td><td>68</td></tr></table> | x | 1 | 2 | 3 | 4 | 5 | y | 14 | 27 | 40 | 55 | 68 | Apply | 7 | | |
| x | 1 | 2 | 3 | 4 | 5 | | | | | | | | | | | | |
| y | 14 | 27 | 40 | 55 | 68 | | | | | | | | | | | | |
| 15 | Fit a straight line y=a +bx from the following data: <table><tr><td>x</td><td>0</td><td>1</td><td>2</td><td>3</td><td>4</td></tr><tr><td>y</td><td>1</td><td>1.8</td><td>3.3</td><td>4.5</td><td>6.3</td></tr></table> | x | 0 | 1 | 2 | 3 | 4 | y | 1 | 1.8 | 3.3 | 4.5 | 6.3 | Understand | 7 | | |
| x | 0 | 1 | 2 | 3 | 4 | | | | | | | | | | | | |
| y | 1 | 1.8 | 3.3 | 4.5 | 6.3 | | | | | | | | | | | | |

| S. No | Question | Blooms Taxonomy Level | Course Outcome | | | | | | | | | | | | | | |
|----------------------|--|-----------------------|----------------|-------|-------|--------|-----|-----|-----|------|-------|-------|-------|------|-------|-------|--------|
| 16 | Fit a straight line to the form $y=a+bx$ for the following data: | Understand | 7 | | | | | | | | | | | | | | |
| | <table><tr><td>x</td><td>0</td><td>5</td><td>10</td><td>15</td><td>20</td><td>25</td></tr><tr><td>y</td><td>12</td><td>15</td><td>17</td><td>22</td><td>24</td><td>30</td></tr></table> | | | x | 0 | 5 | 10 | 15 | 20 | 25 | y | 12 | 15 | 17 | 22 | 24 | 30 |
| | x | | | 0 | 5 | 10 | 15 | 20 | 25 | | | | | | | | |
| y | 12 | 15 | 17 | 22 | 24 | 30 | | | | | | | | | | | |
| | | | | | | | | | | | | | | | | | |
| 17 | By the method of least squares, fit a second degree polynomial $y=a+bx+cx^2$ to the following data. | Understand | 7 | | | | | | | | | | | | | | |
| | <table><tr><td>x</td><td>2</td><td>4</td><td>6</td><td>8</td></tr><tr><td>y</td><td>3.07</td><td>12.85</td><td>31.47</td><td>57.38</td></tr></table> | | | x | 2 | 4 | 6 | 8 | y | 3.07 | 12.85 | 31.47 | 57.38 | | | | |
| | x | | | 2 | 4 | 6 | 8 | | | | | | | | | | |
| y | 3.07 | 12.85 | 31.47 | 57.38 | | | | | | | | | | | | | |
| | | | | | | | | | | | | | | | | | |
| 18 | Fit a curve $y=a+bx+cx^2$ from the following data | Understand | 7 | | | | | | | | | | | | | | |
| | <table><tr><td>X</td><td>1</td><td>2</td><td>3</td><td>4</td></tr><tr><td>Y</td><td>6</td><td>11</td><td>18</td><td>27</td></tr></table> | | | X | 1 | 2 | 3 | 4 | Y | 6 | 11 | 18 | 27 | | | | |
| | X | | | 1 | 2 | 3 | 4 | | | | | | | | | | |
| Y | 6 | 11 | 18 | 27 | | | | | | | | | | | | | |
| | | | | | | | | | | | | | | | | | |
| 19 | Using the method of least squares find the constants a and b such that $y=ae^{bx}$ fits the following data: | Apply | 7 | | | | | | | | | | | | | | |
| | <table><tr><td>x</td><td>0</td><td>0.5</td><td>1</td><td>1.5</td><td>2</td><td>2.5</td></tr><tr><td>y</td><td>0.10</td><td>0.45</td><td>2.15</td><td>9.15</td><td>40.35</td><td>180.75</td></tr></table> | | | x | 0 | 0.5 | 1 | 1.5 | 2 | 2.5 | y | 0.10 | 0.45 | 2.15 | 9.15 | 40.35 | 180.75 |
| | x | | | 0 | 0.5 | 1 | 1.5 | 2 | 2.5 | | | | | | | | |
| y | 0.10 | 0.45 | 2.15 | 9.15 | 40.35 | 180.75 | | | | | | | | | | | |
| | | | | | | | | | | | | | | | | | |
| 20 | Obtain a relation of the form $y=ab^x$ for the following data by the method of least squares. | Understand | 7 | | | | | | | | | | | | | | |
| | <table><tr><td>x</td><td>2</td><td>3</td><td>4</td><td>5</td><td>6</td></tr><tr><td>y</td><td>8.3</td><td>15.4</td><td>33.1</td><td>65.2</td><td>127.4</td></tr></table> | | | x | 2 | 3 | 4 | 5 | 6 | y | 8.3 | 15.4 | 33.1 | 65.2 | 127.4 | | |
| | x | | | 2 | 3 | 4 | 5 | 6 | | | | | | | | | |
| y | 8.3 | 15.4 | 33.1 | 65.2 | 127.4 | | | | | | | | | | | | |
| | | | | | | | | | | | | | | | | | |
| UNIT-IV | | | | | | | | | | | | | | | | | |
| NUMERICAL TECHNIQUES | | | | | | | | | | | | | | | | | |
| 1 | Find the real root of the equation $x^3-x-4=0$ by bisection method. | Apply | 10 | | | | | | | | | | | | | | |
| 2 | Find the real root of the equation $3x=e^x$ by bisection method. | Apply | 10 | | | | | | | | | | | | | | |
| 3 | Find the square root of 25 up to 2 decimal place s by using bisection method | Apply | 10 | | | | | | | | | | | | | | |
| 4 | Find a real root of the equation $e^x \sin x= 1$, using Regulafalsi method | Apply | 10 | | | | | | | | | | | | | | |
| 5 | Solve $xe^x=1$ by iterative method | Understand | 10 | | | | | | | | | | | | | | |
| 6 | Solve $2x=\cos x+3$ by iterative method | Understand | 10 | | | | | | | | | | | | | | |
| 7 | Find a real root of the equation, $\log x = \cos x$ using Regulafalsi method | Apply | 10 | | | | | | | | | | | | | | |
| 8 | Use the method of false position to find the fourth root of 32 correct to three decimal places | Apply | 10 | | | | | | | | | | | | | | |
| 9 | Find a real root of the equation $3x-\cos x-1=0$ using Newton Raphson method | Apply | 10 | | | | | | | | | | | | | | |
| 10 | Find a real root of the equation $e^x \sin x=1$, using Newton Raphson method. | Apply | 10 | | | | | | | | | | | | | | |
| 11 | Using Newton's iterative method find the real root of $x \log_{10} x = 1.2$ correct to four decimal places | Apply | 10 | | | | | | | | | | | | | | |
| 12 | Evaluate $x \tan x+1=0$ by Newton Raphson method. | Understand | 10 | | | | | | | | | | | | | | |
| 13 | Find the square root of 28 by Newton Raphson method. | Apply | 10 | | | | | | | | | | | | | | |
| 14 | Solve $x+3y+8z=4$, $x+4y+3z=-2$, $x+3y+4z=1$ using LU decomposition | Understand | 11 | | | | | | | | | | | | | | |
| 15 | Solve by LU decomposition method $x+y+z=9$, $2x-3y+4z=13$, $3x+4y+5z=40$ | Understand | 11 | | | | | | | | | | | | | | |
| 16 | Find the inverse of the matrix $\begin{bmatrix} 3 & 2 & 1 \\ 2 & 3 & 2 \\ 1 & 2 & 2 \end{bmatrix}$ by LU decomposition method | Apply | 11 | | | | | | | | | | | | | | |
| 17 | Solve $5x-y+3z=10$, $3x+6y=18$, $x+y+5z=-10$ with initial approximations (3,0,-2) by Jacobi's iteration method | Understand | 11 | | | | | | | | | | | | | | |

| S. No | Question | Blooms Taxonomy Level | Course Outcome |
|--|--|-----------------------|----------------|
| 18 | Using Jacobi's iteration method solve the system of equation $10x+4y-2z=12$, $x-10y-z=-10$, $5x+2y-10z=-3$ | Understand | 11 |
| 19 | Solve $20x+y-2z=17$, $3x+20y-z=-18$, $2x-3y+20z=25$ by Gauss-Seidel iterative method | Understand | 11 |
| 20 | Using Gauss-seidel iterative method solve the system of equations $5x+2y+z=12$, $x+4y+2z=15$, $x+2y+5z=20$ | Understand | 11 |
| UNIT-V | | | |
| NUMERICAL INTEGRATION AND NUMERICAL SOLUTIONS OF DIFFERENTIAL EQUATIONS | | | |
| 1 | Use the trapezoidal rule with $n=4$ to estimate $\int_0^1 \frac{dx}{1+x^2}$ correct to four decimal places | Understand | 12 |
| 2 | Estimate $\int_0^6 \frac{dx}{1+x^2}$ correct to four decimal places | Understand | 12 |
| 3 | Evaluate $\int_0^{\pi} \left(\frac{\sin x}{x} \right) dx$ by using i) Trapezoidal rule ii) Simpson's $\frac{1}{3}$ rule taking $n=6$ | Understand | 12 |
| 4 | Using Taylor's series method, find an approximate value of y at $x=0.2$ for the differential equation $y'-2y = 3e^x$ for $y(0)=0$. | Apply | 13 |
| 5 | Find $y(0.1)$, $y(0.2)$, $z(0.1)$, $z(0.2)$, given $\frac{dy}{dx} = x + z$, $\frac{dz}{dx} = x - y^2$ and $y(0)=2$, $z(0)=1$ by using Taylor's series method | Apply | 13 |
| 6 | Given $y' = 1 + xy$, $y(0) = 1$ compute $y(0.1)$, $y(0.2)$ using Picard's method | Understand | 13 |
| 7 | Find an approximation value of y for $x=0.1, 0.2$ if $\frac{dy}{dx} = x + y$ and $y(0)=1$ using Picard's method and check your answer with exact particular solution | Apply | 13 |
| 8 | Solve by Euler's method $\frac{dy}{dx} = \frac{2y}{x}$ given $y(1)=2$ and find $y(2)$. | Understand | 13 |
| 9 | Using Euler's method, solve for y at $x=2$ from $\frac{dy}{dx} = 3x^2 + 1$, $y(1)=2$ taking step size: $h=0.5$ and $h=0.25$ | Understand | 13 |
| 10 | Given $\frac{dy}{dx} = xy$ and $y(0)=1$. Find $y(0.1)$ using Euler's method | Apply | 13 |
| 11 | Find $y(0.5)$, $y(1)$ and $y(1.5)$ given that $\frac{dy}{dx} = 4 - 2x$ and $y(0)=2$ with $h=0.5$ using modified Euler's method | Apply | 13 |
| 12 | Find $y(0.1)$ and $y(0.2)$ using Euler's modified formula given that $\frac{dy}{dx} = x^2 - y$ and $y(0)=1$ | Apply | 13 |
| 13 | Given $y' = 4-2x$, $y(0)=2$ then find $y(0.5)$, $y(1)$, $y(1.5)$ using Euler's modified formula | Apply | 13 |
| 14 | Find $y(0.1)$ and $y(0.2)$ using Runge Kutta fourth order formula given | Apply | 13 |

| S. No | Question | Blooms Taxonomy Level | Course Outcome |
|-------|---|-----------------------|----------------|
| | that $\frac{dy}{dx} = x + x^2 y$ and $y(0)=1$. | | |
| 15 | Obtain the values y at $x=0.1, 0.2$ using Runge Kutta method of second and fourth order for $y' + y = 0, y(0)=1$ | Understand | 13 |
| 16 | using Runge Kutta method of order 4 find $y(0.2)$ for the equation $\frac{dy}{dx} = \frac{y-x}{y+x}, y(0) = 1, h = 0.2$ | Apply | 13 |
| 17 | Use power method find numerically largest Eigen value $\begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix}$ and corresponding Eigen vector and other Eigen value | Apply | 14 |
| 18 | Use power method find numerically largest Eigen value $\begin{bmatrix} 1 & 6 & 1 \\ 1 & 2 & 0 \\ 0 & 0 & 3 \end{bmatrix}$ | Apply | 14 |
| 19 | Write the largest Eigen value of the matrix $\begin{bmatrix} 25 & 1 & 2 \\ 1 & 3 & 0 \\ 2 & 0 & -4 \end{bmatrix}$ | Understand | 14 |
| 20 | Solve the boundary value problem $y^{(11)} - 2y(x)/x^2 = -5/x, 1 < x < 2, y(1)=1; y(2)=2$; with h value of 0.5 | Understand | 14 |

3. Group - III (Analytical Questions)

| S. No | Questions | Blooms Taxonomy Level | Program Outcome |
|--|---|-----------------------|-----------------|
| UNIT-I | | | |
| VECTOR CALCULUS | | | |
| 1 | If $\vec{r} = x\vec{i} + y\vec{j} + z\vec{k}$ then what is $\Delta^2(\frac{1}{r})$? | Understand | 1 |
| 2 | If $\text{curl } \vec{f} = \vec{0}$ then what is \vec{f} ? | Understand | 1 |
| 3 | If \vec{a} and \vec{b} are irrotational vectors then what is $\vec{a} \times \vec{b}$? | Understand | 1 |
| 4 | What is the physical interpretation of $ \Delta\phi $? | Understand | 1 |
| 5 | If $\text{div } \vec{A} = 0$ then what is called \vec{A} ? | Understand | 1 |
| 6 | What is $\int f \circ g \cdot d\vec{r}$? | Understand | 2 |
| 7 | What is the necessary and sufficient condition for the line integral $\int_c \vec{A} \cdot d\vec{r} = 0$ for every closed curve c ? | Understand | 2 |
| 8 | What is $\int \vec{r} \times \vec{n} dS$? | Understand | 2 |
| 9 | If $\vec{F} = ax\vec{i} + by\vec{j} + cz\vec{k}$ where a, b, c are constants then what is $\iint \vec{F} \cdot \vec{n} dS$ where s is the surface of the unit sphere? | Evaluate | 2 |
| 10 | If $\vec{r} = x\vec{i} + y\vec{j} + z\vec{k}$ then what is $\oint_c \vec{r} \cdot d\vec{r}$? | Understand | 2 |
| UNIT-II | | | |
| FOURIER SERIES AND FOURIER TRANSFORMS | | | |
| 1 | If $f(x)$ is an even function in the interval $-(l, l)$ then what is the value of b_n ? | Understand | 5 |
| 2 | If $f(x) = x$ in $(-\pi, \pi)$ then what is the Fourier coefficient a_2 ? | Understand | 5 |
| 3 | What are the conditions for expansion of a function in Fourier series? | Understand | 4 |
| 4 | If $f(x)$ is an odd function in the interval $-(l, l)$ then what are the | Apply | 5 |

| S. No | Questions | Blooms Taxonomy Level | Program Outcome |
|--|---|-----------------------|-----------------|
| | value of a_0, a_n ? | | |
| 5 | If $f(x) = x^2$ in $-(l, l)$ then what is b_1 ? | Understand | 5 |
| 6 | What is the Fourier sine series for $f(x) = x$ in $(0, \pi)$? | Understand | 5 |
| 7 | What is the half range sine series for $f(x) = e^x$ in $(0, \pi)$? | Understand | 5 |
| 8 | What is the Fourier sine transform of $f(x) = x$? | Understand | 6 |
| 9 | What is the Fourier cosine transform of $f(x)$? | Understand | 6 |
| 10 | What is the $F_c \{e^{-at}\}$? | Understand | 6 |
| UNIT-III | | | |
| INTERPOLATION AND CURVE FITTING | | | |
| 1 | For what values of y the Gauss backward interpolation formula is used to interpolate? | Evaluate | 8 |
| 2 | For what values of y the Gauss forward interpolation formula is used to interpolate? | Evaluate | 8 |
| 3 | What is the difference between interpolation and extrapolation | Understand | 7 |
| 4 | Write a short note on difference equation | Remember | 7 |
| 5 | Write about curve fitting | Remember | 7 |
| 6 | If $y = a + \frac{b}{x}$ is a curve then write it's normal equations | Analyze | 7 |
| 7 | If $y = a_0 + a_1 x + a_2 x^2$ then what is the third normal equation of $\sum x_i^2 y_i$ by least squares method? | Analyze | 7 |
| 8 | If $y = a_0 + a_1 x^2$, then what is the first normal equation of $\sum y_i$? | Analyze | 7 |
| 9 | If $y = ax^b$, then what is the first normal equation of $\sum \log y_i$? | Analyze | 7 |
| 10 | If $y = 2x + 5$ is the best fit for 6 pairs of values (x, y) by the best method of least-squares, find $\sum x_i$ if $\sum y_i = 120$? | Apply | 7 |
| UNIT-IV | | | |
| NUMERICAL TECHNIQUES | | | |
| 1 | What is difference between polynomial and algebraic function? | Understand | 10 |
| 2 | What is Transcendental equation | Understand | 10 |
| 3 | Define root of an equation | Remember | 10 |
| 4 | What are the merits and demerits of Newton-Raphson Method | Understand | 10 |
| 5 | Explain about order of convergence? | Understand | 10 |
| 6 | Define linear, quadratic and cubic convergence? | Remember | 10 |
| 7 | Explain about False-position method | Understand | 10 |
| 8 | Explain about Regula-Falsi method | Understand | 10 |
| 9 | What is Crout's method in LU decomposition | Understand | 11 |
| 10 | What is Dolittle's method in LU decomposition | Understand | 11 |
| UNIT-V | | | |
| NUMERICAL INTEGRATION AND NUMERICAL SOLUTIONS OF DIFFERENTIAL EQUATIONS | | | |
| 1 | How many number of subintervals are required to get accuracy, while evaluating a definite integral by trapezoidal rule? | Analyze | 12 |
| 2 | What is the interval h for closer application, in Simpson's $\frac{1}{3}$ rule? | Analyze | 12 |
| 3 | What is the disadvantage of picard's method? | Understand | 13 |
| 4 | What is the method of Runge-Kutta method? | Understand | 13 |
| | If $y_0 = 1, h = 0.2, f(x_0, y_0) = 1$ then by using Euler's method | Understand | 13 |

| S. No | Questions | Blooms Taxonomy Level | Program Outcome |
|-------|---|-----------------------|-----------------|
| 5 | what is the value of y_1 ? | | |
| 6 | If $y_1 = 1.2, h = 0.2, f(x_1, y_1) = 1.4$ then by using Euler's method what is the value of y_2 ? | Understand | 13 |
| 7 | what is the iterative formula of Euler's method for solving $\frac{dy}{dx} = f(x, y)$ with $y(x_0) = y_0$? | Understand | 13 |
| 8 | What is the n^{th} difference of a polynomial of degree n ? | Understand | 13 |
| 9 | If $\frac{dy}{dx} = x - y$ and $y(0)=1$ then by picards method what is the value of $y^{(1)}(x)$? | Understand | 13 |
| 10 | What is the disadvantage of Euler's method over Modified Euler method? | Understand | 13 |

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Date: 13 June, 2016

HOD, FRESHMAN ENGINEERING